

# Constrained Aero-elastic Multi-Point Optimization Using the Coupled Adjoint Approach

M. Abu-Zurayk

MUSAF II Colloquium

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Knowledge for Tomorrow

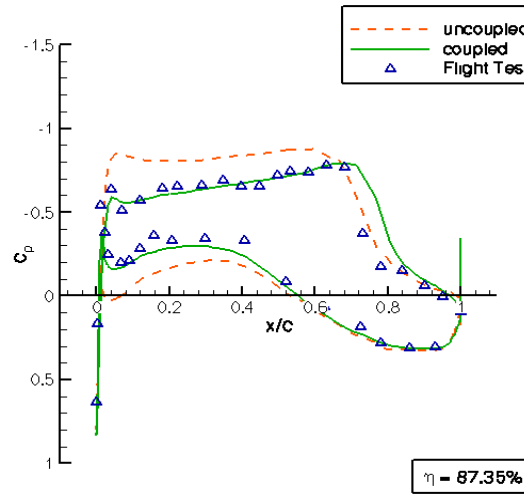
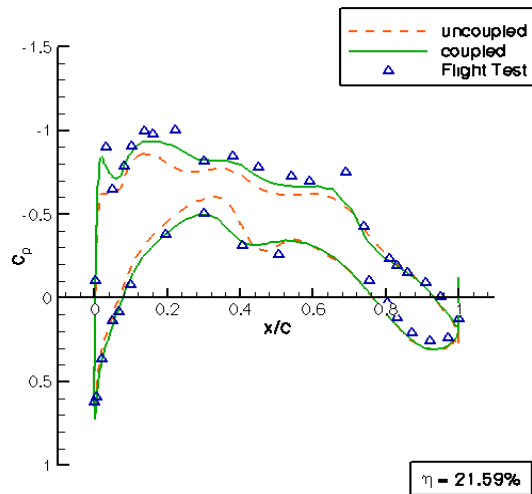
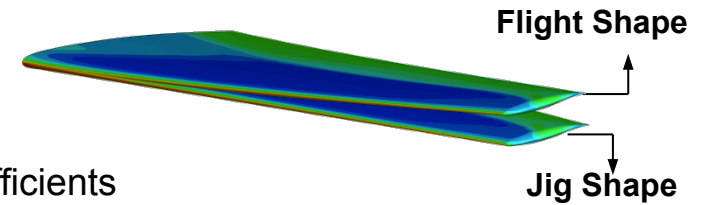
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## Motivation

- During the flight, the wing deforms due to the aero-elastic effects.
- The aero-elastic deformation significantly modifies the wing shape (twist and bending) and impacts the aerodynamic coefficients => need to take them into account in the design phase.

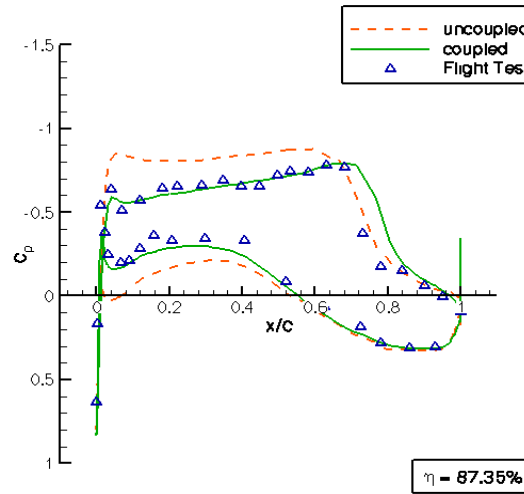
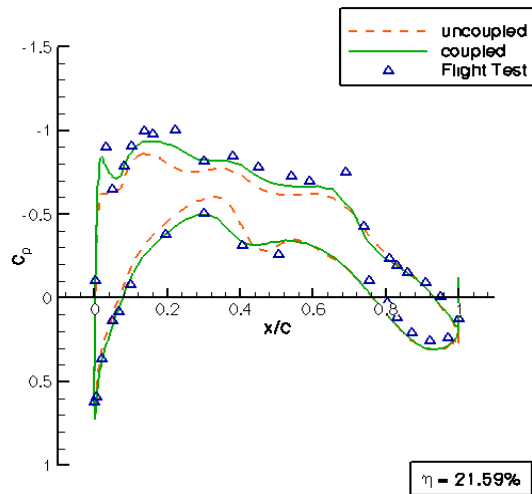
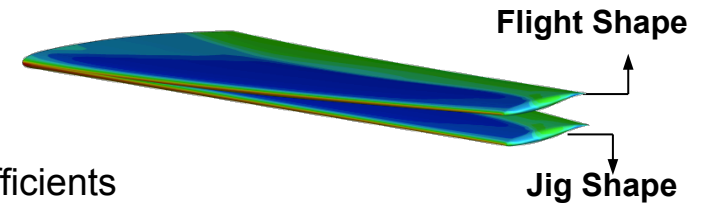


Courtesy of Stefan Keye



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The effect becomes more evident towards the wing tip

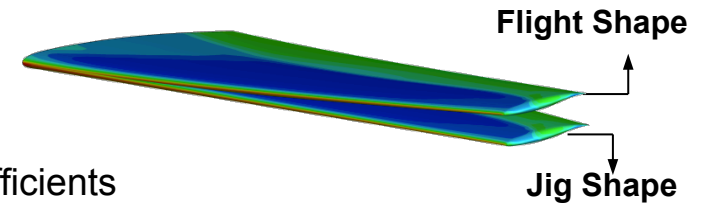
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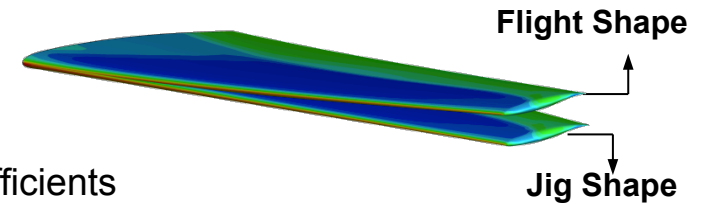
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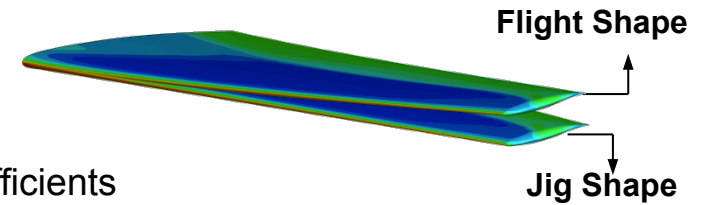
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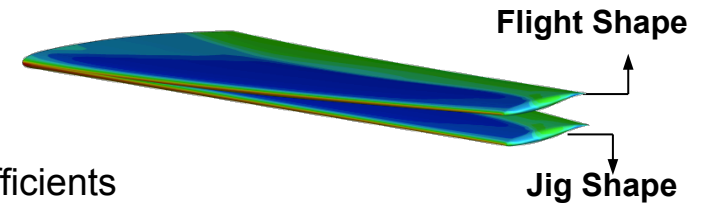
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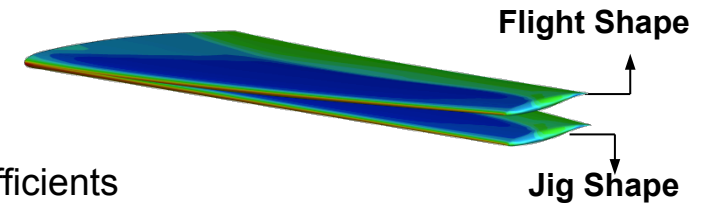


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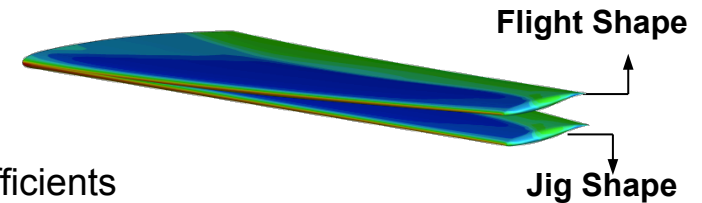
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Aeroelastic deformation is dependent on the flow condition (Mach, lift,...)



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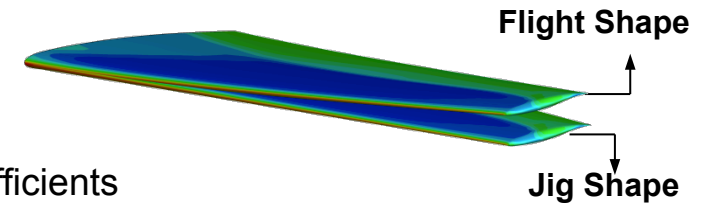
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Aeroelastic deformation is dependent on the flow condition (Mach, lift,...)
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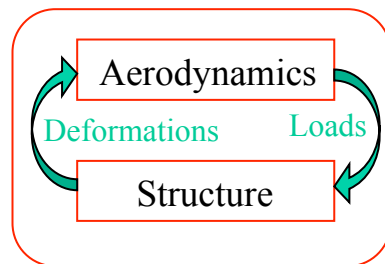


## Motivation

- The aero-elastic equilibrium is obtained after several couplings between aerodynamics and structure and incurs high-computational cost
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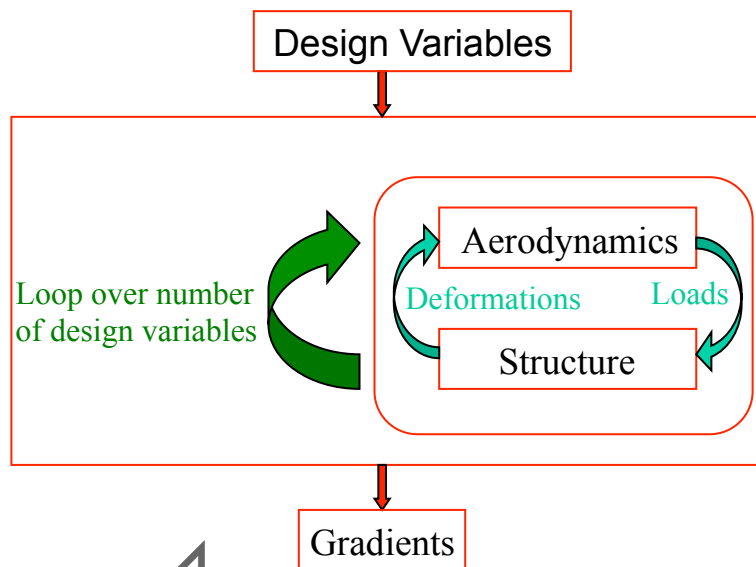
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- Gradient-based optimization algorithms are known to be efficient but computing the gradients is expensive with the standard finite differences approach.

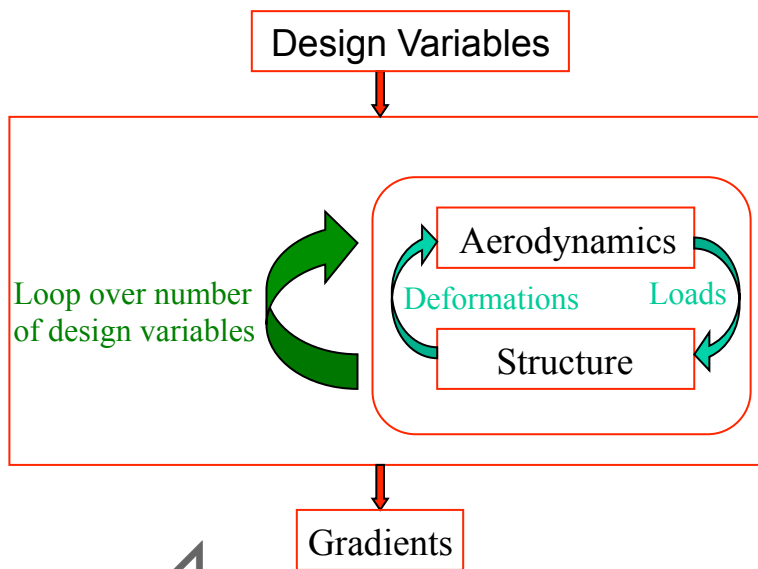
### Traditional Finite Differences Approach



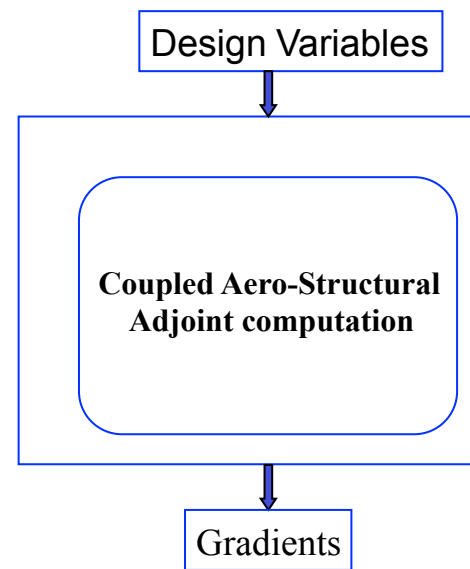
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- Gradient-based optimization algorithms are known to be efficient but computing the gradients is expensive with the standard finite differences approach.  
=> need for an efficient approach to determine the gradients: **the coupled aero-structural adjoint approach**

### Traditional Finite Differences Approach



### Coupled Adjoint Approach



Adjoint approach  
is independent on the  
number of design variables

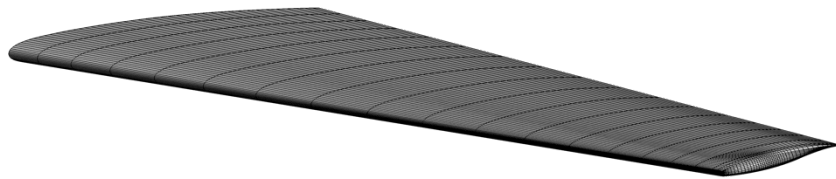


# Formulation of the Coupled Adjoint Approach

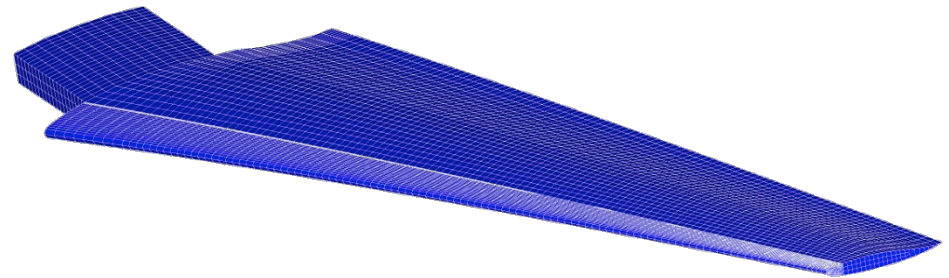


## Components of the Coupled System

- Loose aero-structural coupling is employed at DLR



TAU



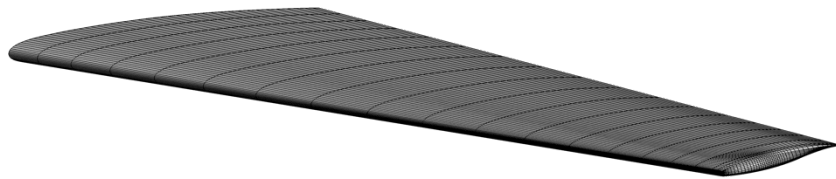
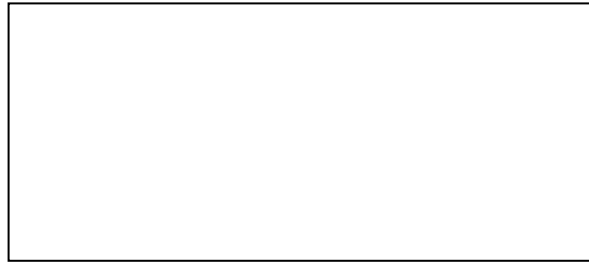
ANSYS



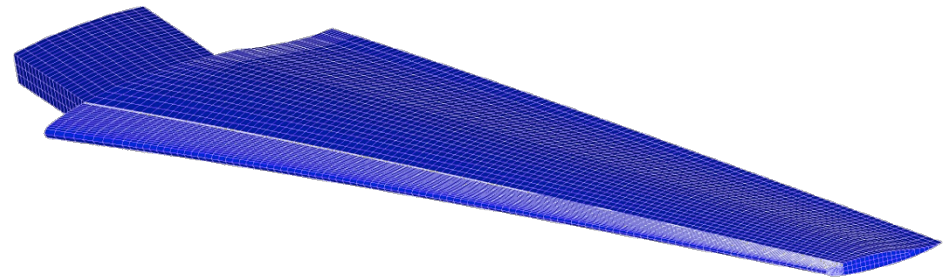


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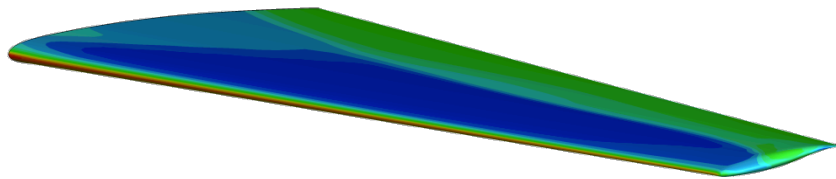


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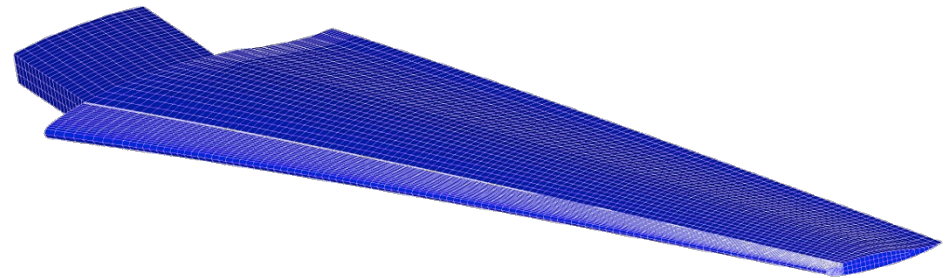


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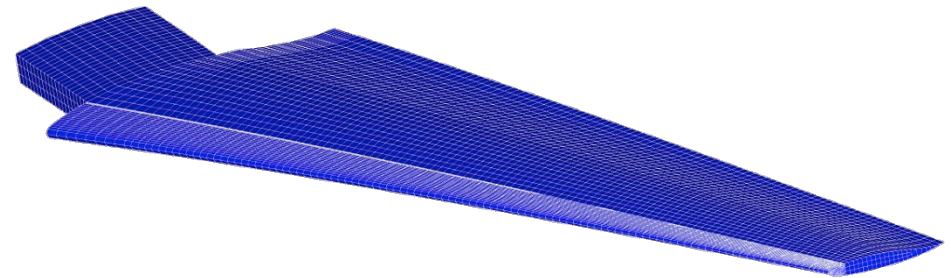
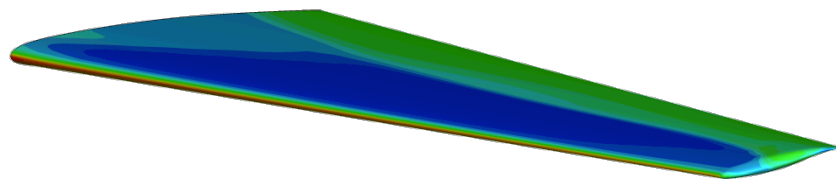


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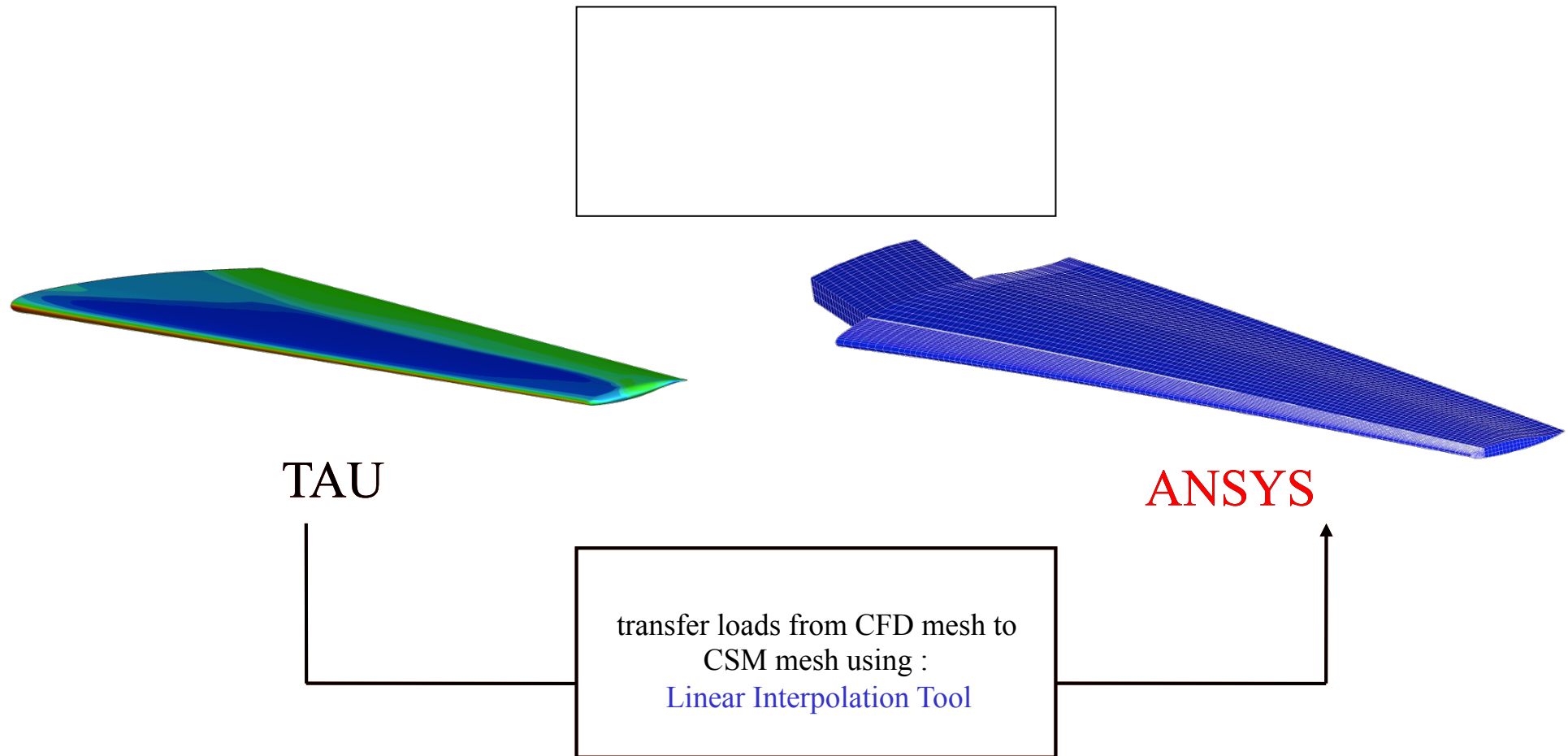
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transfer loads from CFD mesh to  
CSM mesh using :  
**Linear Interpolation Tool**



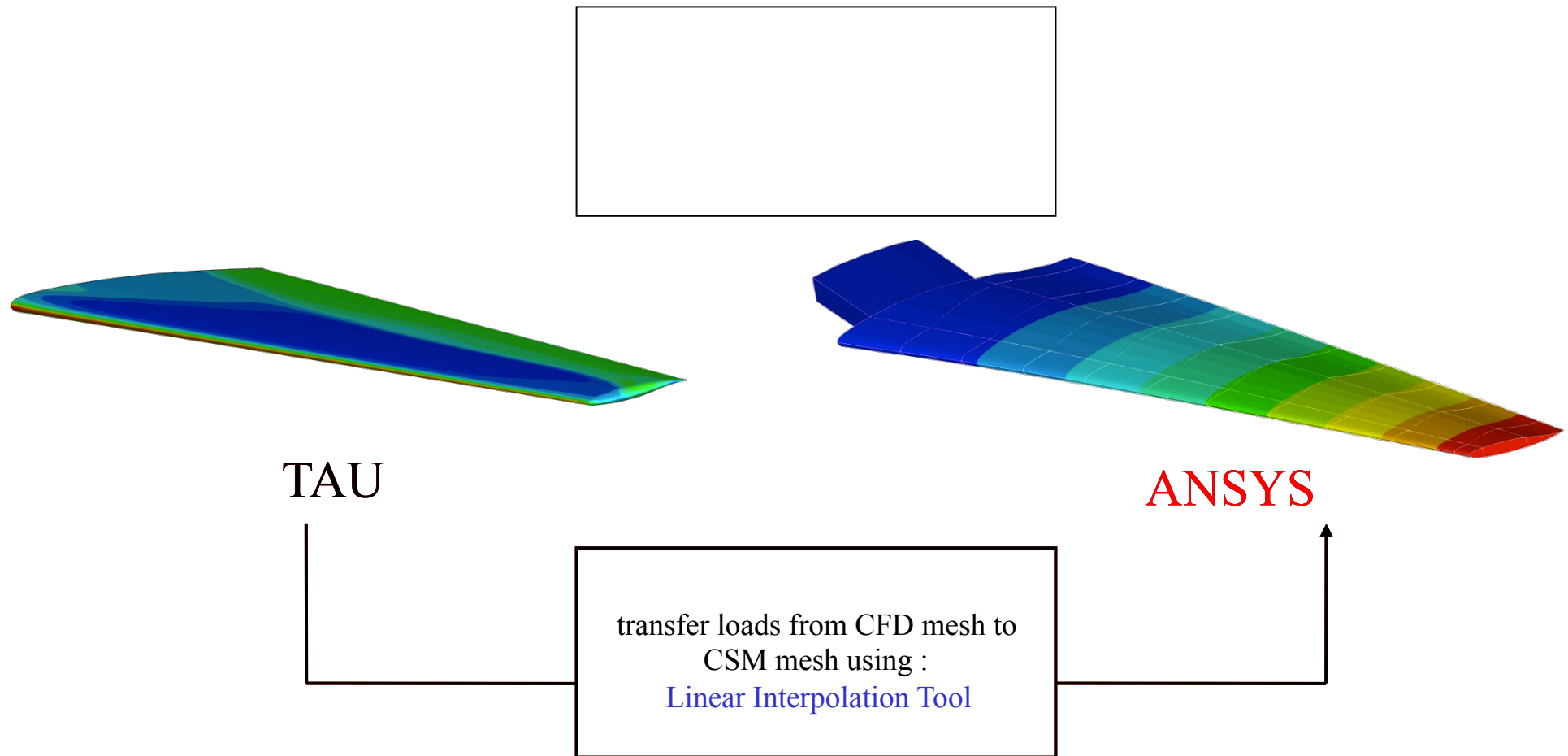
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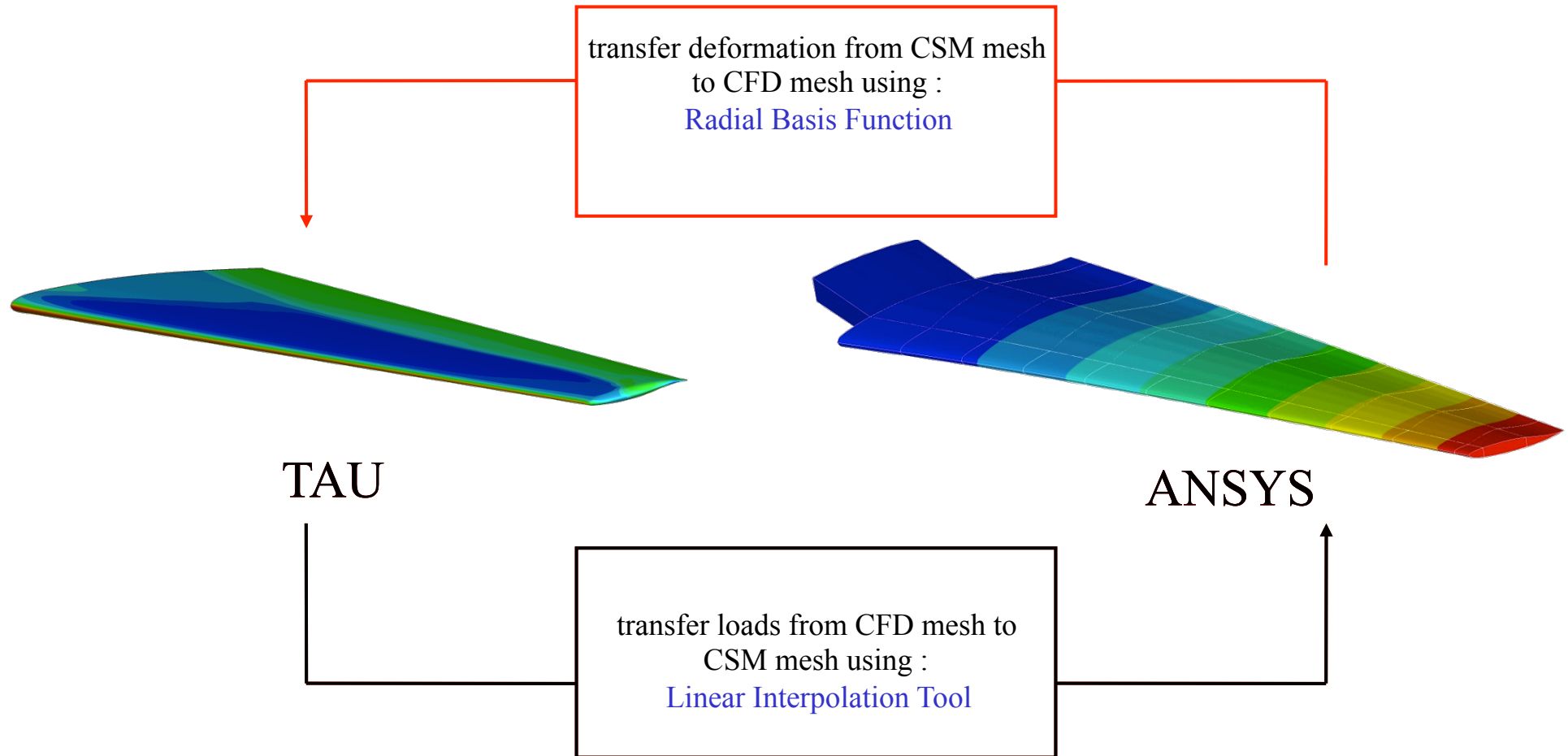
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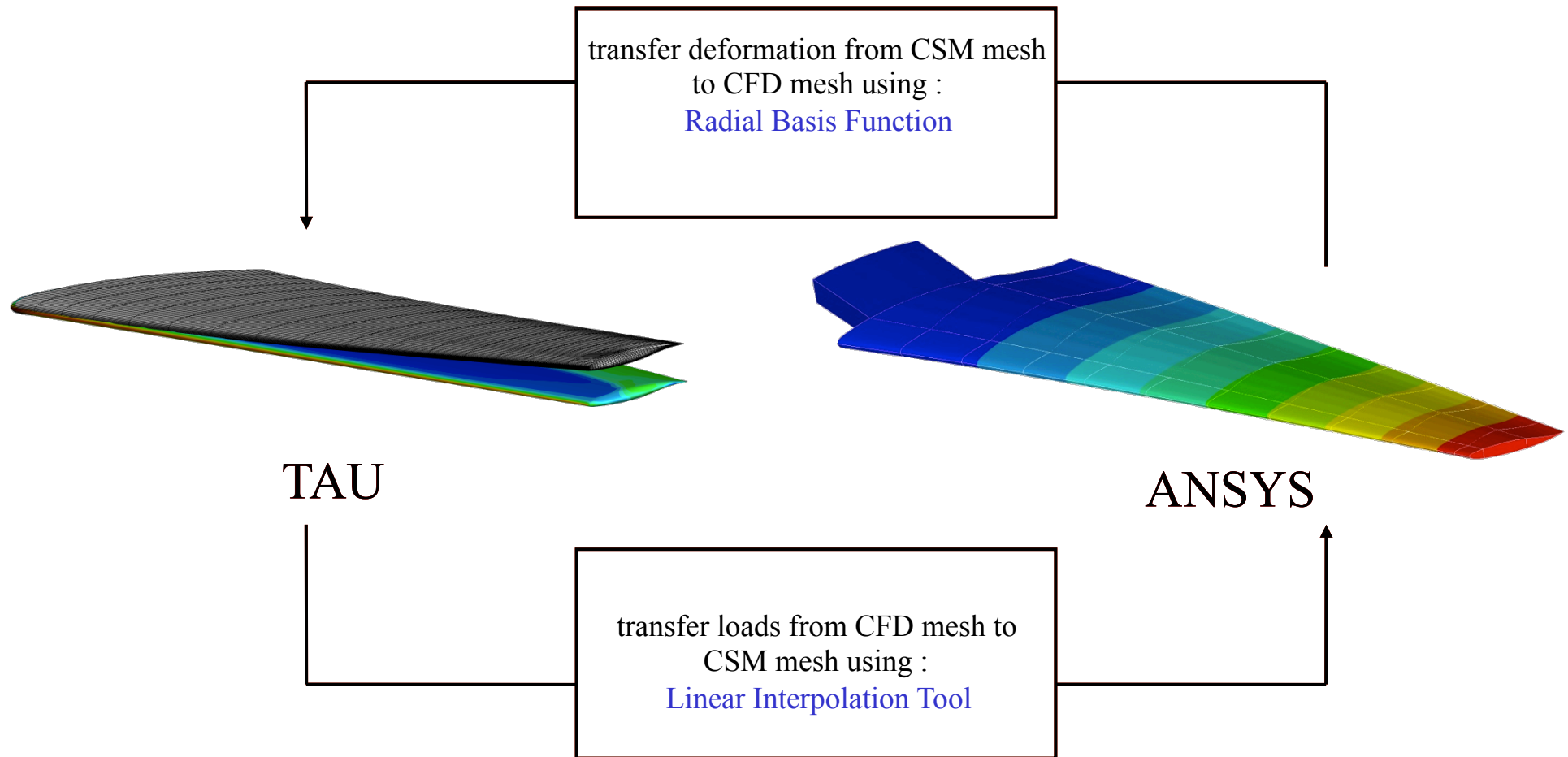
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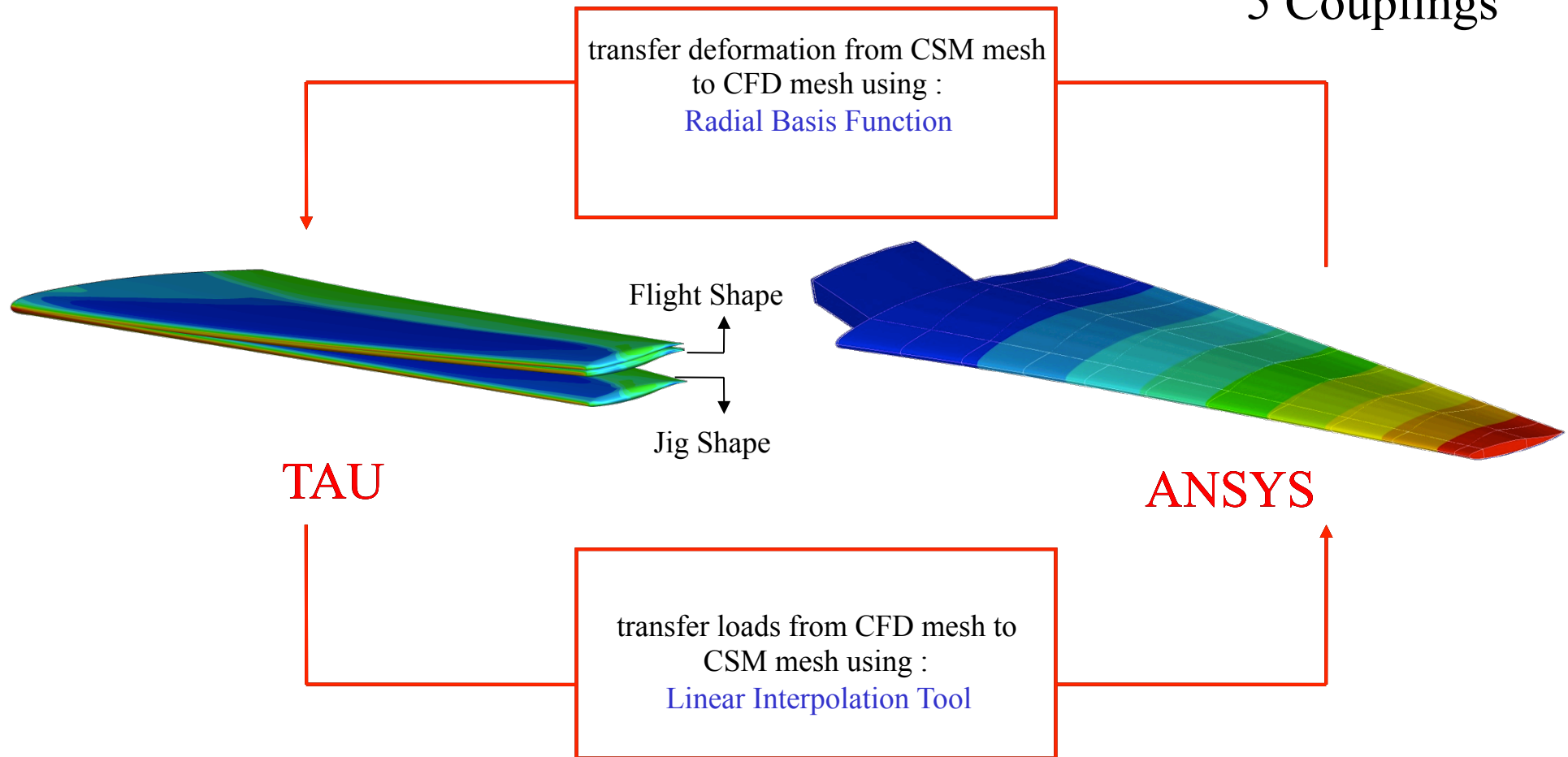
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## Components of the Coupled System

- Loose aero-structural coupling is employed at DLR

5 Couplings



## Formulation of the Coupled Adjoint Equations

- Motivation: Efficient computation of the gradient of a cost function (I) w.r.t the design parameters (D).
- The aero-structural coupled system is defined by:

$$I=I(W,D) ; R=R(W,D)=0$$

- Define the Lagrange:  $L = I + \Psi R$

Residual Vector	$R = \begin{bmatrix} Ra \\ Rs \end{bmatrix}$	Aerodynamic residual Structural residual
State variables Vector	$W = \begin{bmatrix} w \\ u \end{bmatrix}$	Flow variables Structural deformation
Design variables Vector	$D = \begin{bmatrix} A \\ T \end{bmatrix}$	Shape design variables Structural thickness

$$\begin{bmatrix} \frac{\partial \mathbf{Ra}^T}{\partial \mathbf{w}} & \frac{\partial \mathbf{Ra}^T}{\partial \mathbf{u}} \\ \frac{\partial \mathbf{Rs}^T}{\partial \mathbf{w}} & \frac{\partial \mathbf{Rs}^T}{\partial \mathbf{u}} \end{bmatrix} \begin{Bmatrix} \psi_a \\ \psi_s \end{Bmatrix} = - \begin{bmatrix} \frac{\partial I}{\partial \mathbf{w}} \\ \frac{\partial I}{\partial \mathbf{u}} \end{bmatrix}$$

The Coupled Adjoint Equation

$$\left\{ \frac{dI}{d\mathbf{D}} \right\}^T = \left\{ \frac{dL}{d\mathbf{D}} \right\}^T = \left( \begin{bmatrix} \frac{\partial I}{\partial \mathbf{A}} \\ \frac{\partial I}{\partial \mathbf{T}} \end{bmatrix}^T + \begin{Bmatrix} \psi_a \\ \psi_s \end{Bmatrix}^T \begin{bmatrix} \frac{\partial \mathbf{Ra}}{\partial \mathbf{A}} & \frac{\partial \mathbf{Ra}}{\partial \mathbf{T}} \\ \frac{\partial \mathbf{Rs}}{\partial \mathbf{A}} & \frac{\partial \mathbf{Rs}}{\partial \mathbf{T}} \end{bmatrix} \right)$$

The Gradients

Where  $\psi_a$  and  $\psi_s$  are the aerodynamic and the structure Lagrange multipliers.



## Test case description



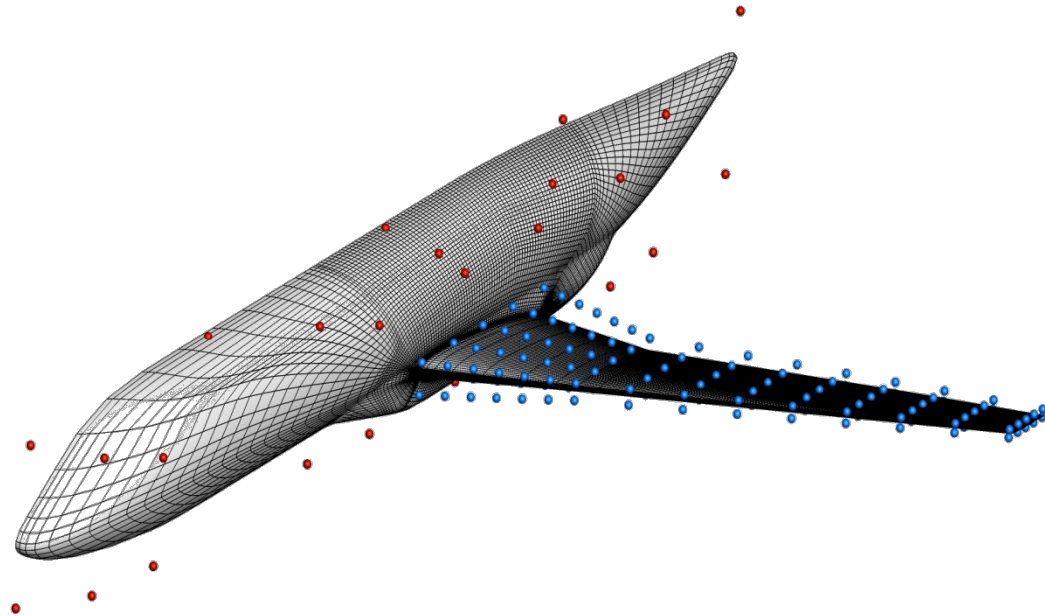
## Test Case Description

- Wing-Body configuration based on the DO728 geometry used as a test case.
- Reynolds number : 21e06
- Lift is kept constant by varying angle of attack (**implicit lift constraint** → requires gradient correction)
  
- **CFD**
- One-Equation turbulence model Spalart-Allmaras
- 
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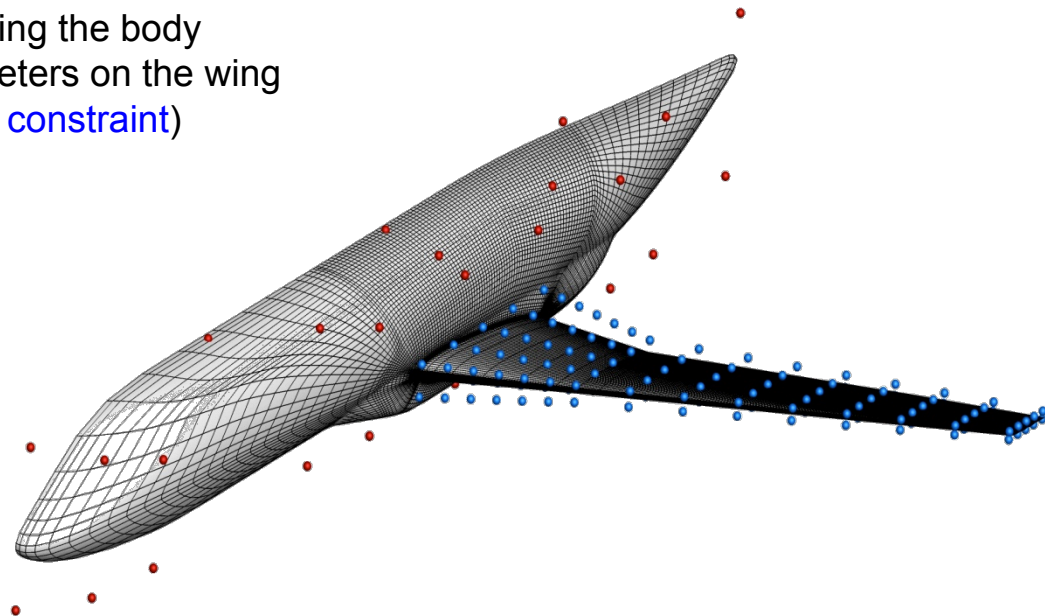
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- CFD structured mesh; 1.2 Million nodes
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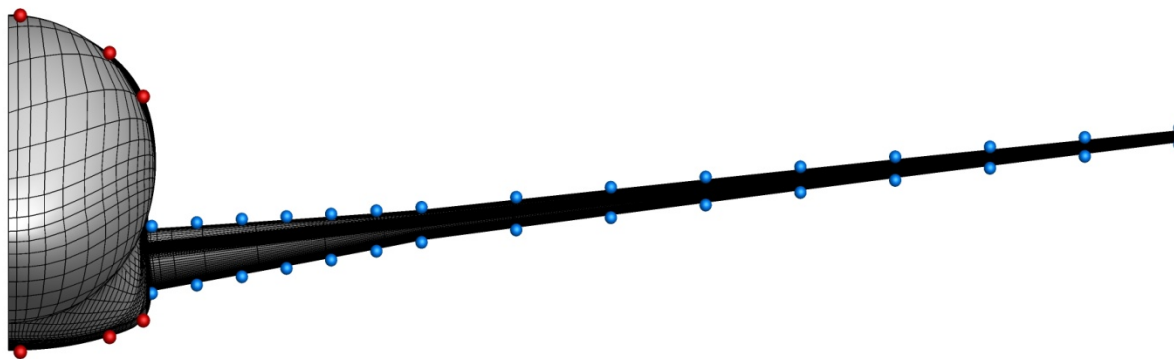
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150/2 FFD parameters on the wing  
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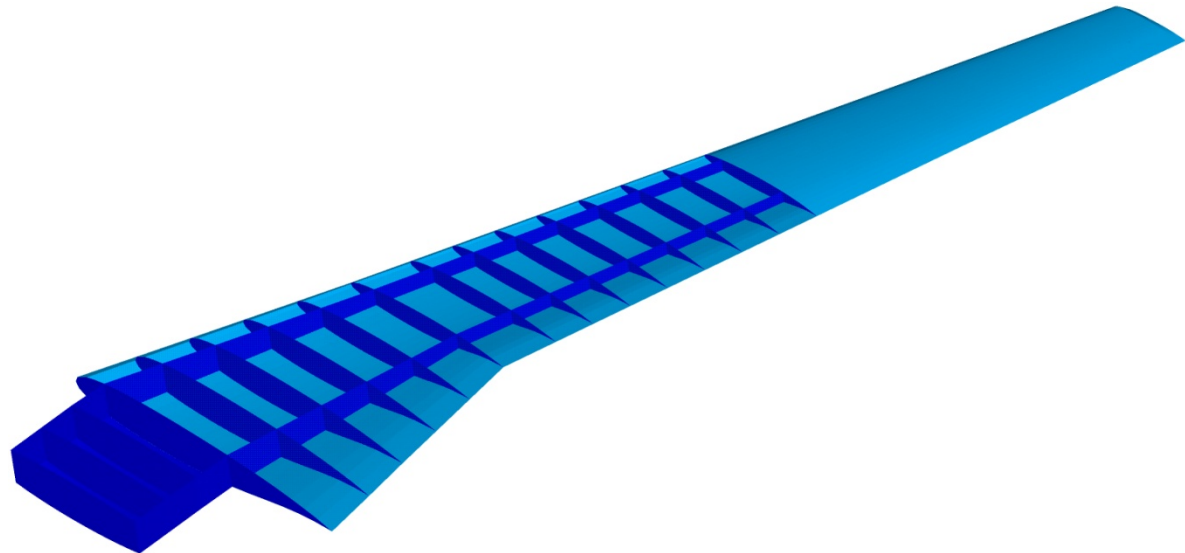
$$\frac{d(C_D)@ \text{constant Lift}}{dA} = \frac{dC_D}{dA} - \left( \frac{dC_D}{d\alpha} / \frac{dC_L}{d\alpha} \right) \frac{dC_L}{dA}$$



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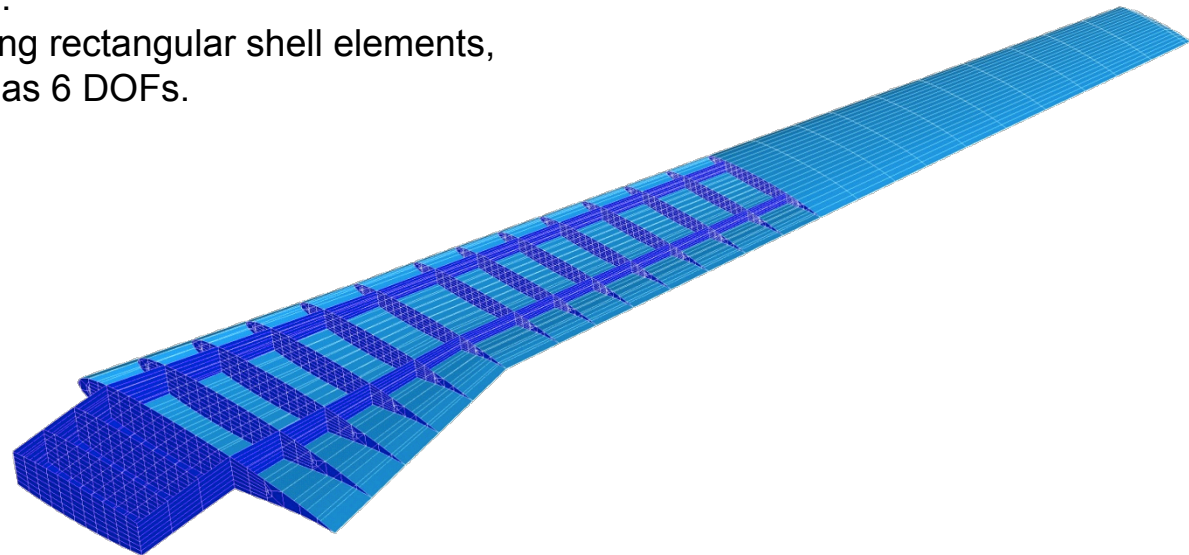
- Wing-Body configuration based on the DO728 geometry used as a test case.
- The Structure model:
  - 27 Ribs
  - 2 Spars
  - Lower & Upper Skin

▪  
▪  
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▪



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- Wing-Body configuration based on the DO728 geometry used as a test case.
- The Structure model:
  - 27 Ribs
  - 2 Spars
  - Lower & Upper Skin
- **CSM**
- The CSM mesh:
  - 4000 nodes.
  - Modeled using rectangular shell elements,
  - each node has 6 DOFs.



# Optimizations



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## Optimizations

➤ Three optimizations were performed

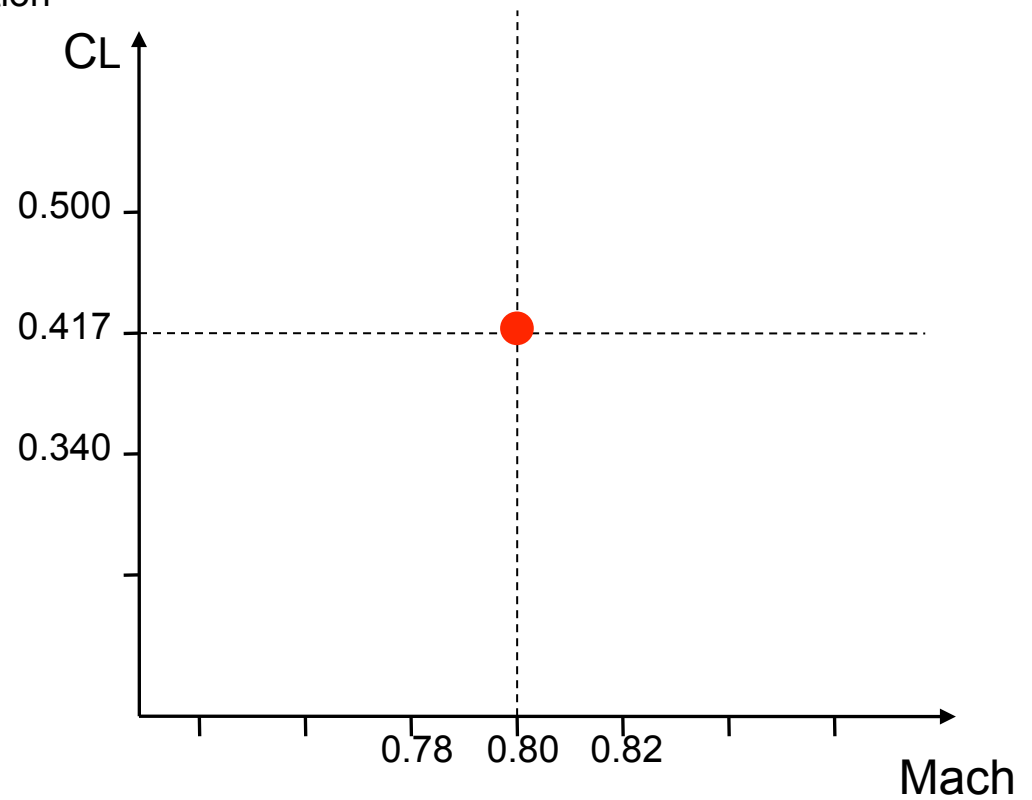
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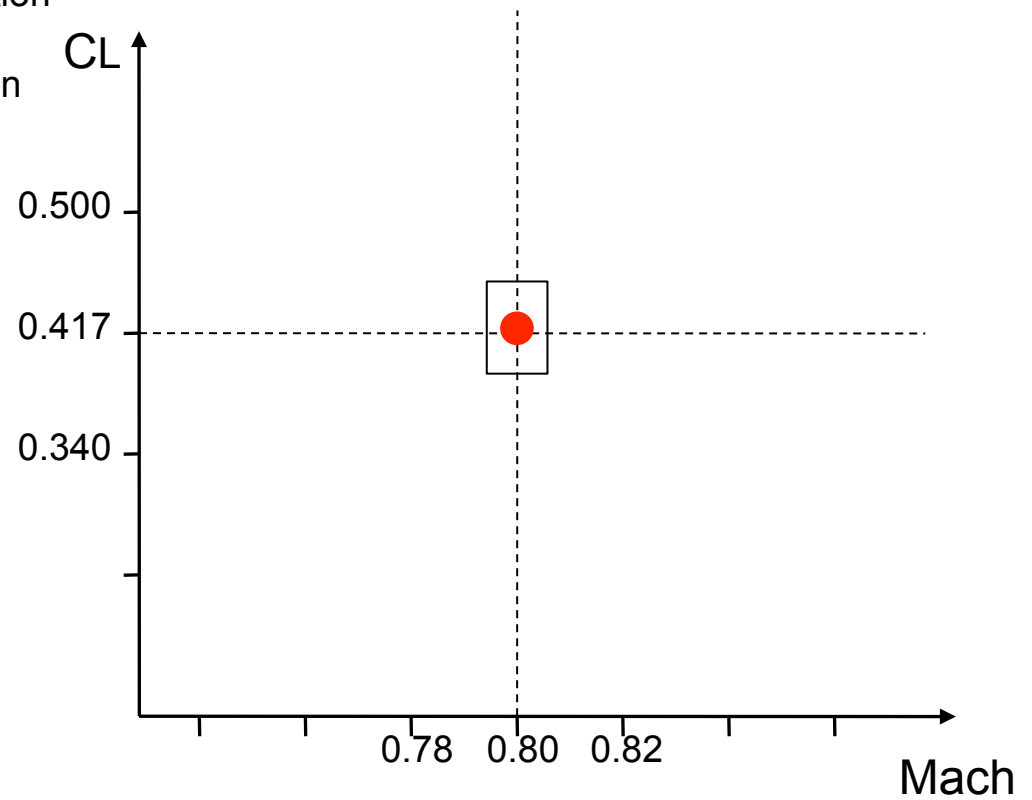
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- 1. Unconstrained Single-point optimization at the design point
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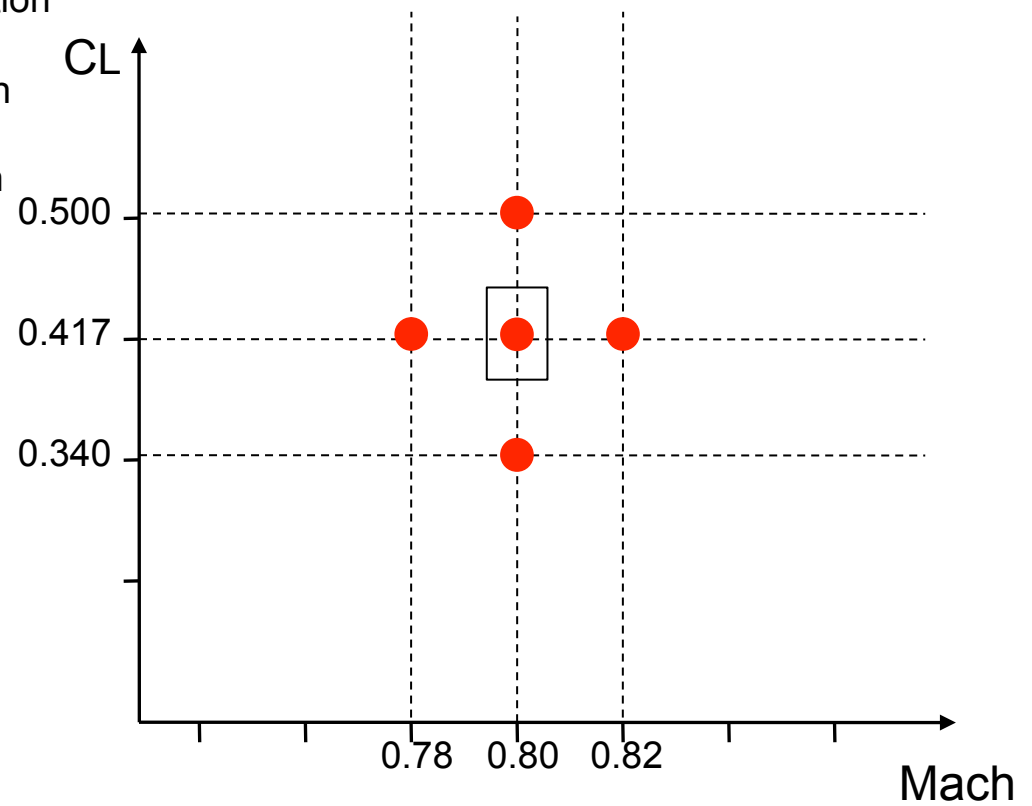
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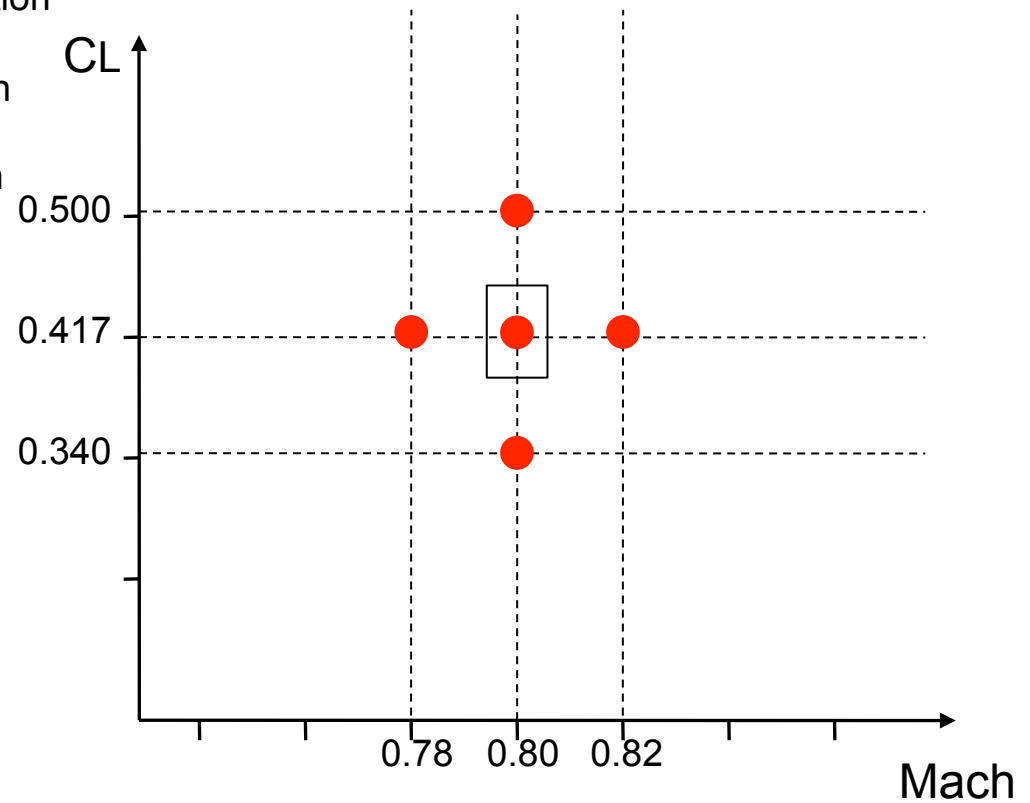
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- 3. Constrained Multi-Point Optimization



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- 3. Constrained Multi-Point Optimization
- The objective is drag reduction at constant CL and wing thickness.  
(Aerodynamic objective with elastic effects taken into account)



## Unconstrained Single-point Optimization

➤ The optimization employed a quasi-Newton gradient-based algorithm.

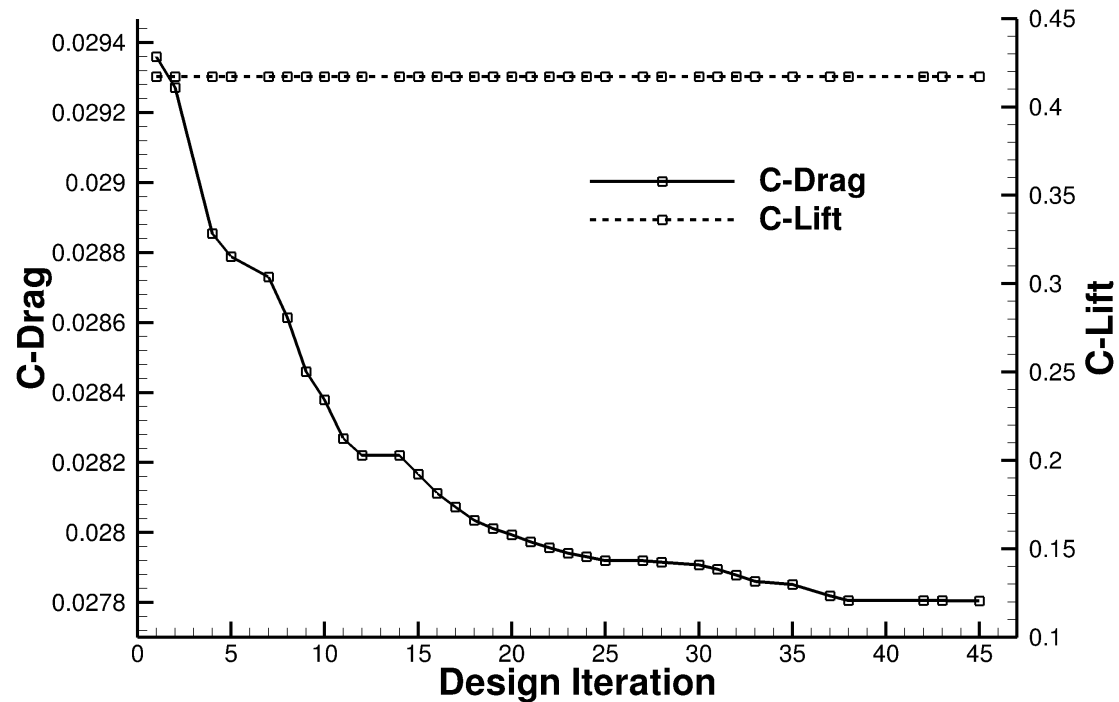
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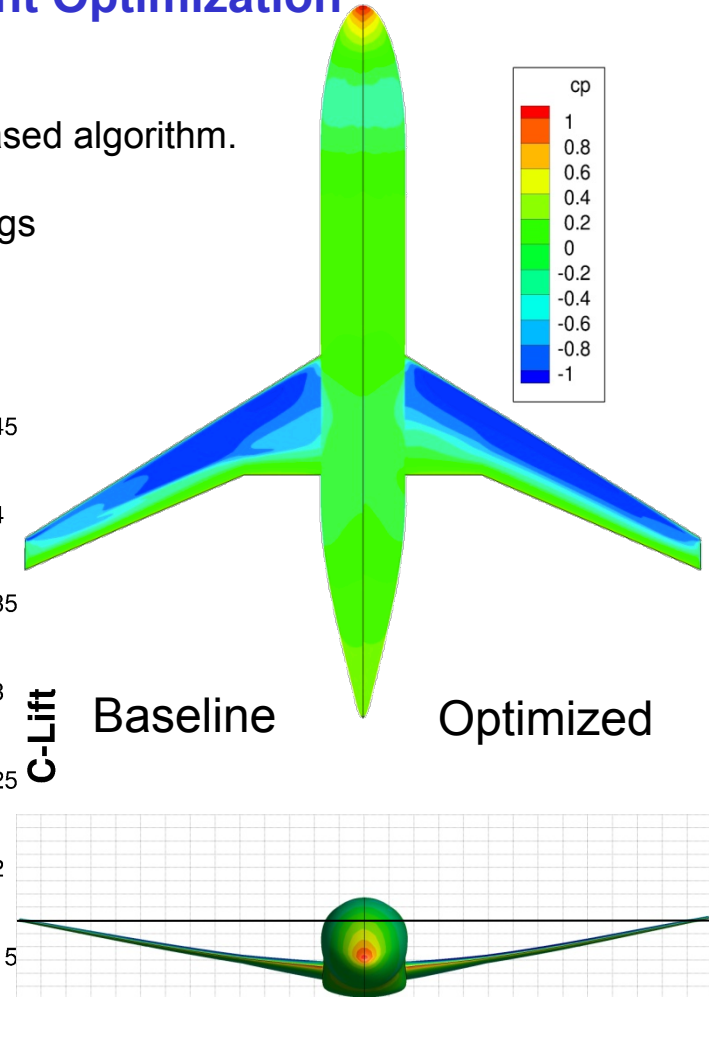
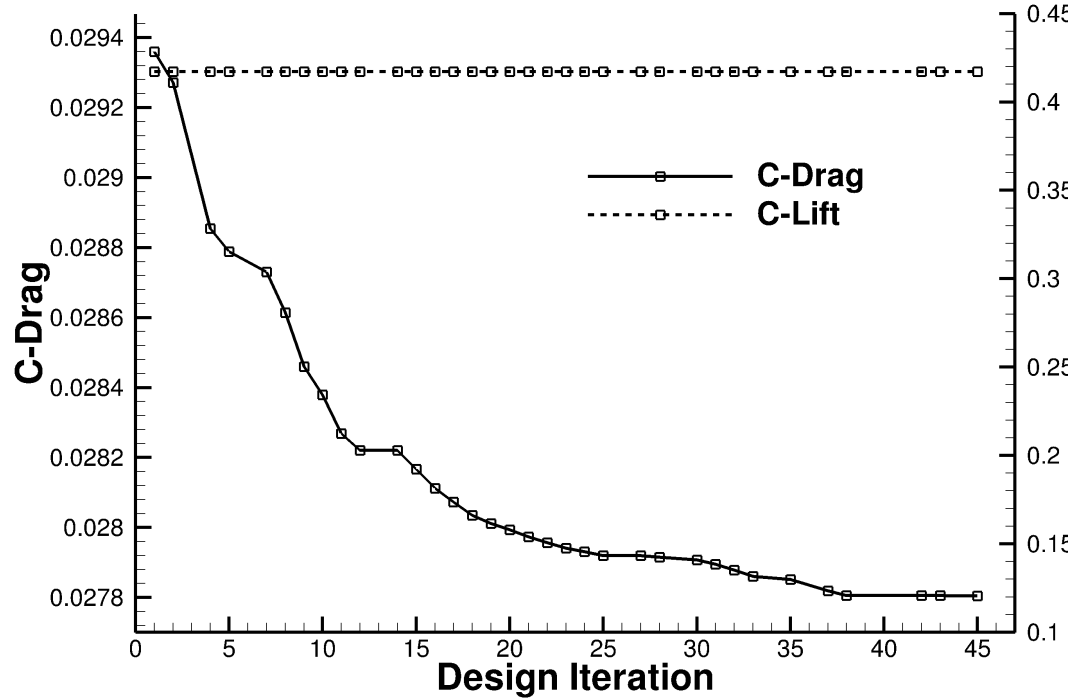
- The optimization employed a quasi-Newton gradient-based algorithm.
- Optimization converged after 41 aero-structural couplings and 25 coupled adjoint computations.
- The optimization reduced the drag by 15 drag counts while keeping the lift and the thickness constant.





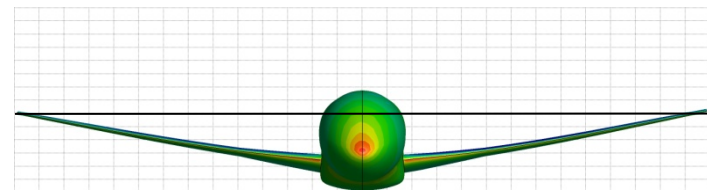
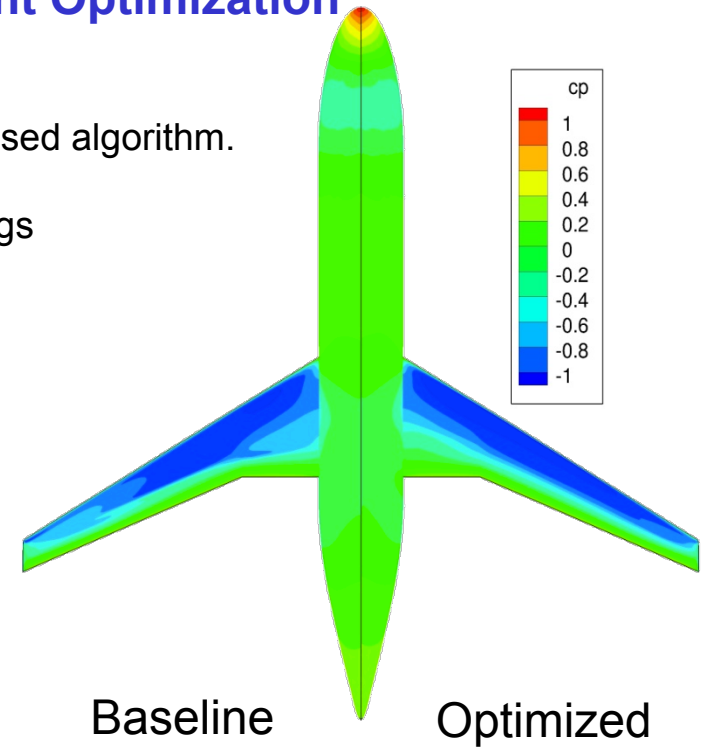
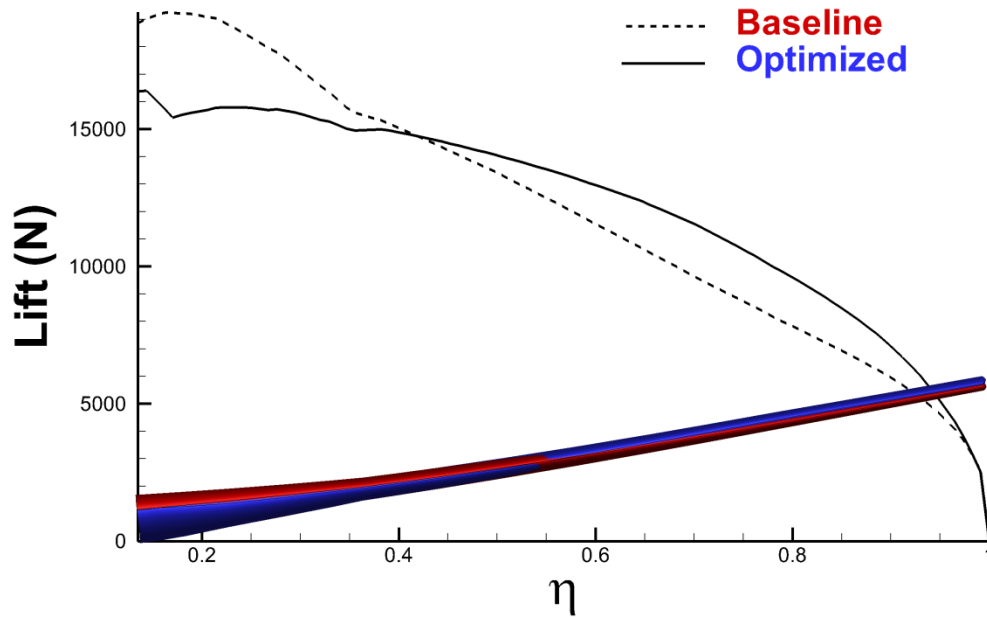
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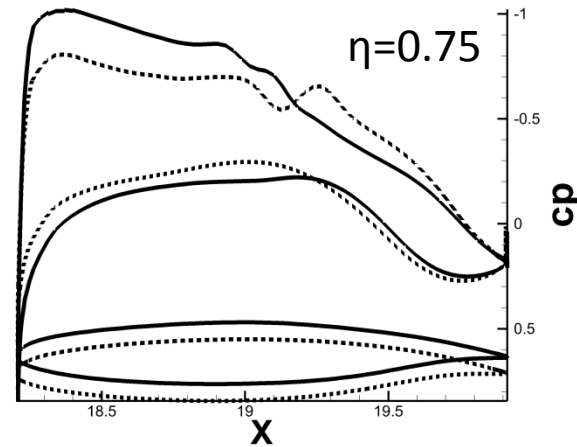
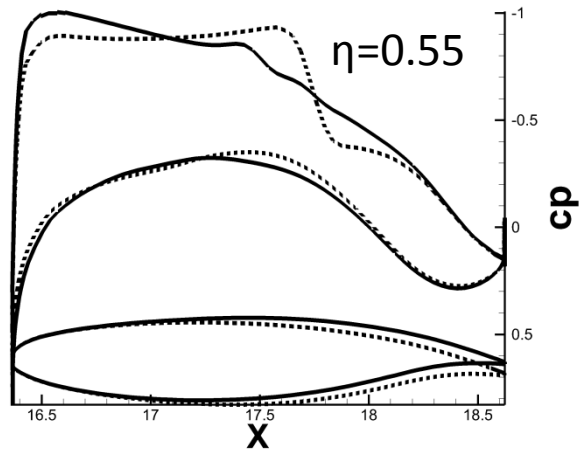
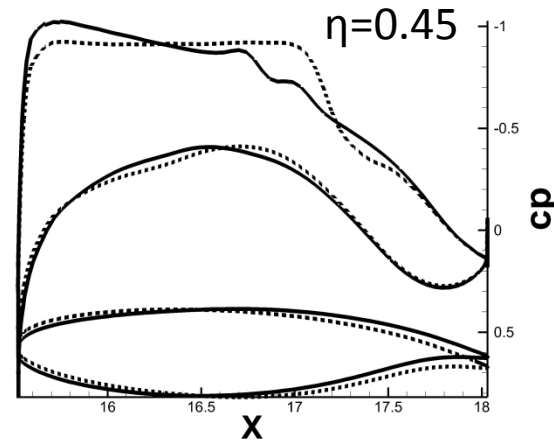
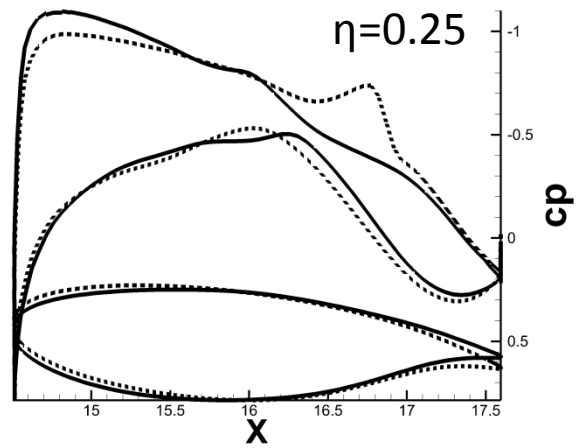


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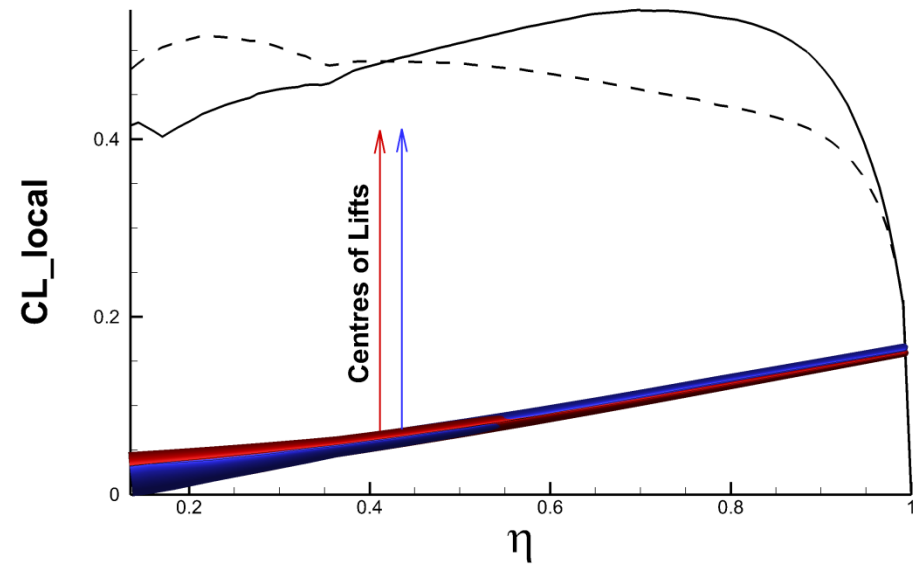
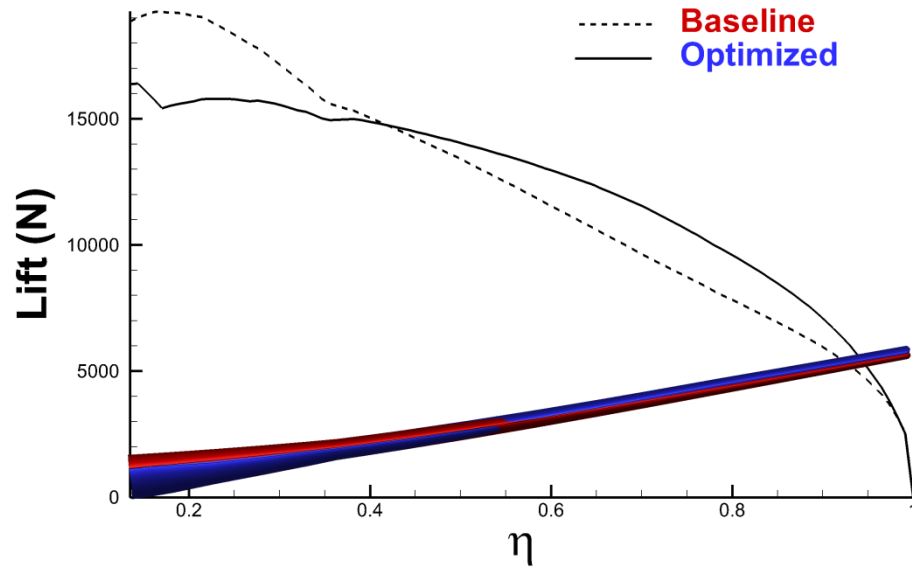
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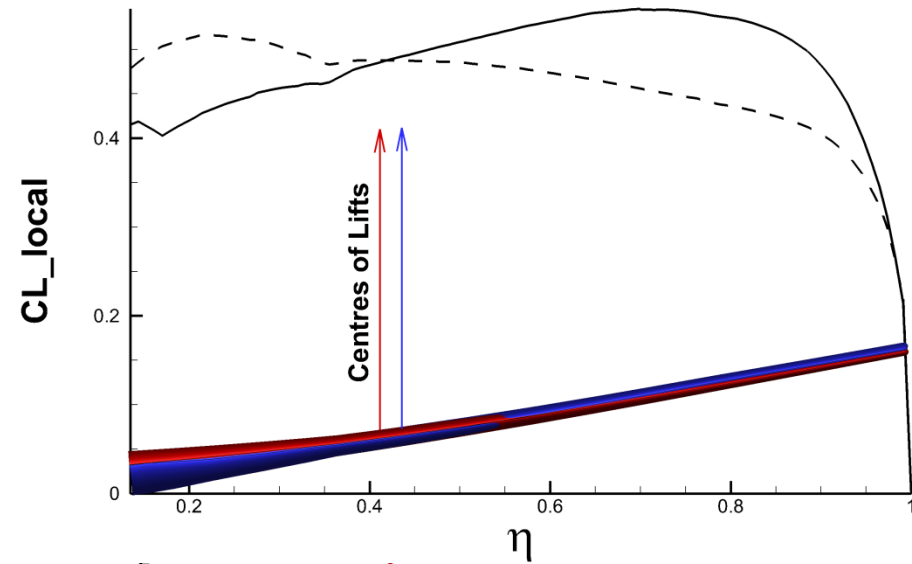
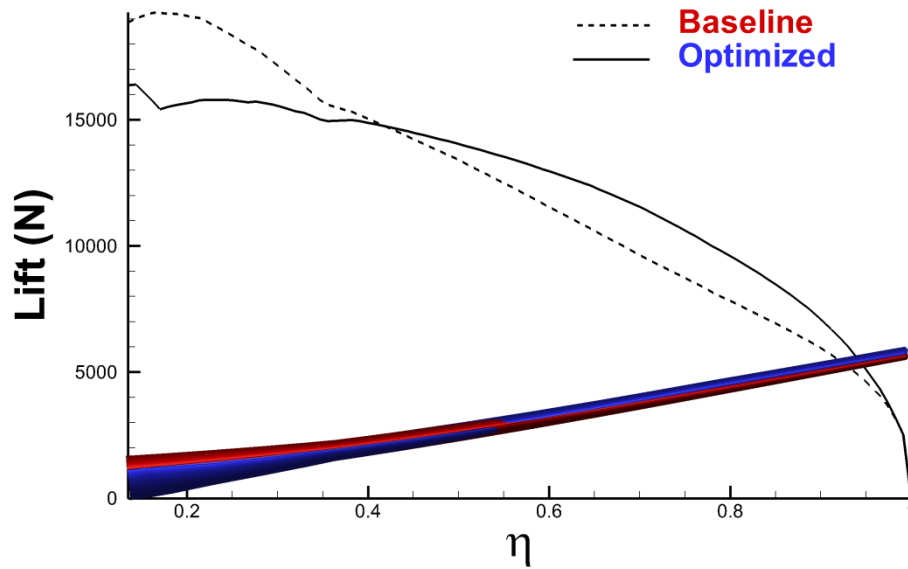
----- Baseline  
———— Optimized



## Unconstrained Single-point Optimization

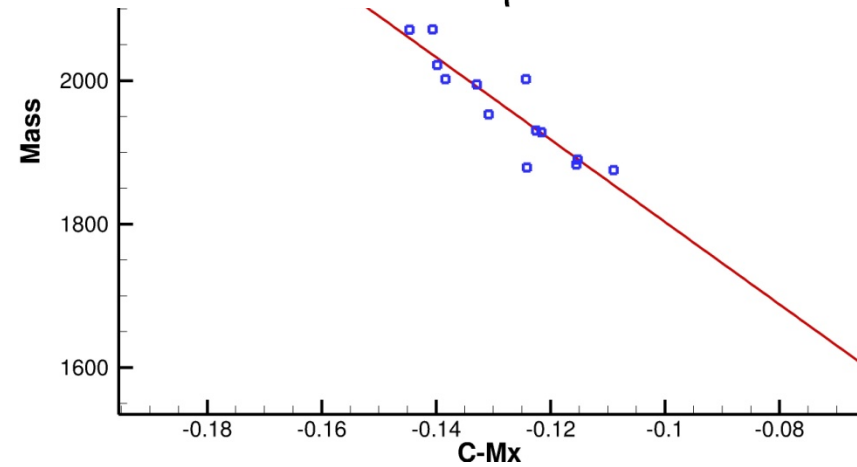


## Unconstrained Single-point Optimization



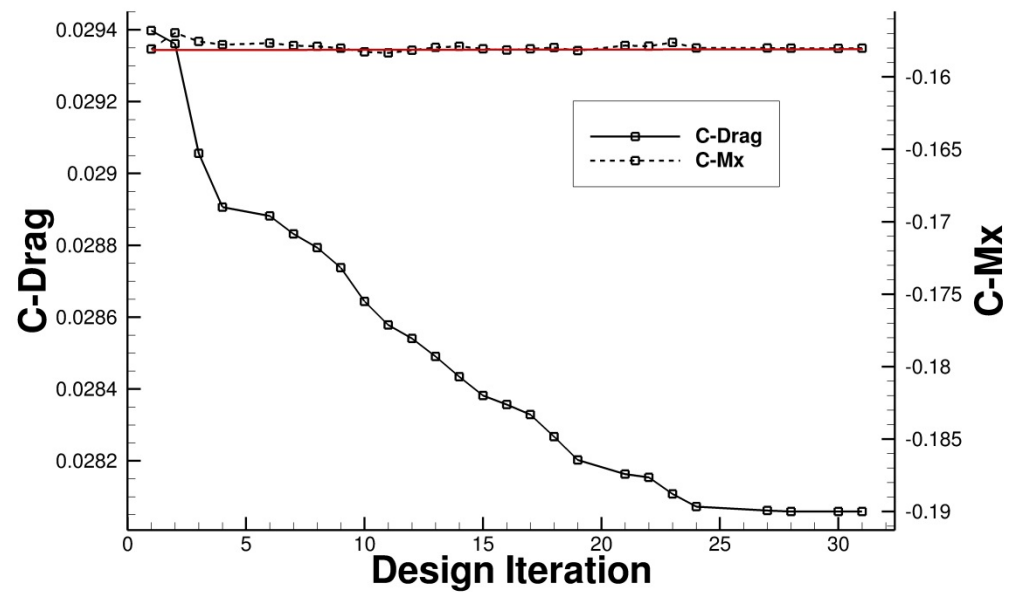
This (at constant lift) increases the bending moment at the Wing's root

⇒ Keep  $CM_x$  constant during the aero-elastic optimization



## Constrained Single-point Optimization

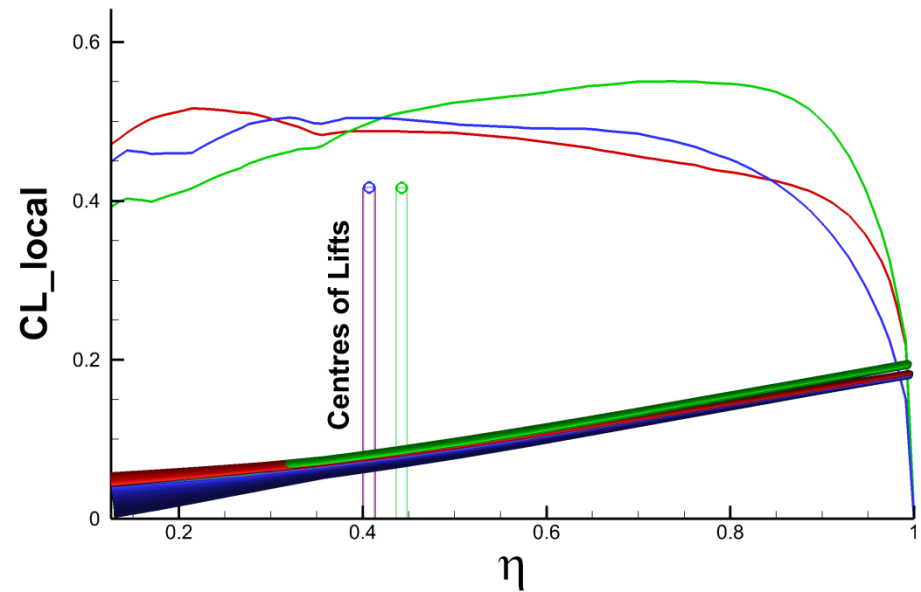
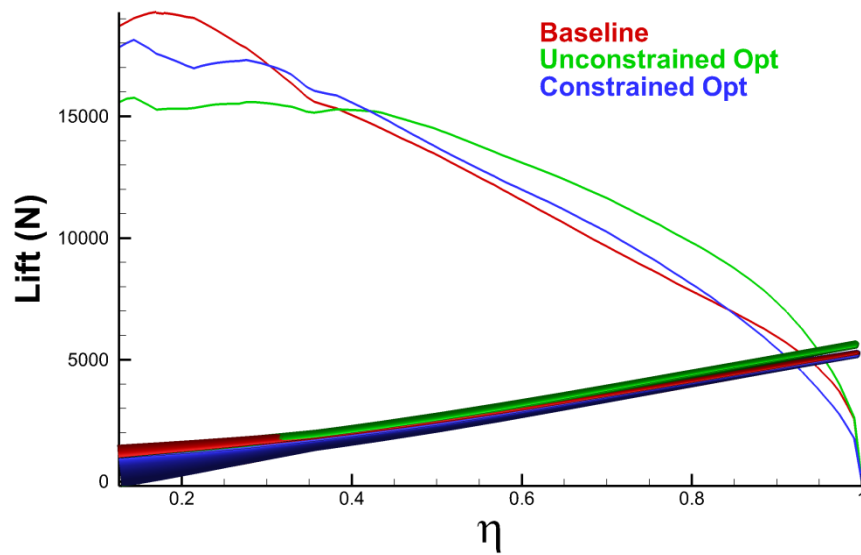
- The optimization employed SQP gradient-based algorithm.
- Optimization converged after 31 aero-structural couplings and 19 coupled adjoint computations.
- The optimization reduced the drag by 13 drag counts while keeping the lift and the thickness constant.





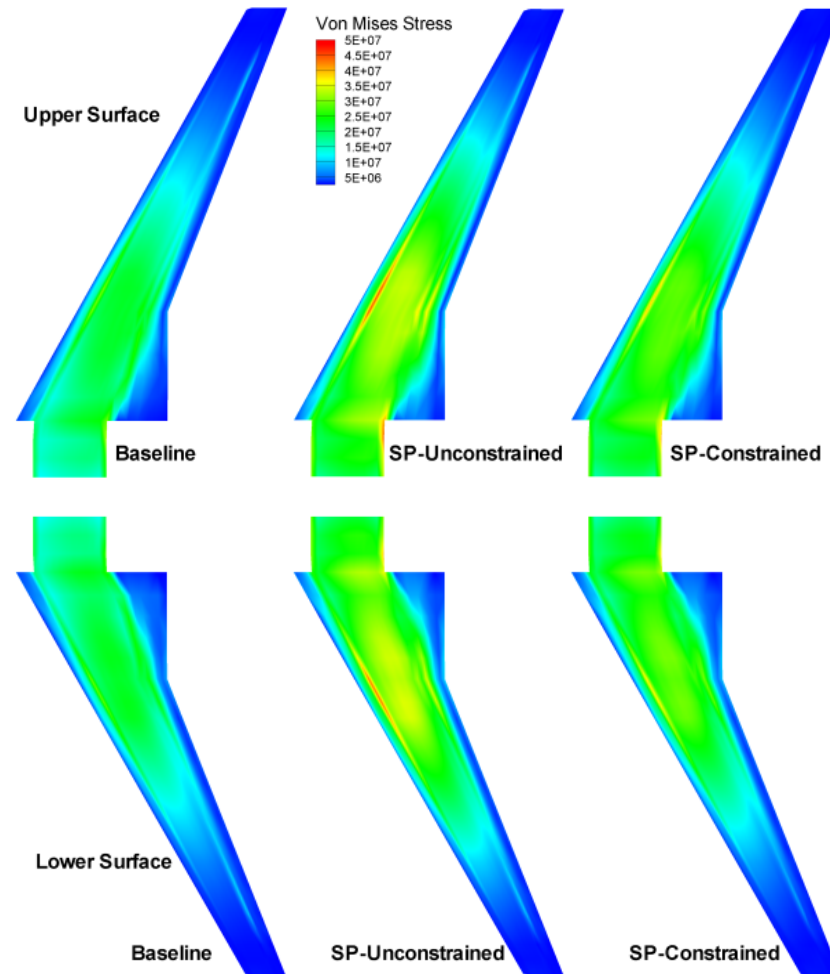
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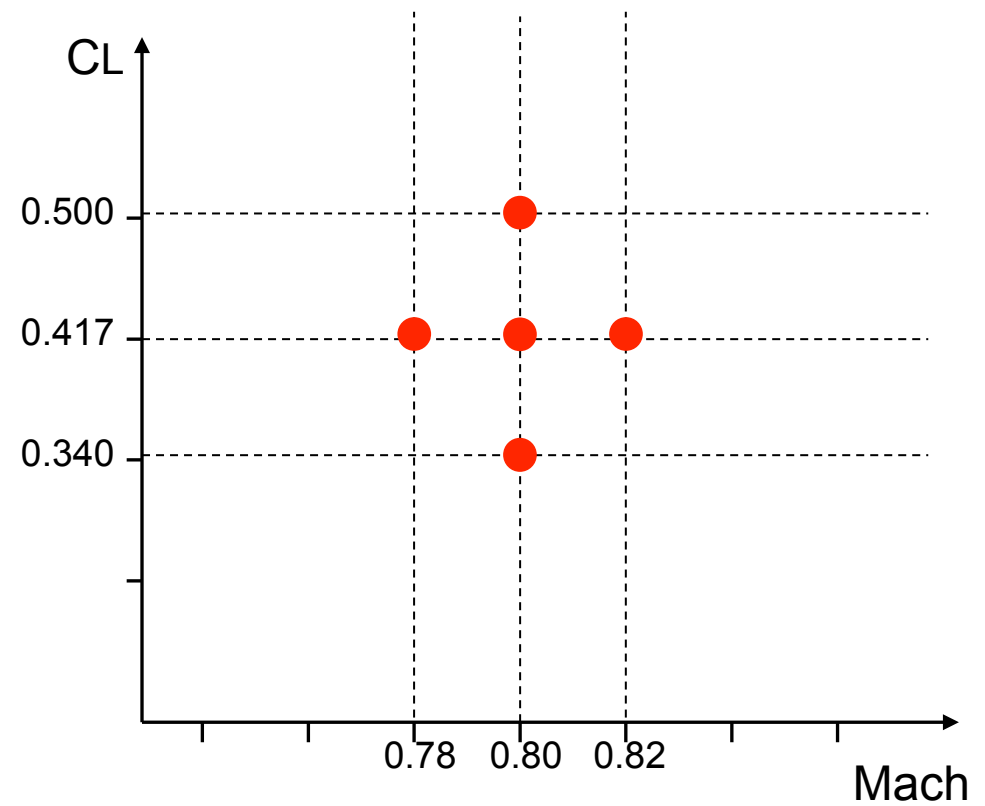
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## Constrained Multi-point Optimization

- The points were equally weighted.

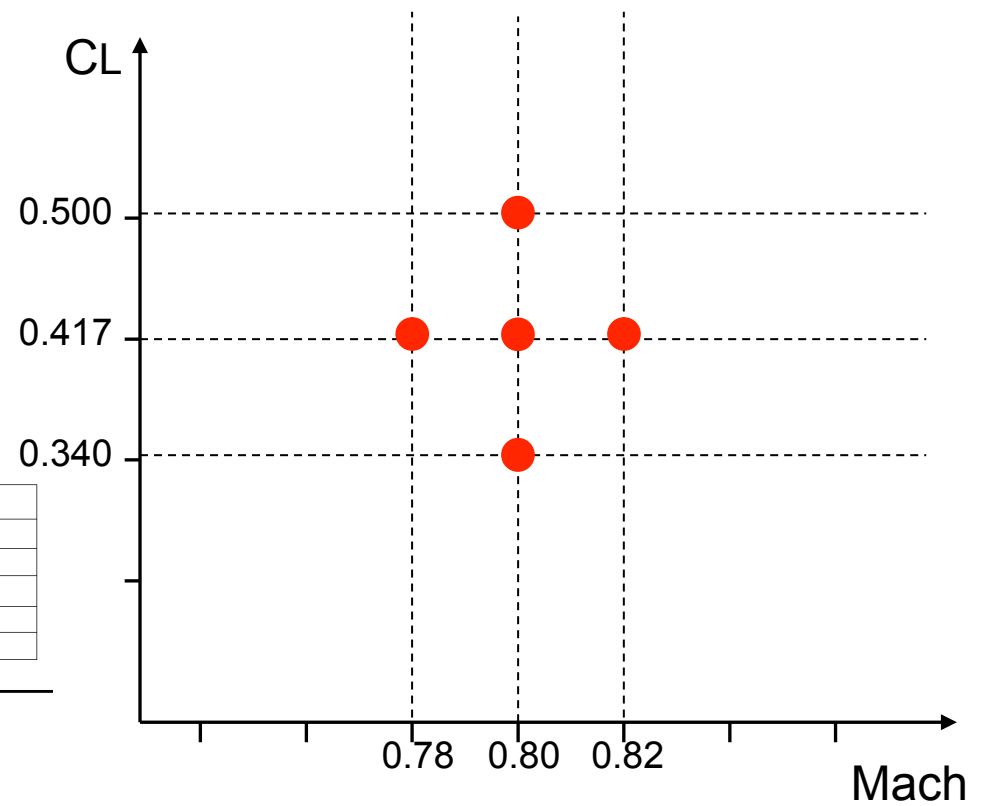
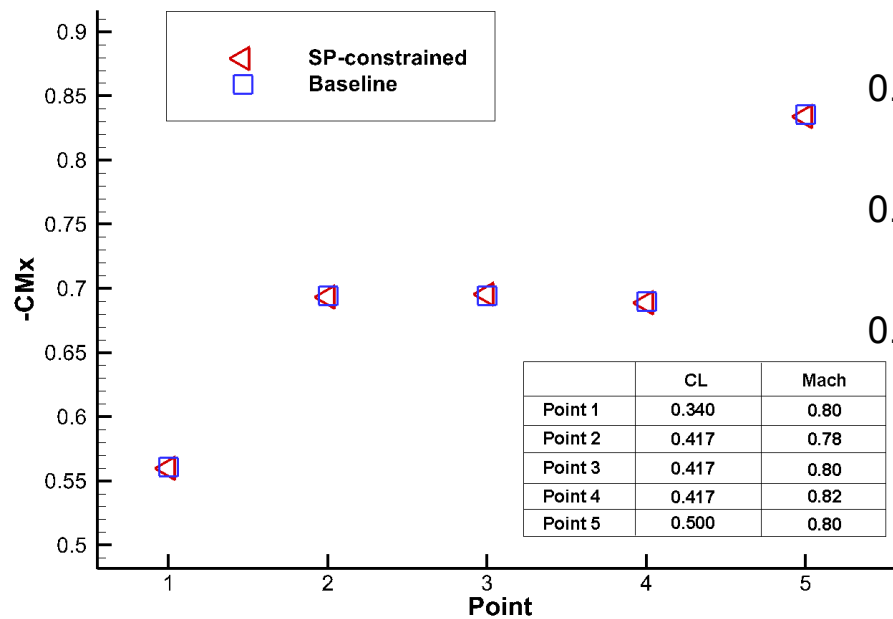
$$\text{Cost\_Function} = \sum_{i=1}^5 0.2 * C_{Di}$$



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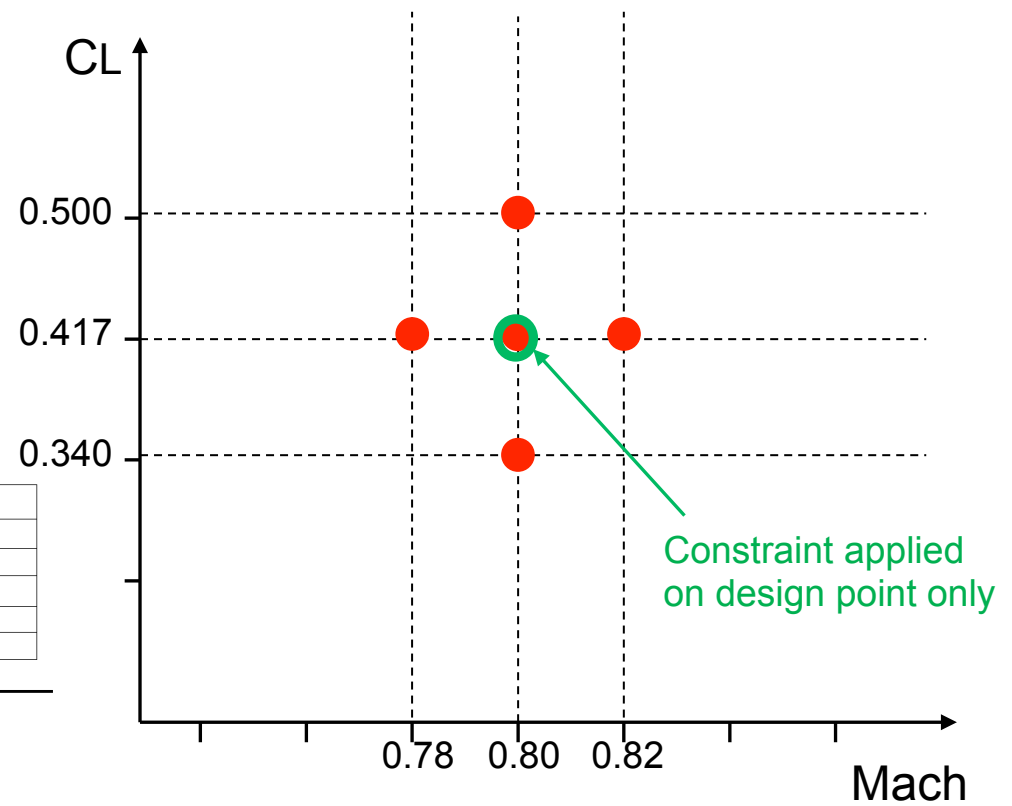
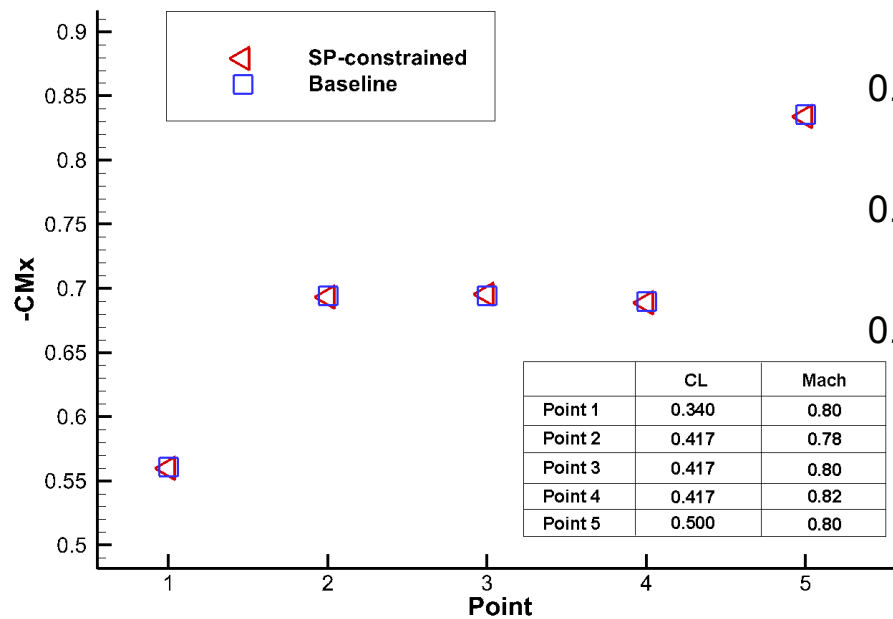
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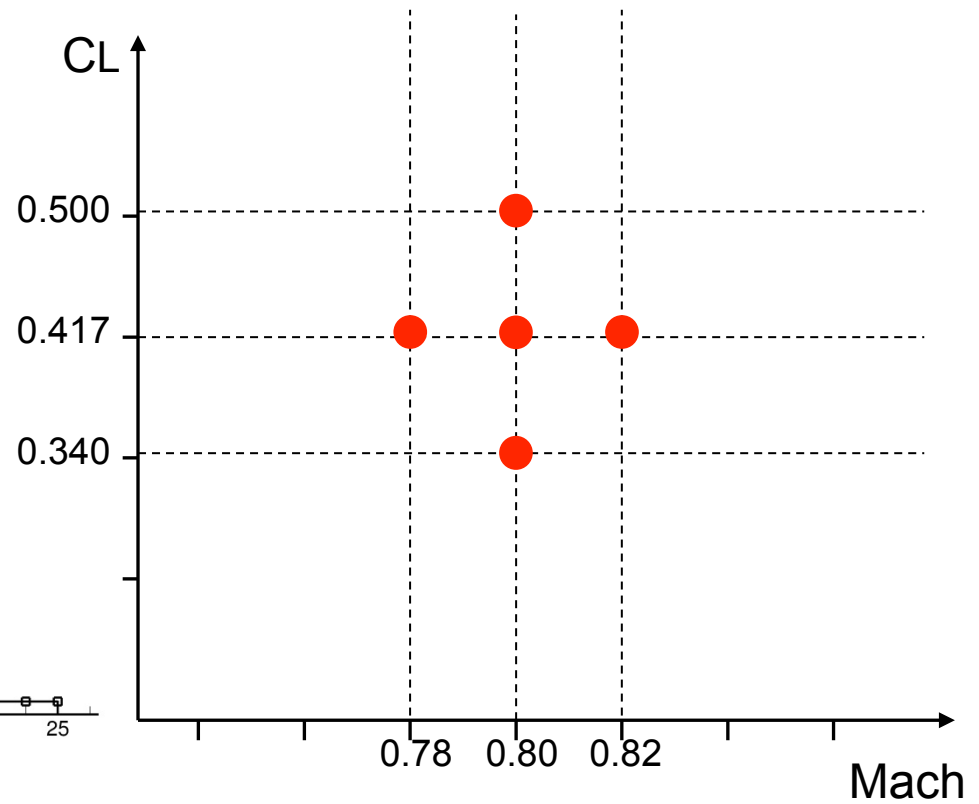
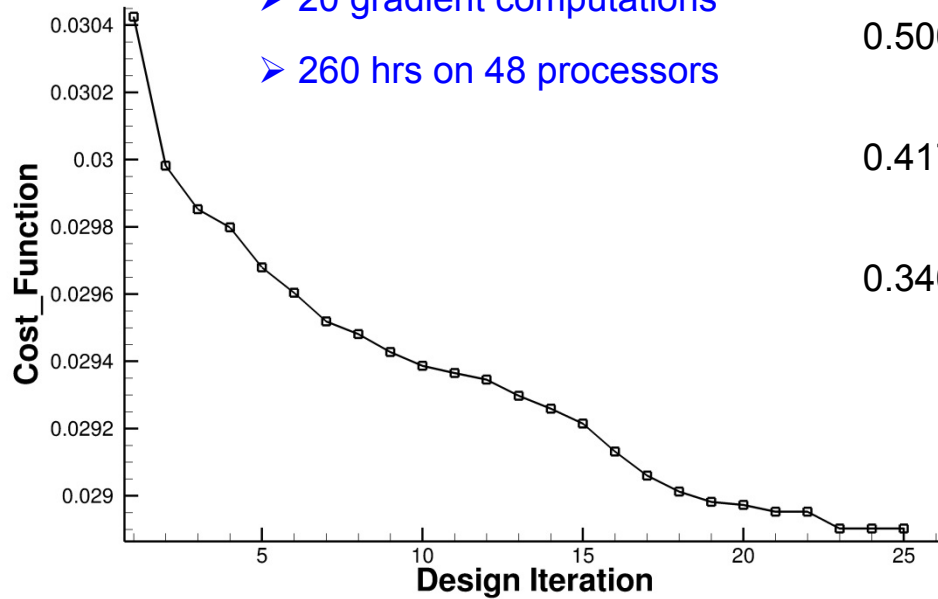


## Constrained Multi-point Optimization

- The points were equally weighted. ➡ Highest gradients bring highest change (drag reduction)

$$\text{Cost\_Function} = \sum_{i=1}^5 0.2 * C_{Di}$$

- 25 design iterations
- 20 gradient computations
- 260 hrs on 48 processors

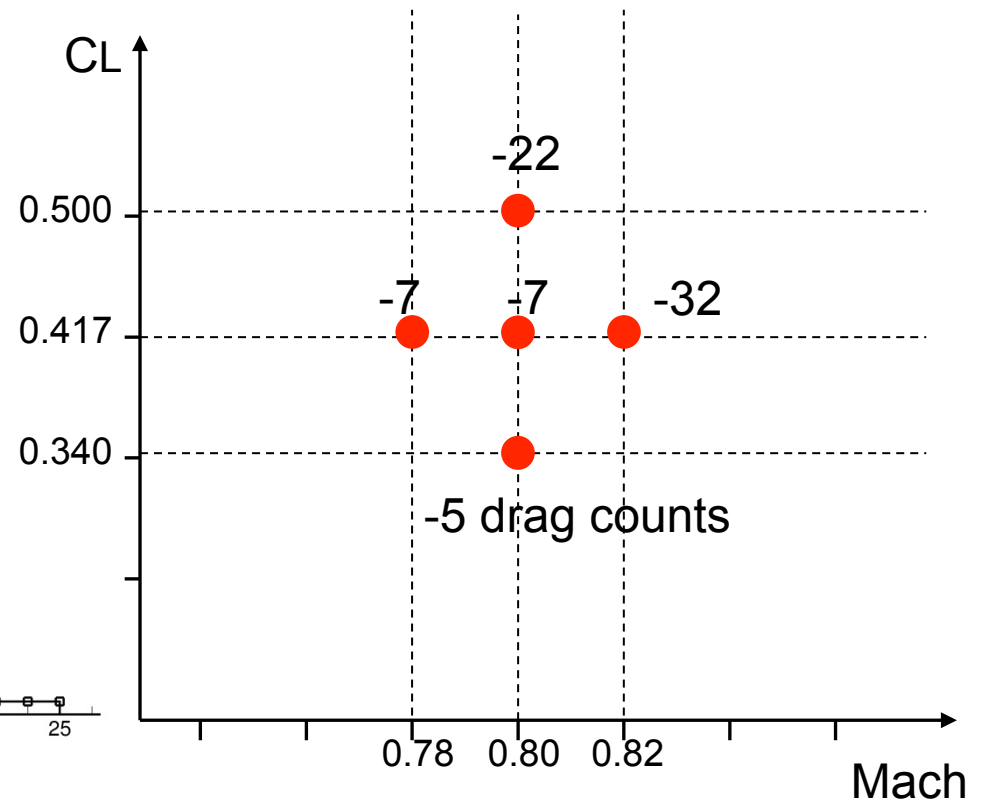
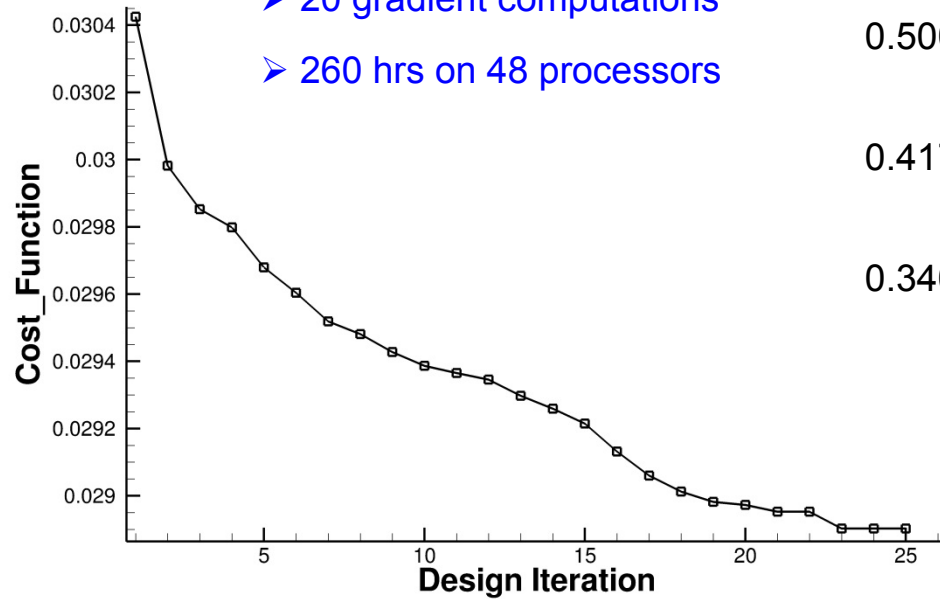


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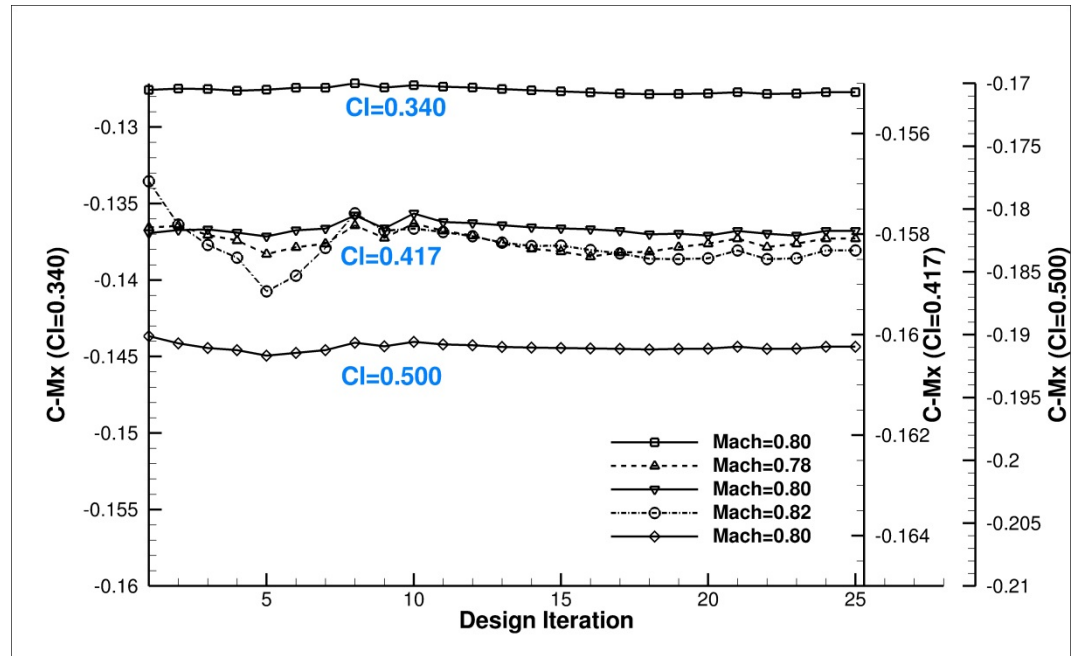
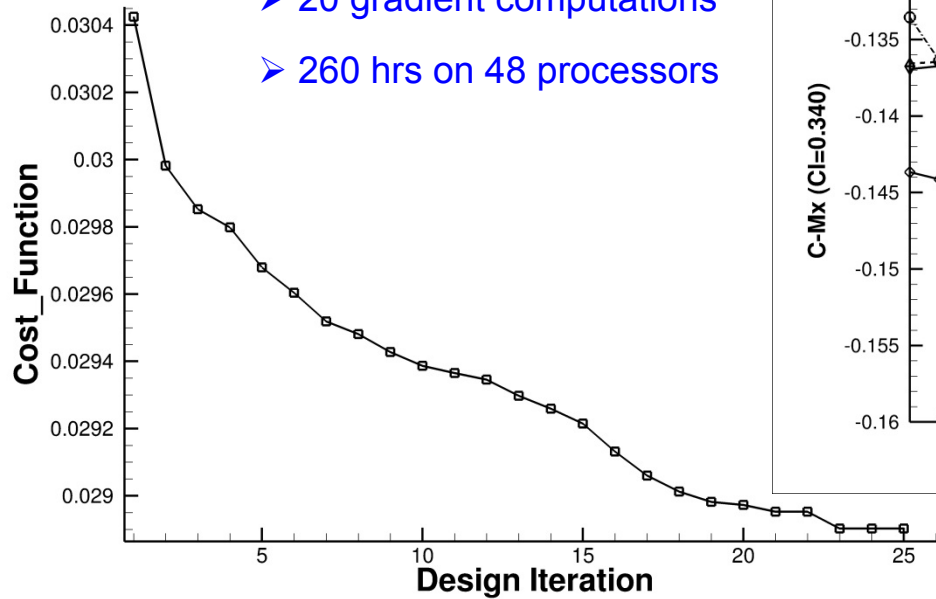


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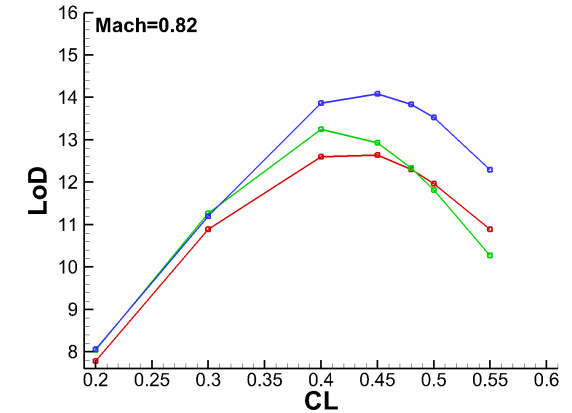
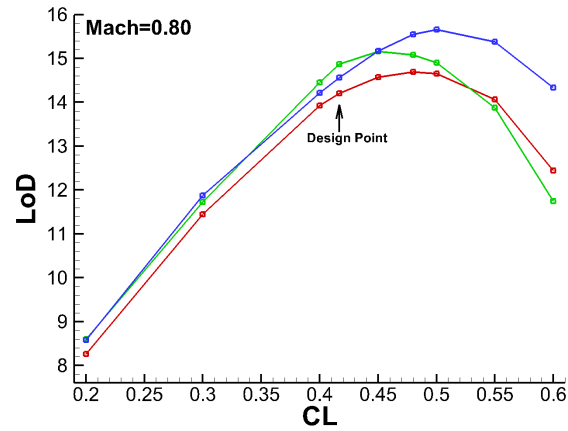
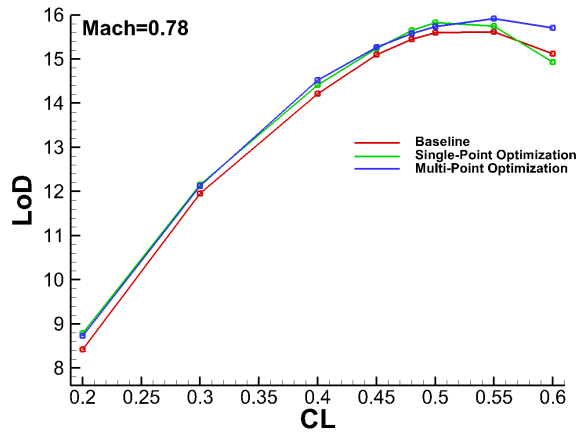
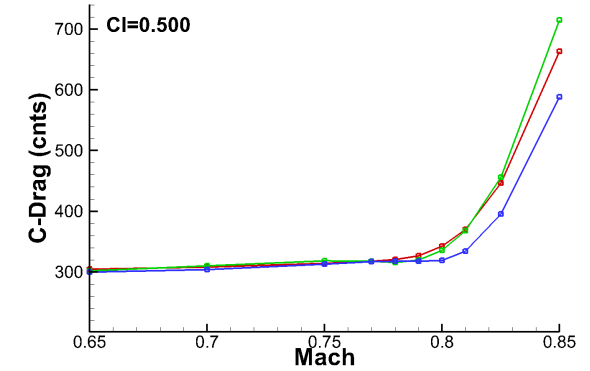
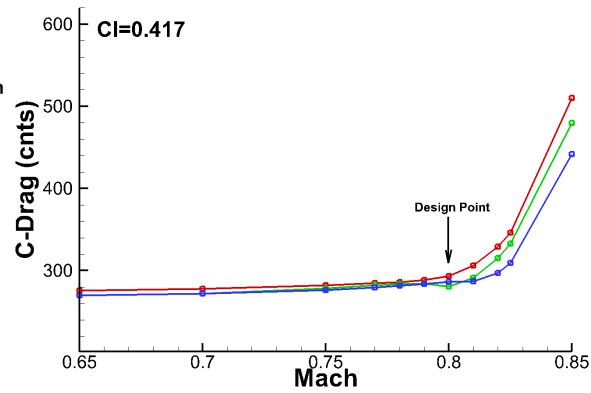
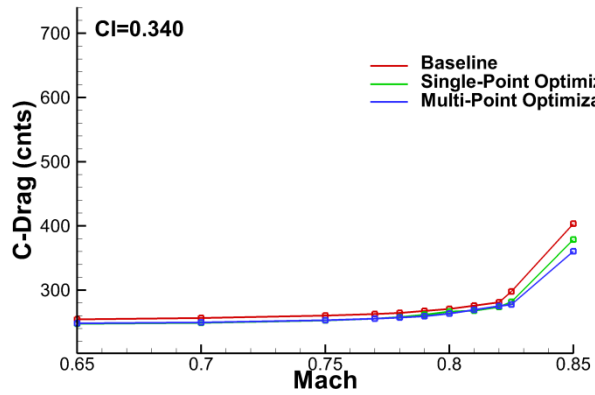
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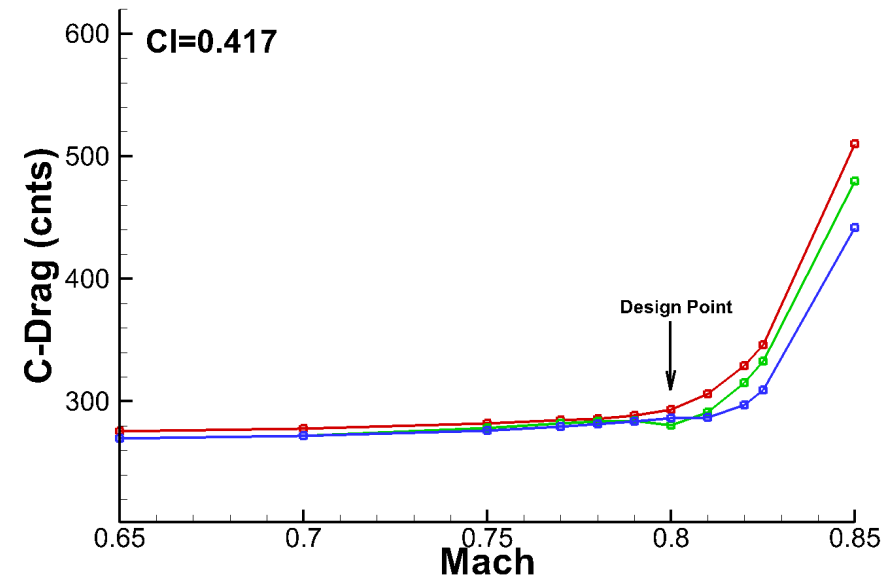
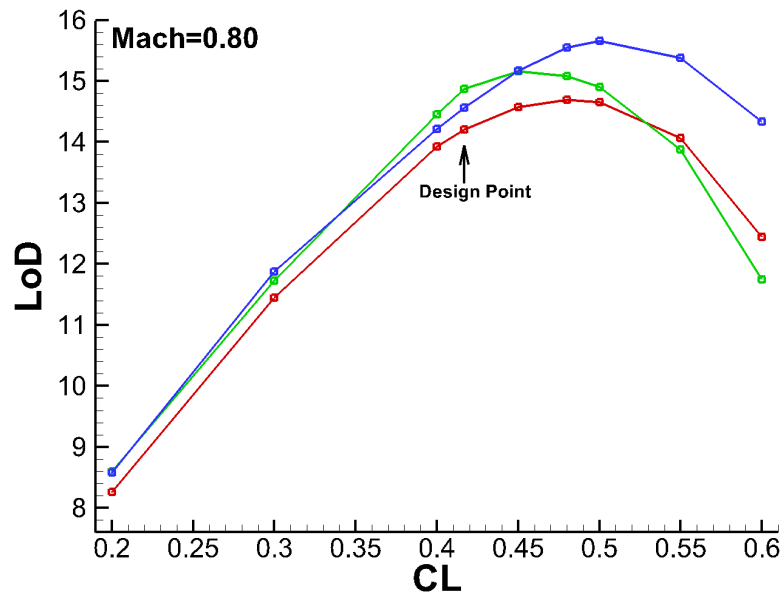
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## Constrained Multi-point Optimization



## Constrained Multi-point Optimization



## Future Work: Gradient Correction due to Trimming

- Trimming the flight with a horizontal tailplane (to reach a target pitching moment) will be considered during the Optimization.
- The gradients of our cost function need to be corrected if the flight is trimmed using horizontal tailplane. (similar to correcting gradients of drag when running for target lift).
- Use the Lagrange formulation to predict the correction term in the gradients.



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- Use the Lagrange formulation to predict the correction term in the gradients.
- If our cost function is drag then:

Correction Term

$$\frac{dC_D}{dD} @ trim = \frac{C_D}{dD} + \frac{\partial C_D}{\partial \alpha_w} \left[ \frac{1}{\partial C_L / \partial \alpha_w} \left( -\frac{dC_L}{dD} - \frac{\partial C_L}{\partial \alpha_t} \delta \alpha_t \right) \right] + \frac{\partial C_D}{\partial \alpha_t} \delta \alpha_t$$

$$\delta \alpha_t = \left( \frac{\partial C_{my} / \partial \alpha_w}{\partial C_L / \partial \alpha_w} \frac{dC_L}{dD} - \frac{dC_{my}}{dD} \right) / \left( \frac{\partial C_{my}}{\partial \alpha_t} - \frac{(\partial C_{my} / \partial \alpha_w)(\partial C_L / \partial \alpha_t)}{\partial C_L / \partial \alpha_w} \right)$$

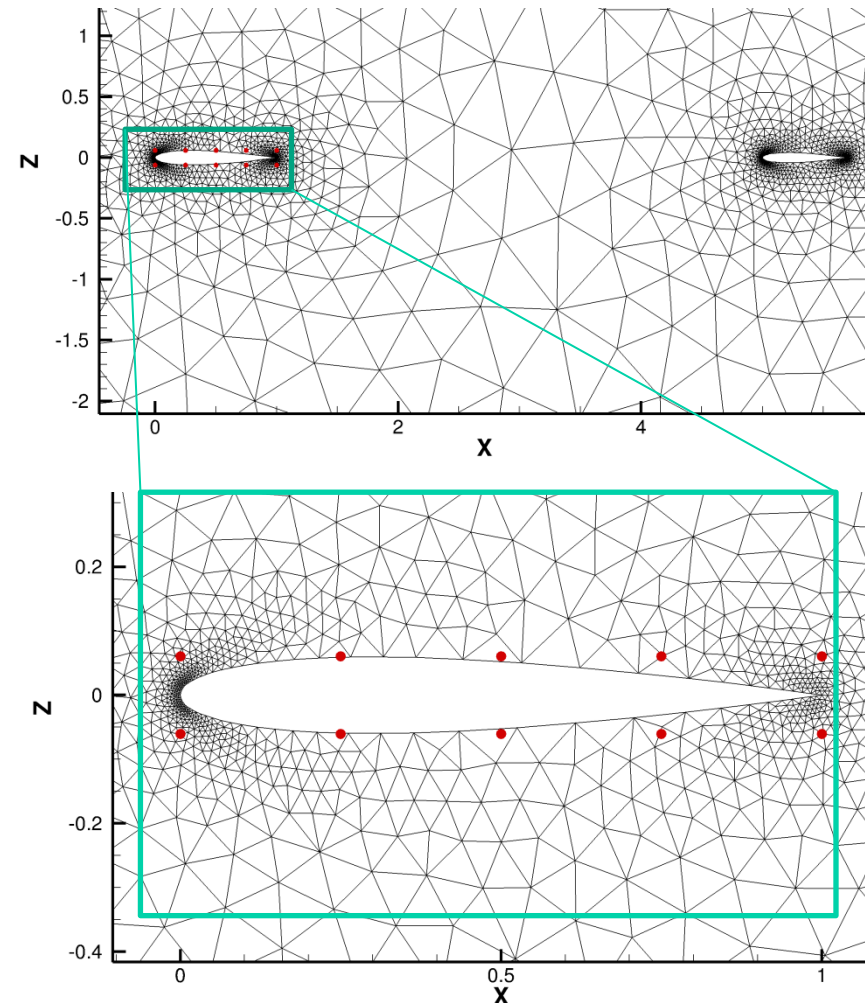
$\alpha_w$  : far-field angle of attack

$\alpha_t$  : tail's angle of incidence



## Future Work: Gradient Correction due to Trimming

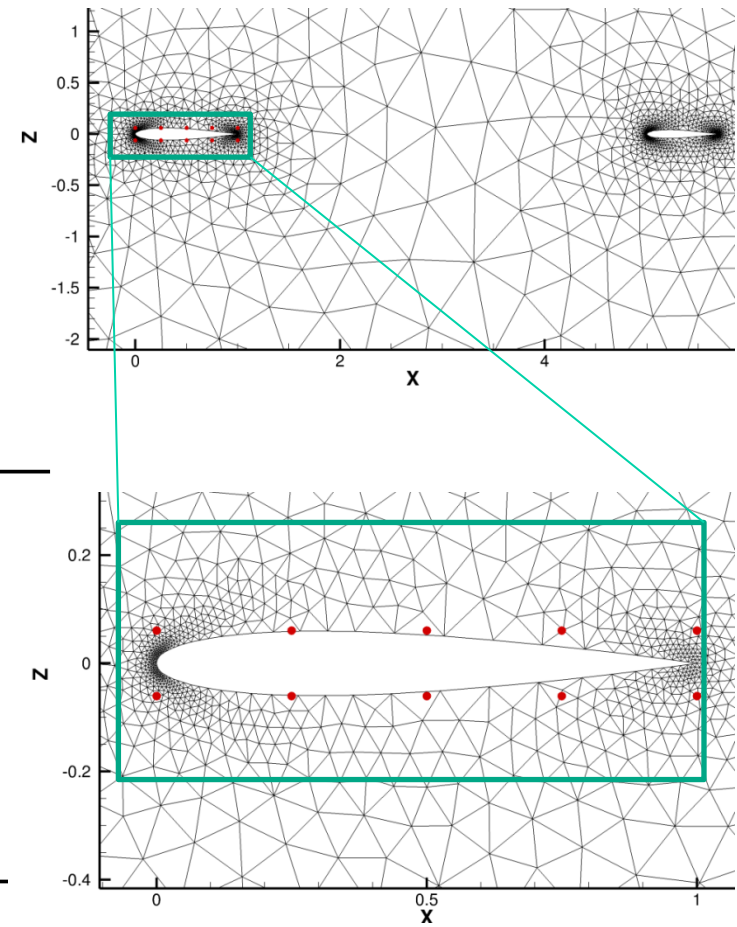
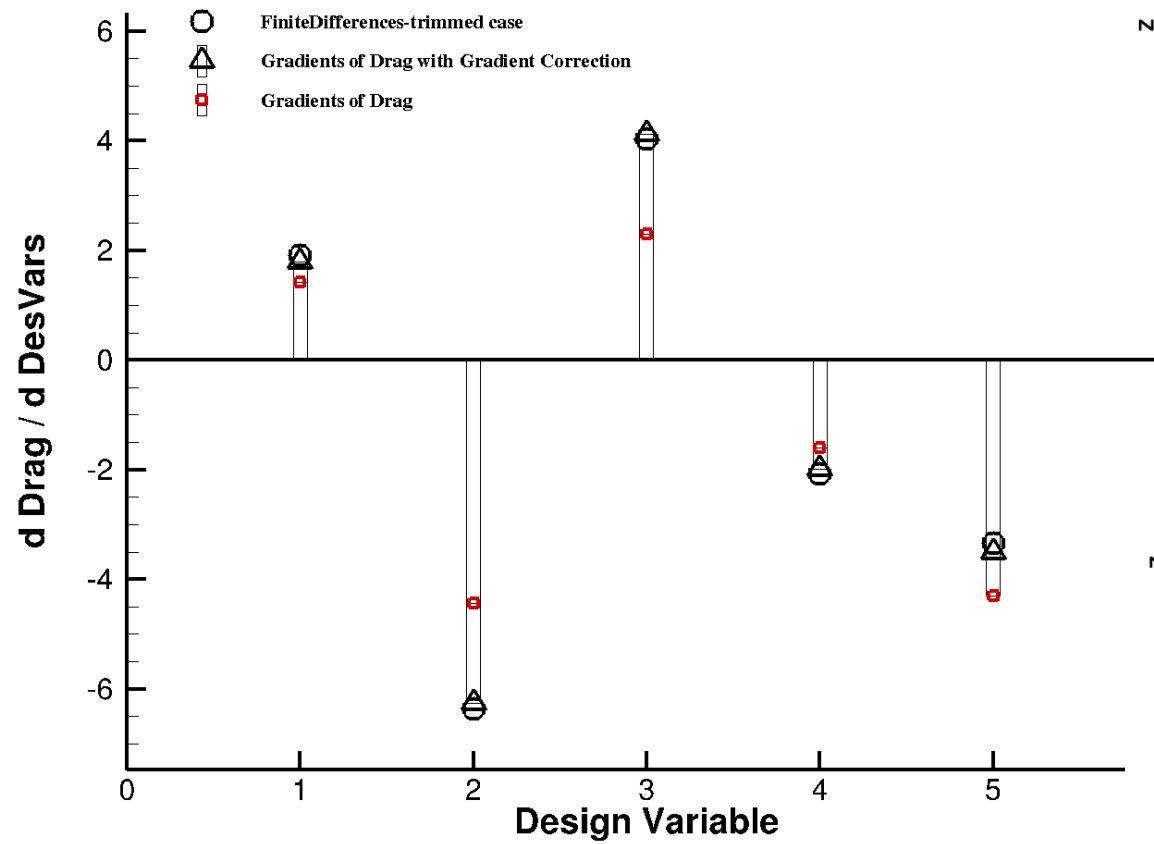
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## Future Work: Gradient Correction due to Trimming

➤ Tested on 2D Euler case





## Conclusions

- The coupled aero-structural adjoint approach was employed to efficiently obtain the gradients employed in single- and multi-point aero-elastic optimizations.
- The approach employs DLR's TAU code to solve the flow equations and ANSYS Mechanical to solve the structure equations, and deals with inviscid as well as viscous turbulent flows.
- The coupled adjoint approach could save around 75% of computational time, which makes it now possible to perform aero-elastic optimizations using the gradient-based techniques, even for multi-point optimizations.
- A single- and multi-point optimizations with constrained rolling moment were performed and expected to have better effect on the structure (less weight).
- Future optimizations will include aerodynamic to structure cross sensitivities
- Future optimizations will include (horizontal tail) trimming effect



THANK YOU FOR YOUR ATTENTION

