

*"For a plane to fly well it must be beautiful"*



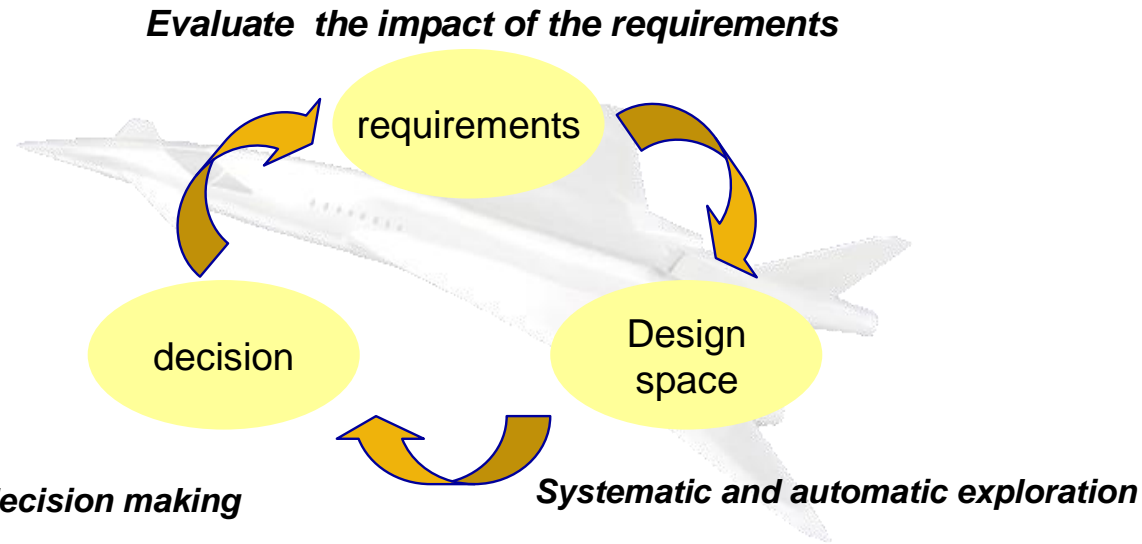
# **Multidisciplinary Optimization**

**M. Ravachol.**

Dassault-Aviation, St-Cloud, France



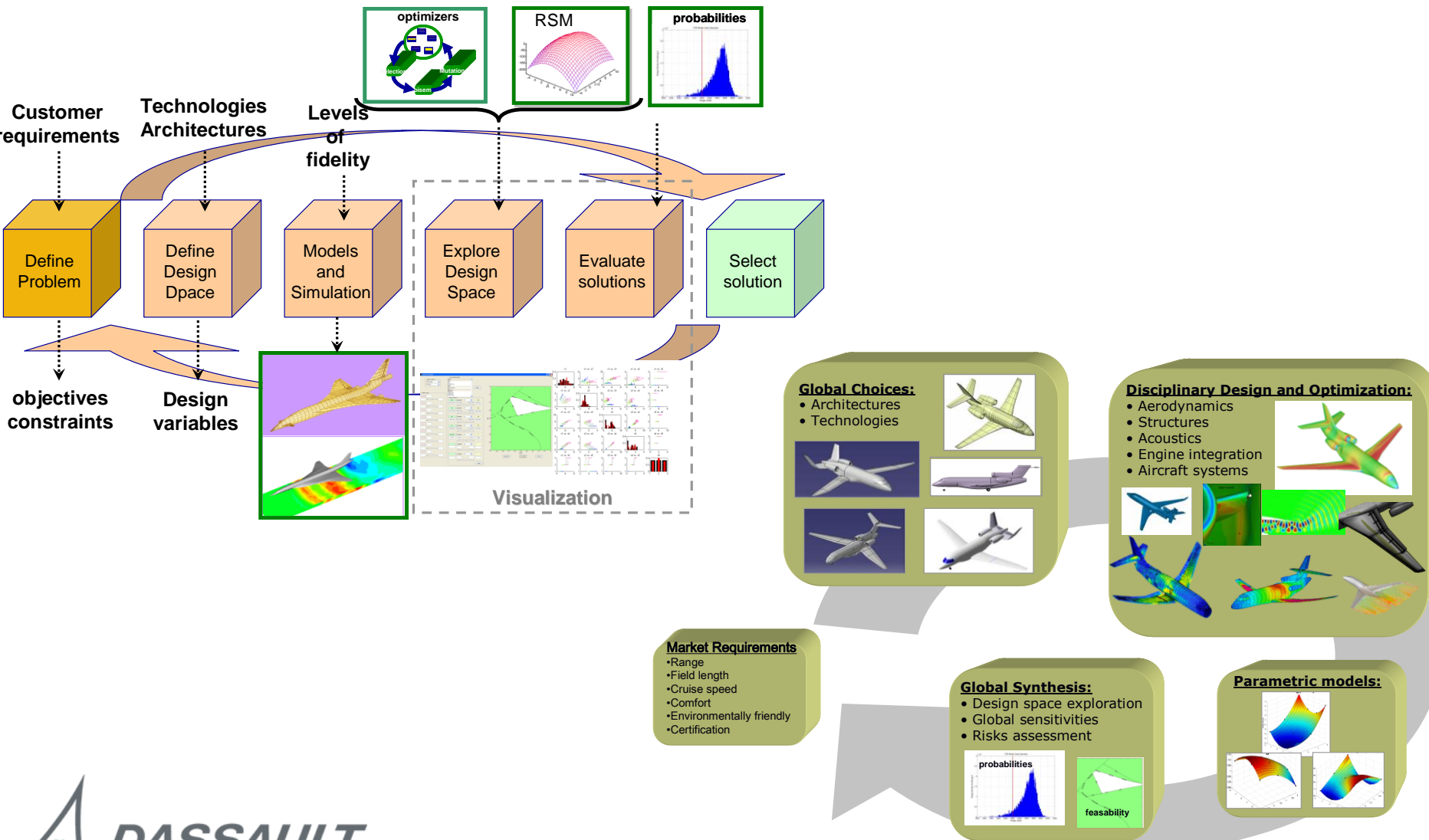
# Decision Loop in Design



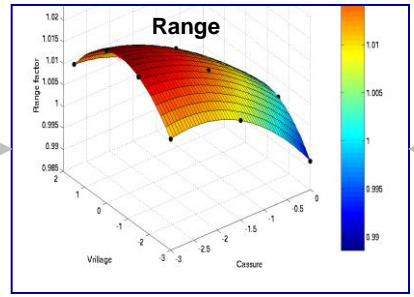
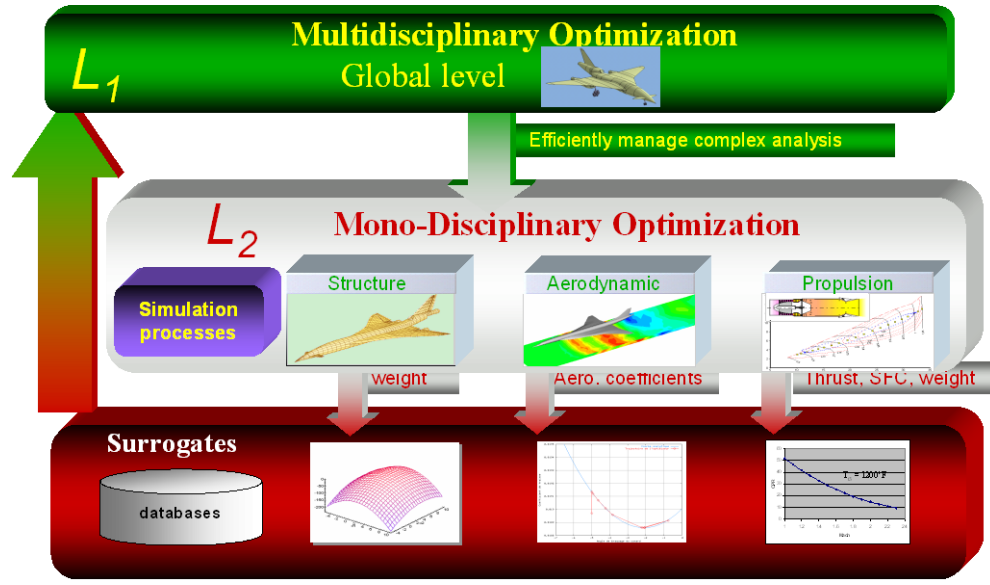
- Synthesis of important parameters
  - What are the limits and where they are.
  - Impact of component performances on global performances
- Propose trade offs
  - Between requirements
  - On design parameters
- Manage risks
  - Quantitative evaluation

- Understand the design space
  - What are the important parameters ?
  - How the requirements interact with each others?
  - Where are the most promising solutions ?
- Generate models dedicated to decision making
  - Trade offs
  - Evaluate risks

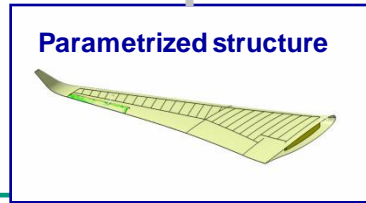
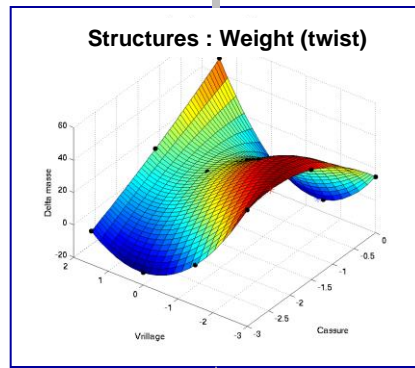
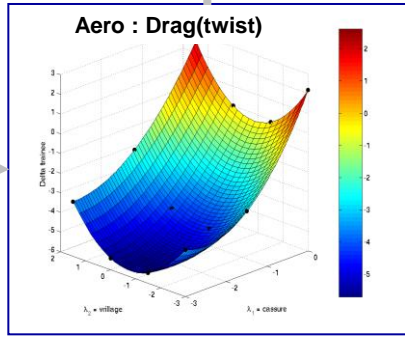
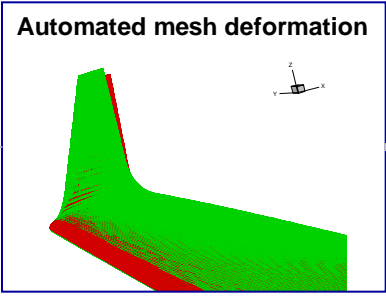
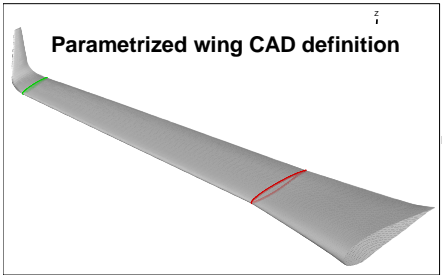
# Design Loop



# Multilevel MDO



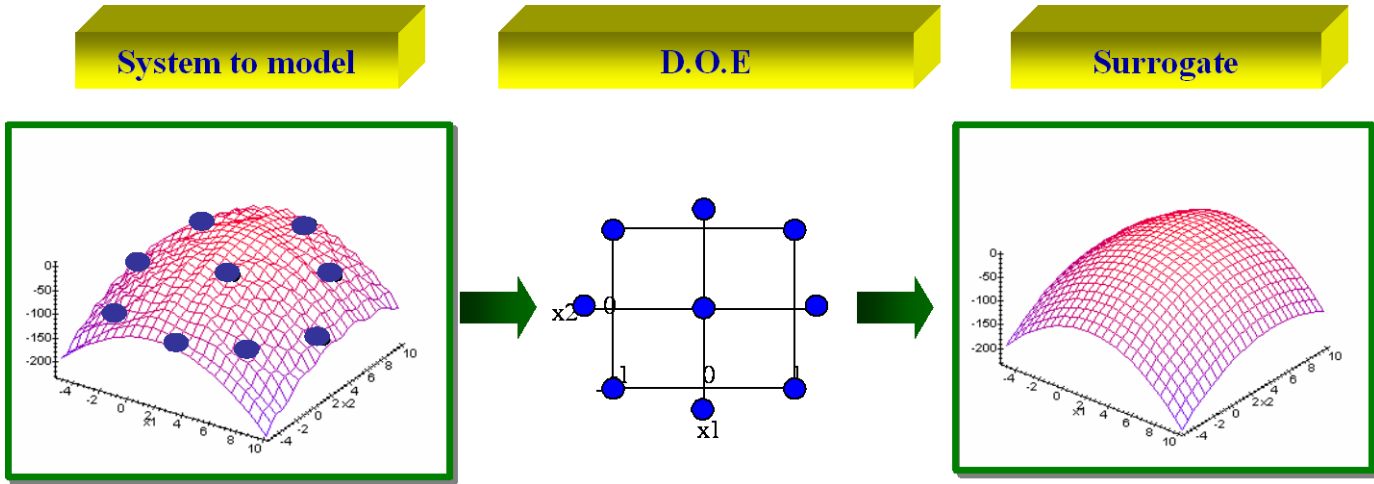
Level 1 Optimization



Level 2 Detailed Optimizations

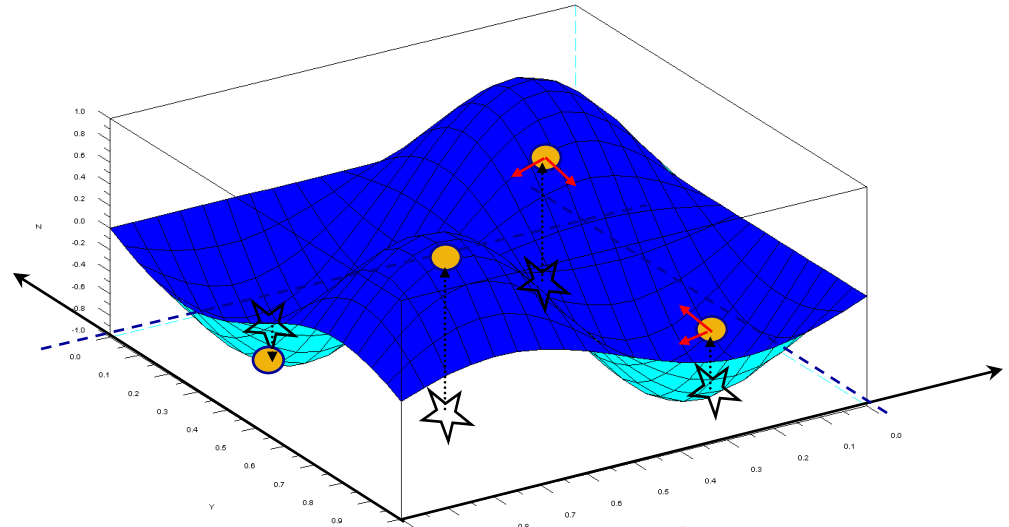


# Surrogates models



- D.O.E:
- LHS
  - max(min)
  - pseudo MC
  - Adapted

- Advanced models
- Radial basis functions
  - Kriging



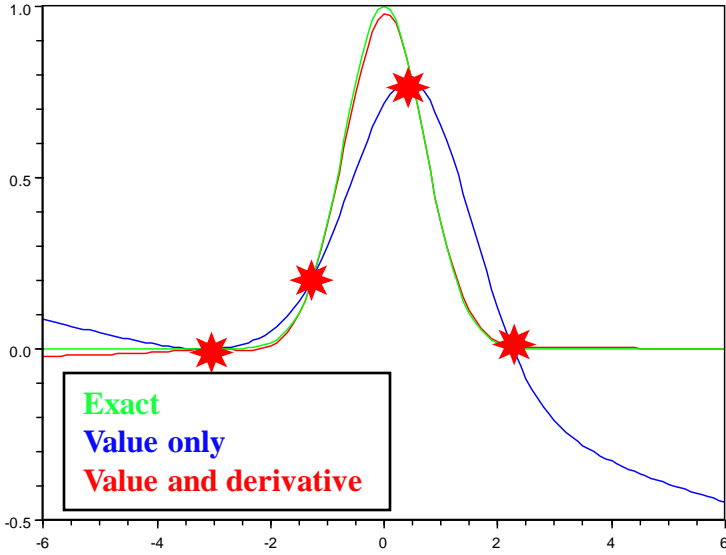
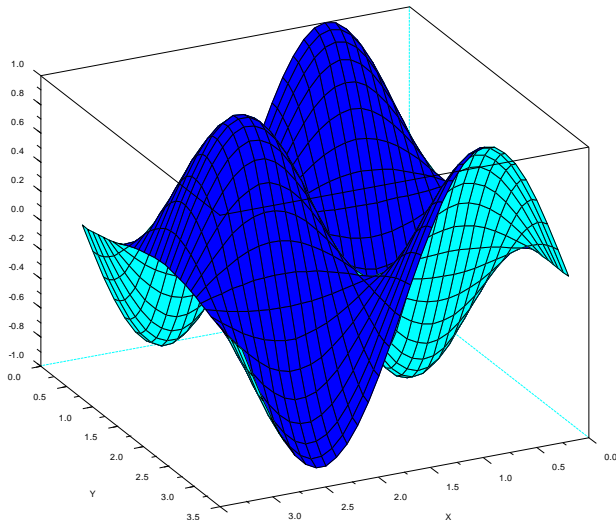
**Surrogates = key ingredient to MDO**

# RBF using derivatives

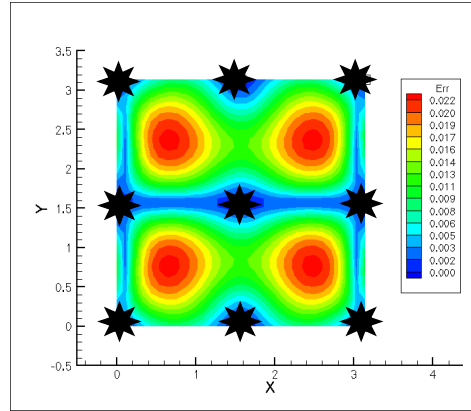
$$s(x) = p(x) + \sum_{i=1}^{n_s} \lambda_i \phi_i(x) + \sum_{l=1}^d \sum_{j=1}^{n_s} \mu_{lj} \frac{\partial \phi_j(x)}{\partial x^l} \quad (\phi_i(x) = \phi(x, x_i))$$

$$s(x) = f(x), x \in \mathcal{X} \quad \overline{n_s}$$

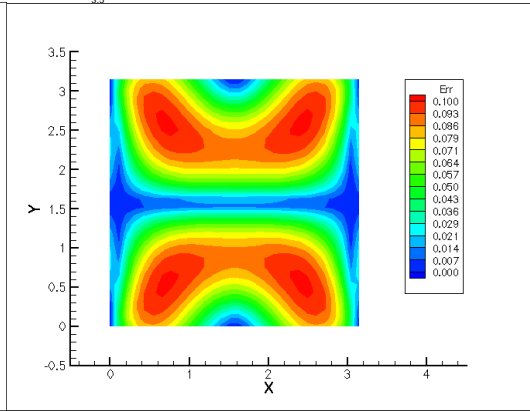
$$\frac{\partial s(x)}{\partial x^l} = \frac{\partial f(x)}{\partial x^l}, x \in \mathcal{X} \quad \overline{n_s}, l = 1, \dots, d$$



1D example



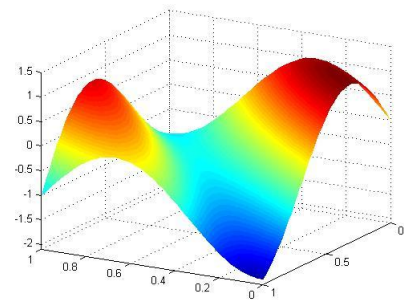
with gradients  $err_{max} = 2.2\%$



without gradient  $err_{max} = 10\%$

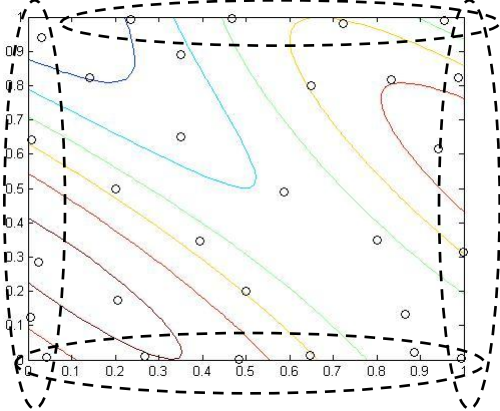
# DOE using Kriging MSE

True Surface

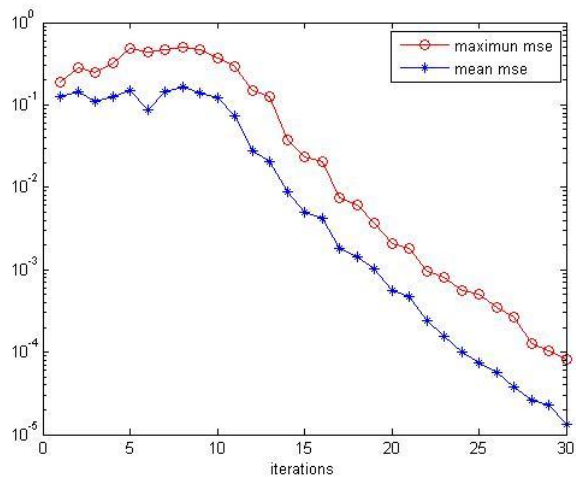


Points on the border of the domain

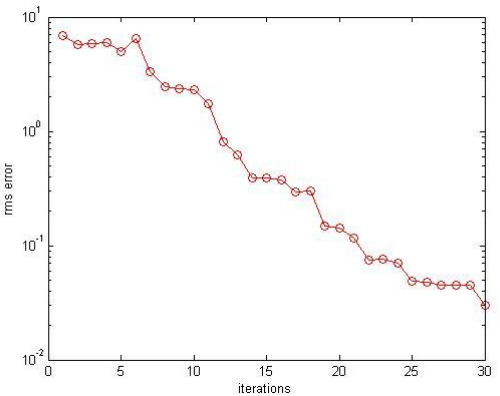
Adapted sampling (30 points)



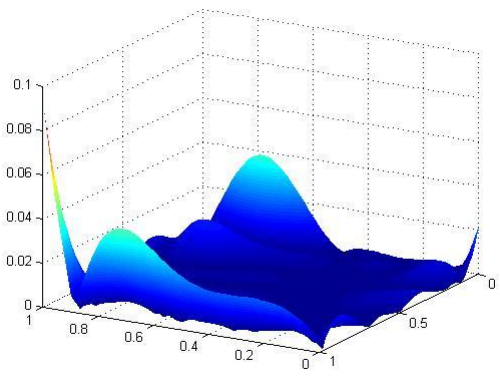
Sampling convergence (mse)



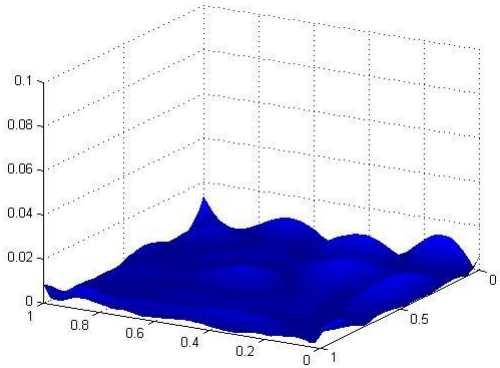
Sampling convergence (rms)



Error space filling sampling (30 points)



Error adapted sampling (30 points)



Adaptive sampling reduces interpolation error for given computational budget

Adaptive sampling is a sequential process



# Illustrative example

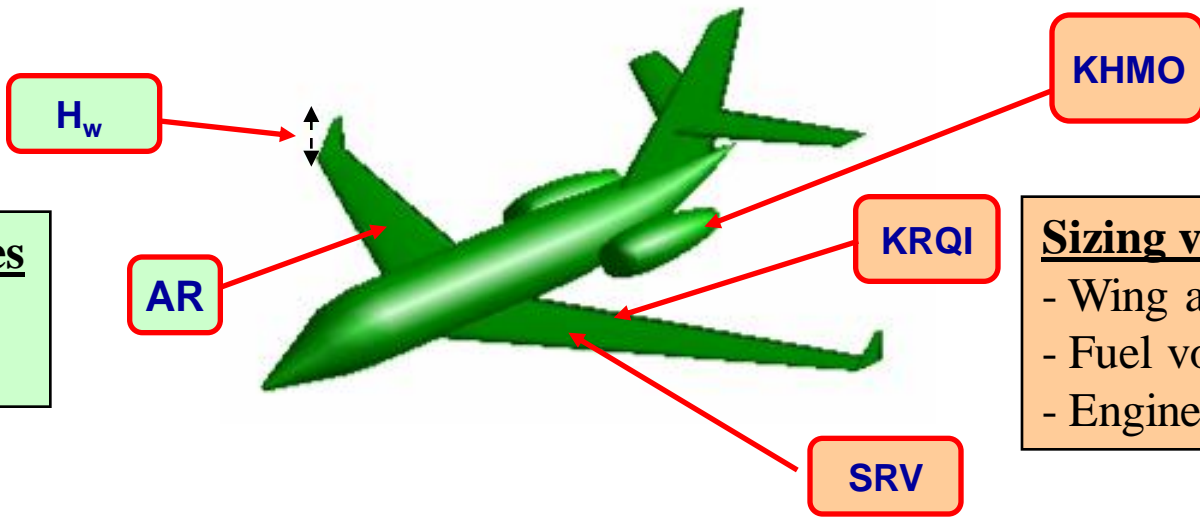
Trade off wing aspect ratio / winglet size for a given plan form

- Requirements**
- Low speed performances : BFL, LFL
  - Range @ economic cruise Mach number
  - Cruise altitude
  - Pax cabine volume and payload

- Sizing scenarios**
- Minimize carbon footprint @ economic cruise
  - Minimize weight

- Detailed analysis**
- Aerodynamics
  - Structures

- Sampling variables**
- Wing aspect ratio
  - Height of winglet



- Sizing variables**
- Wing area
  - Fuel volume
  - Engine size

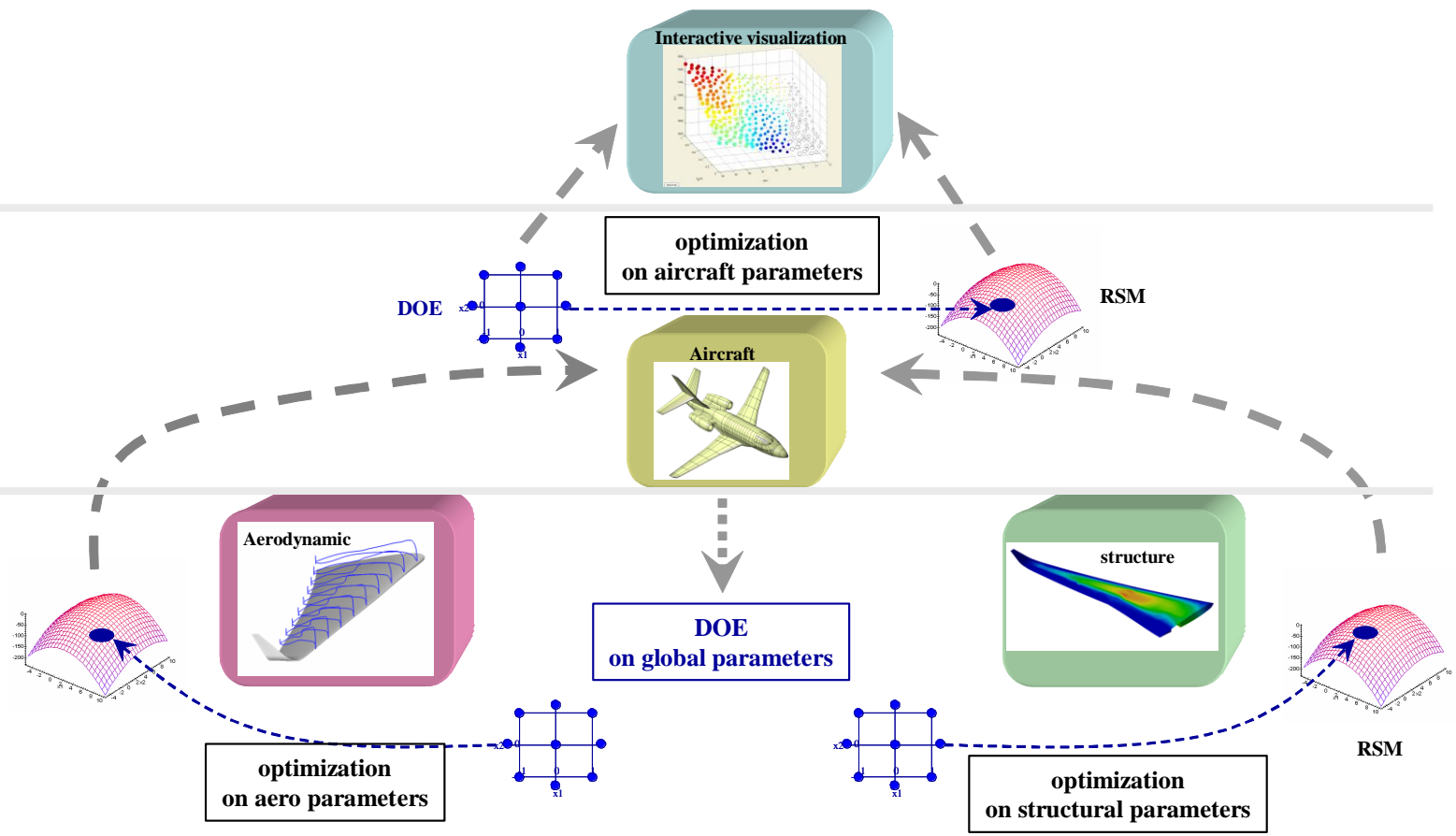


# Sketch of the process

Exploration of Design Space

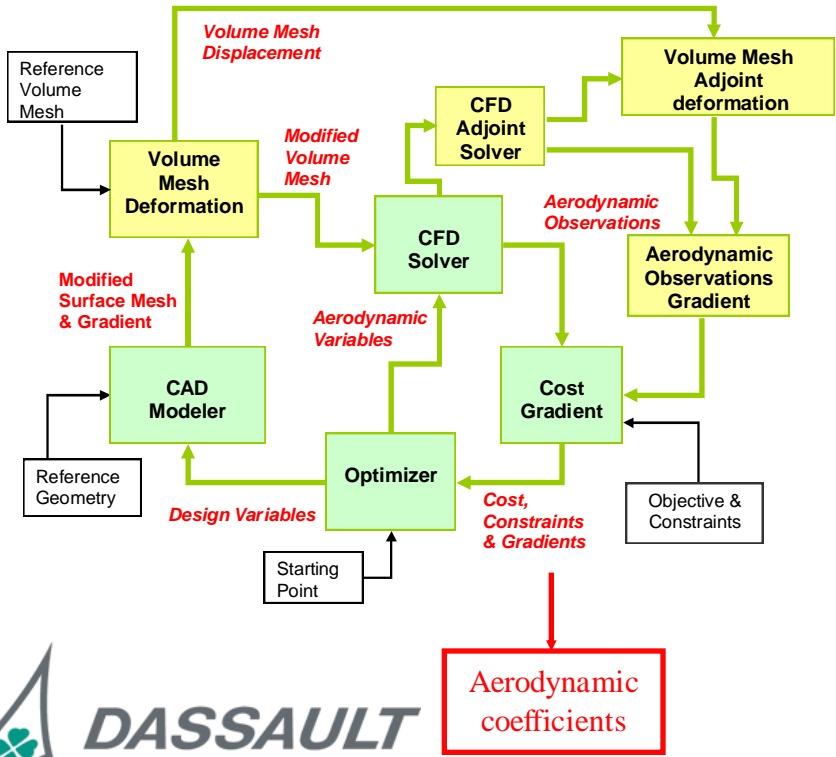
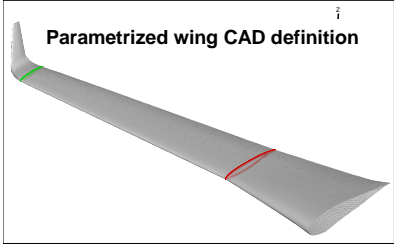
Synthesis at System level

Components performances

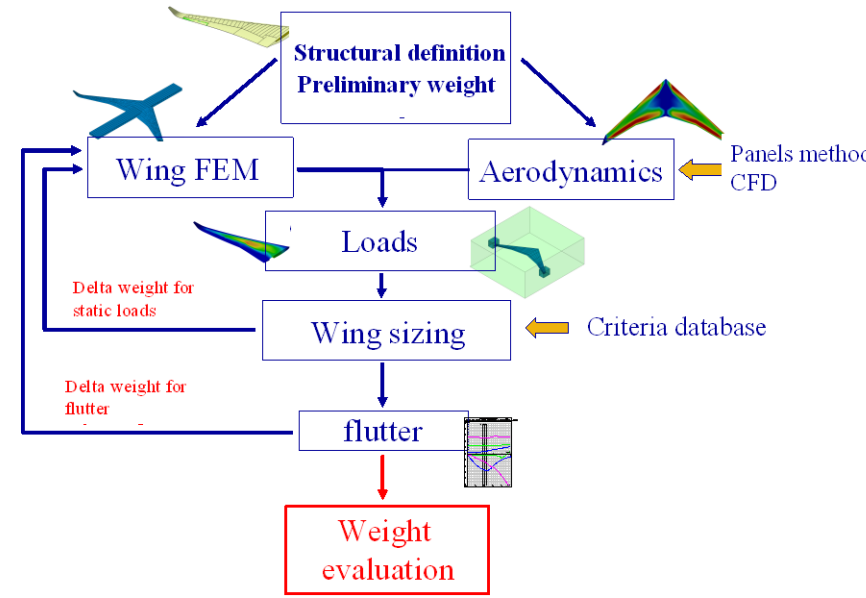
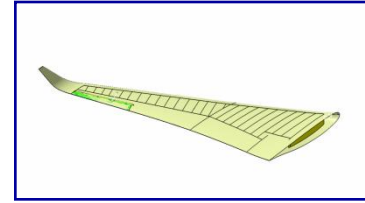


# Detailed analysis workflows

## Aerodynamic

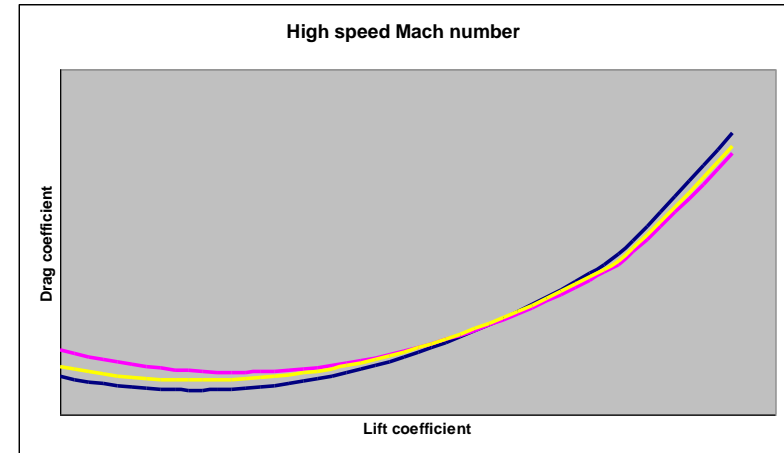
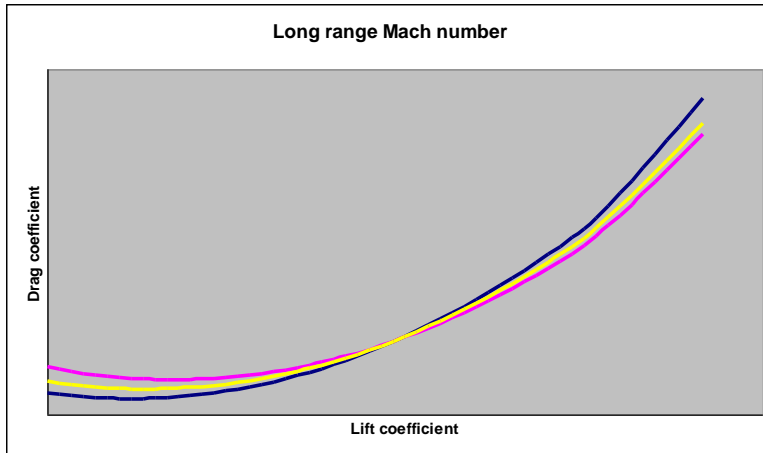
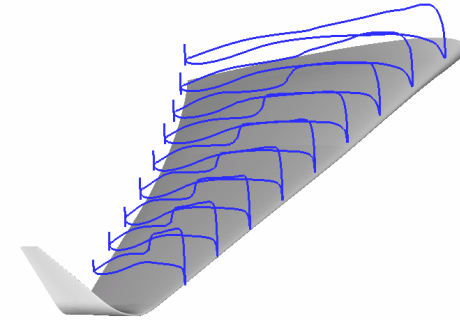


## Structural analysis



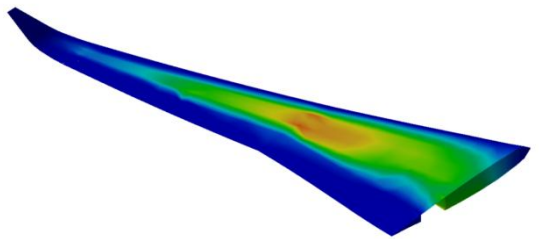
# Aerodynamic

## CFD analysis for 3 winglet heights

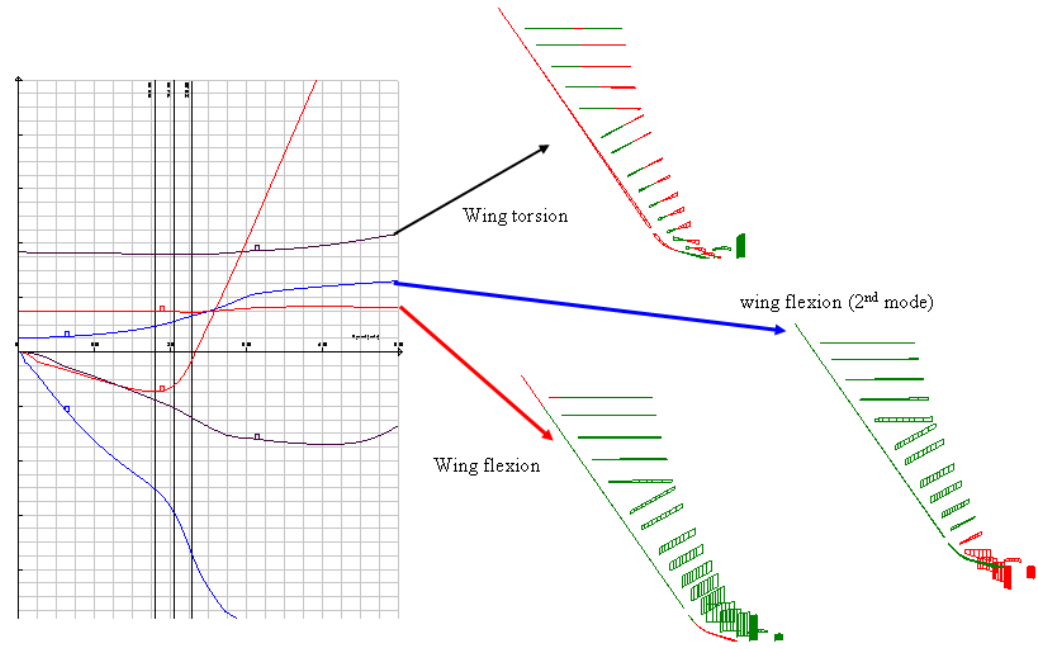


Aspect ratio : pre-existing surrogate model

# Structure

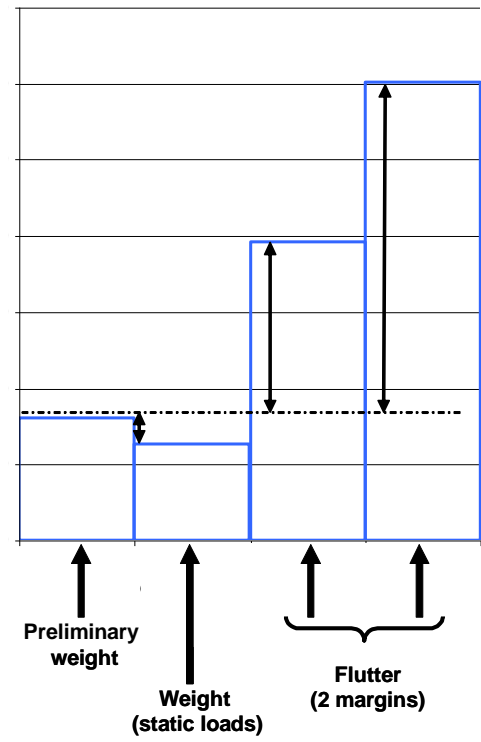


Stresses for a static load case



Flutter analysis

weight



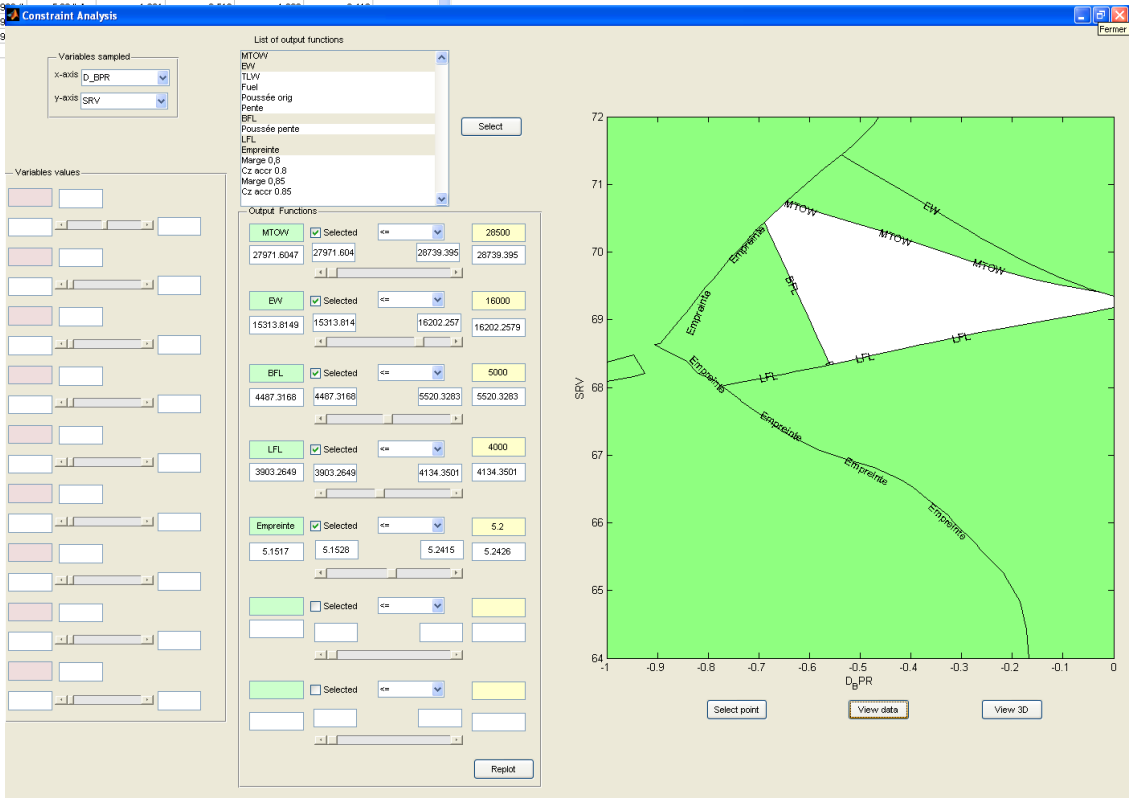
# Interactive design space exploration

Microsoft Excel - data\_16dec\_09.xls

|    | A     | B   | C         | D         | E         | F         | G            | H     | I        | J             | K        | L           | M         | N           | O          | P            | Q |
|----|-------|-----|-----------|-----------|-----------|-----------|--------------|-------|----------|---------------|----------|-------------|-----------|-------------|------------|--------------|---|
| 1  | D_BPR | SRV | MTOW      | EW        | TLW       | Fuel      | Poussée orig | Pente | BFL      | Poussée pente | LFL      | Empreinte   | Marge 0,8 | Cz accr 0,8 | Marge 0,85 | Cz accr 0,85 |   |
| 2  | 0     | 64  | 28 176 kg | 15 609 kg | 17 983 kg | 11 068 kg | 11 800 lbf   | 5,4%  | 4 852 ft | 11 063 lbf    | 4 134 ft | 5,19 lb/ftm | 1,446     | 0,548       | 1,433      | 0,442        |   |
| 3  | 0     | 66  | 28 335 kg | 15 757 kg | 18 135 kg | 11 079 kg | 11 800 lbf   | 5,4%  | 4 759 ft | 11 091 lbf    | 4 080 ft | 5,20 lb/ftm | 1,483     | 0,534       | 1,469      | 0,431        |   |
| 4  | 0     | 68  | 28 381 kg | 15 900 kg | 18 275 kg | 10 982 kg | 11 800 lbf   | 5,4%  | 4 634 ft | 11 072 lbf    | 4 028 ft | 5,15 lb/ftm | 1,371     | 0,519       | 1,320      | 0,419        |   |
| 5  | 0     | 70  | 28 557 kg | 16 050 kg | 18 428 kg | 11 007 kg | 11 800 lbf   | 5,4%  | 4 557 ft | 11 111 lbf    | 3 981 ft | 5,16 lb/ftm | 1,402     | 0,508       | 1,351      | 0,409        |   |
| 6  | 0     | 72  | 28 739 kg | 16 202 kg | 18 586 kg | 11 038 kg | 11 800 lbf   | 5,3%  | 4 487 ft | 11 153 lbf    | 3 937 ft | 5,18 lb/ftm | 1,433     | 0,497       | 1,380      | 0,401        |   |
| 7  | -0,5  | 64  | 28 074 kg | 15 459 kg | 17 840 kg | 11 115 kg | 10 997 lbf   | 4,5%  | 5 189 ft | 11 017 lbf    | 4 115 ft | 5,21 lb/ftm | 1,452     | 0,545       | 1,439      | 0,440        |   |
| 8  | -0,5  | 66  | 28 237 kg | 15 607 kg | 17 992 kg | 11 130 kg | 10 997 lbf   | 4,4%  | 5 095 ft | 11 047 lbf    | 4 062 ft | 5,22 lb/ftm | 1,489     | 0,532       | 1,475      | 0,429        |   |
| 9  | -0,5  | 68  | 28 284 kg | 15 750 kg | 18 132 kg | 11 034 kg | 10 997 lbf   | 4,5%  | 4 970 ft | 11 028 lbf    | 4 010 ft | 5,18 lb/ftm | 1,377     | 0,517       | 1,325      | 0,417        |   |
| 10 | -0,5  | 70  | 28 461 kg | 15 900 kg | 18 286 kg | 11 061 kg | 10 997 lbf   | 4,4%  | 4 833 ft | 11 067 lbf    | 3 964 ft | 5,19 lb/ftm | 1,408     | 0,506       | 1,356      | 0,408        |   |
| 11 | -0,5  | 72  | 28 644 kg | 16 052 kg | 18 443 kg | 11 093 kg | 10 997 lbf   | 4,2%  | 4 824 ft | 11 111 lbf    | 3 920 ft | 5,20 lb/ftm | 1,438     | 0,495       | 1,386      | 0,399        |   |
| 12 | -1    | 64  | 27 972 kg | 15 314 kg | 17 701 kg | 11 158 kg | 10 222 lbf   | 3,5%  | 5 520 ft | 10 973 lbf    | 4 096 ft | 5,23 lb/ftm | 1,457     | 0,543       | 1,444      | 0,438        |   |
| 13 | -1    | 66  | 28 139 kg | 15 462 kg | 17 854 kg | 11 177 kg | 10 222 lbf   | 3,5%  | 5 417 ft | 11 004 lbf    | 4 044 ft | 5,24 lb/ftm | 1,494     | 0,530       | 1,480      | 0,428        |   |
| 14 | -1    | 68  | 28 186 kg | 15 605 kg | 17 994 kg | 11 081 kg | 10 222 lbf   | 3,5%  | 5 276 ft | 10 985 lbf    | 3 992 ft | 5,24 lb/ftm | 1,494     | 0,530       | 1,480      | 0,428        |   |
| 15 | -1    | 70  | 28 365 kg | 15 755 kg | 18 145 kg | 11 110 kg | 10 222 lbf   | 3,5%  | 5 190 ft | 11 026 lbf    | 3 940 ft | 5,24 lb/ftm | 1,494     | 0,530       | 1,480      | 0,428        |   |
| 16 | -1    | 72  | 28 549 kg | 15 907 kg | 18 304 kg | 11 143 kg | 10 222 lbf   | 3,4%  | 5 112 ft | 11 070 lbf    | 3 888 ft | 5,24 lb/ftm | 1,494     | 0,530       | 1,480      | 0,428        |   |

before

now



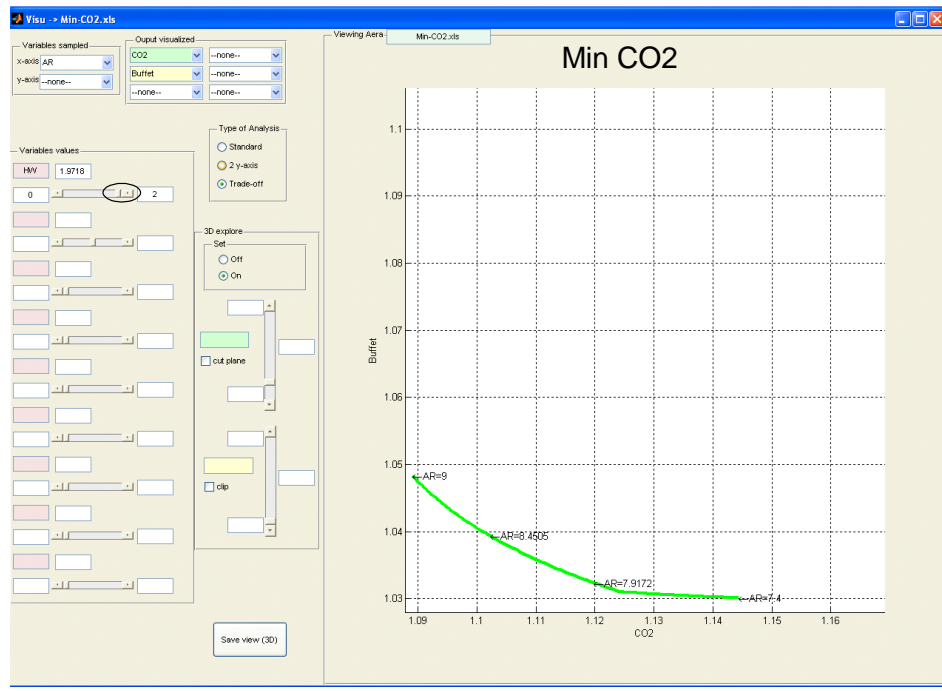
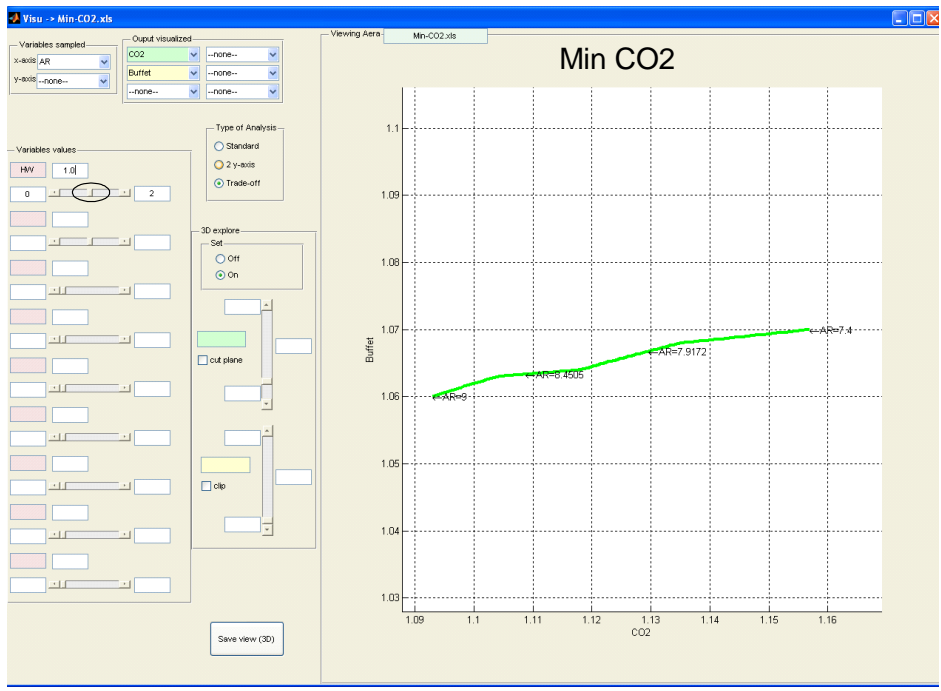
# ***Interactive exploration benefits***

**“Tell me and I'll forget; show me and I may remember; involve me and I'll understand.”**

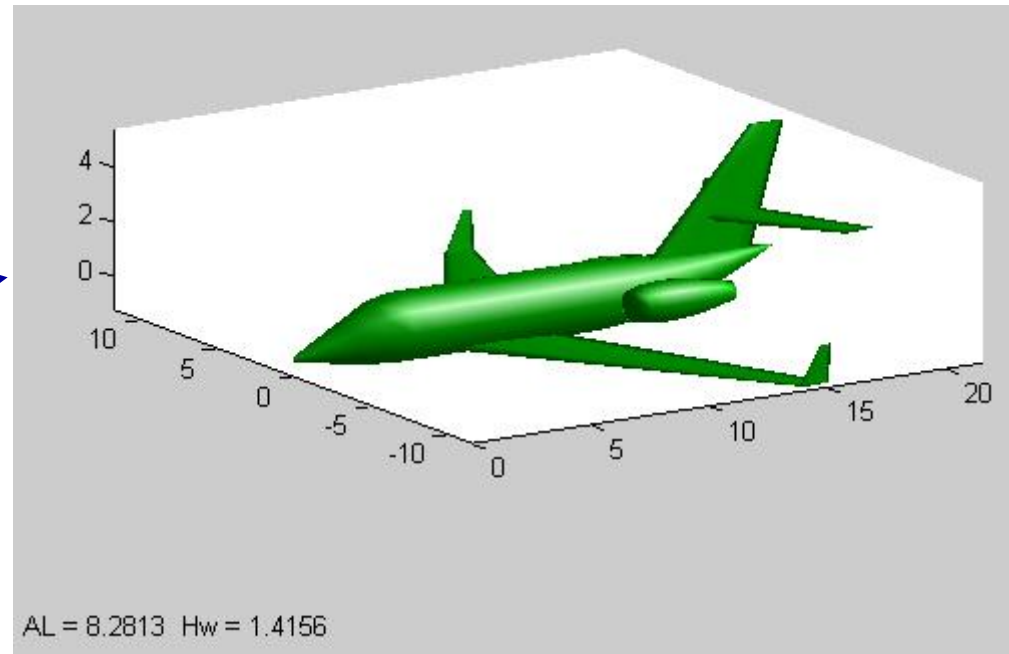
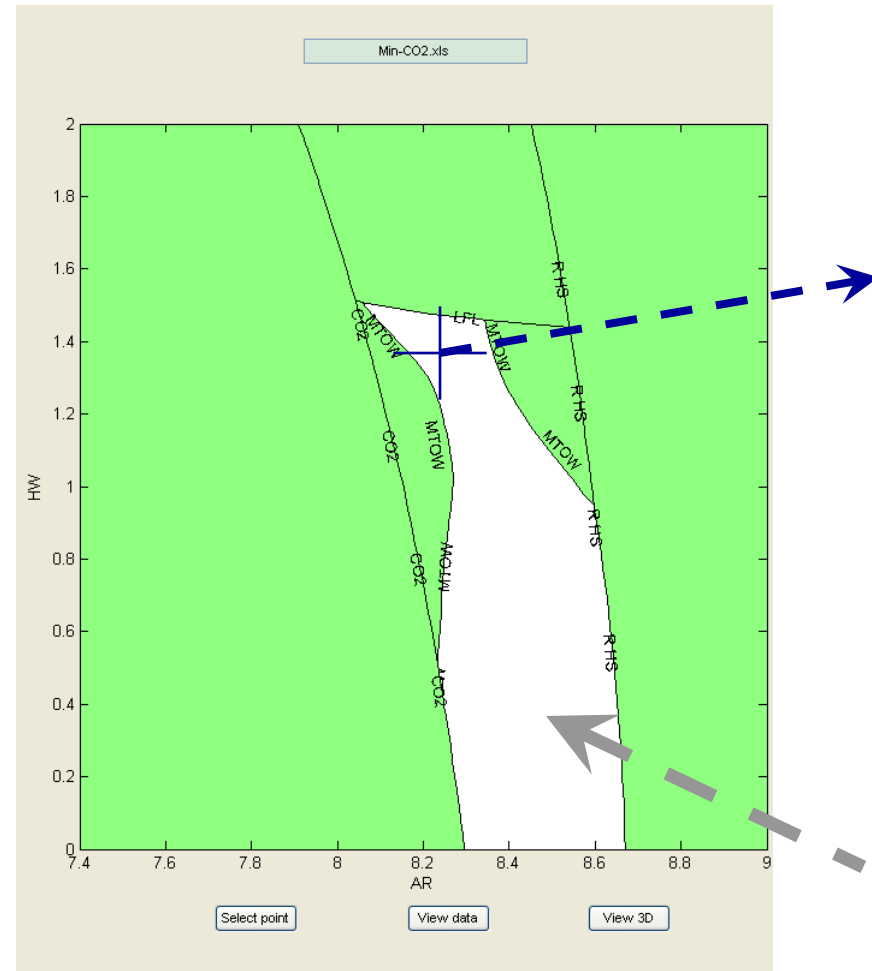
*Chinese proverb*

- **Immerse the decision makers within the space of compromise to enable them to better understand what they need by providing them immediate answers to their questions.**
- **Collaborative visualization ensures that all stakeholders can measure the impact of the multiple interactions and be able to trace the analysis at the system level.**
- **Efficiently manage the trade off between breadth and depth: each compromise decided at the system level allows focusing future efforts on smaller areas but with an increase in the depth of details.**

# Interactive trade off analysis



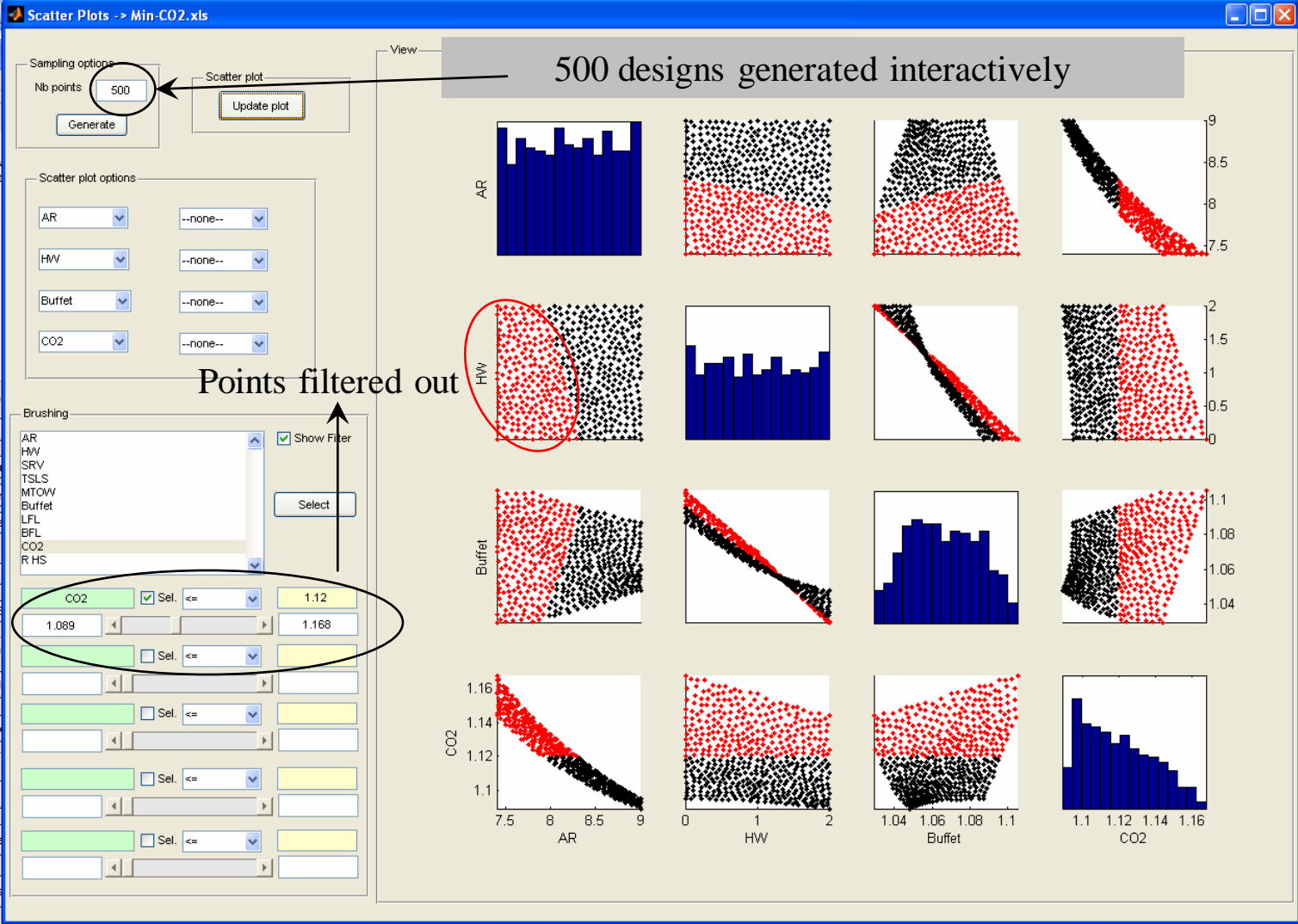
# Interactive constraints analysis



Feasible design space

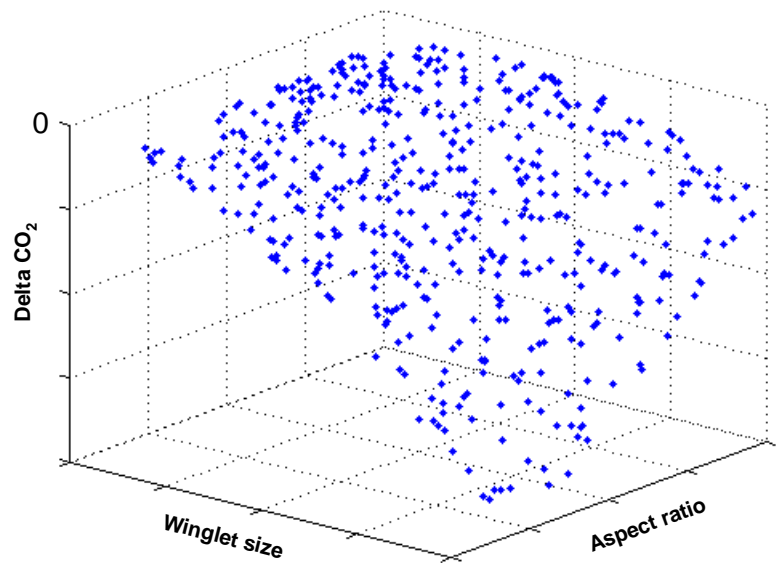


# Filtered scatter plots

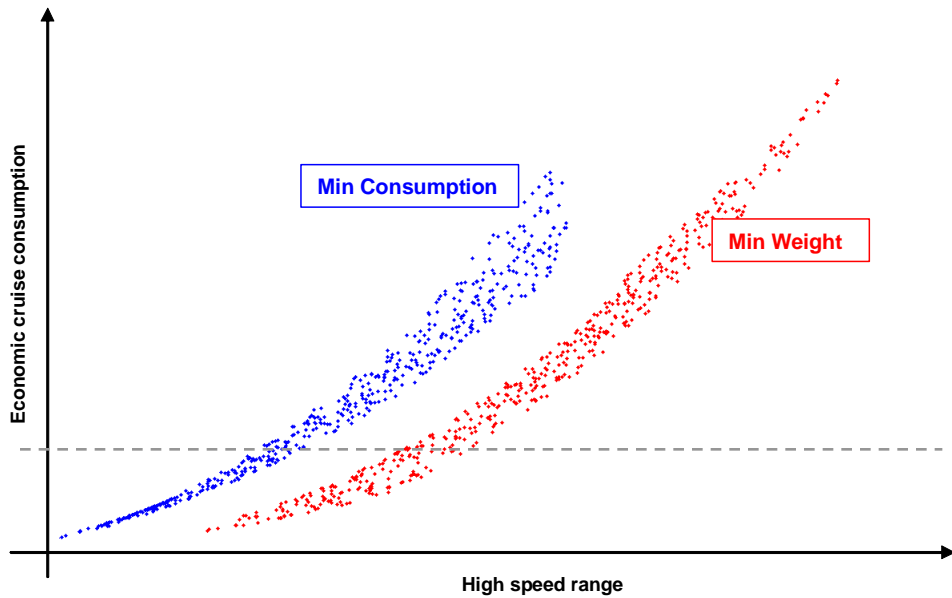


# More detailed comparison

500 designs



Delta CO<sub>2</sub> "Min CO<sub>2</sub> - Min weight"



Trade off CO<sub>2</sub> vs high speed range

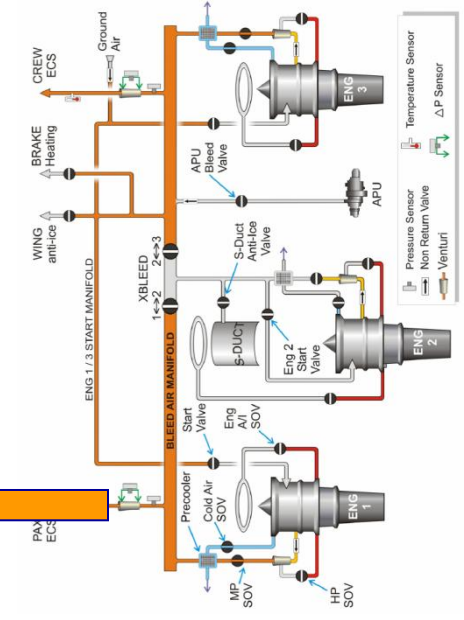
Selected design region must result of a comparative analysis of *all the performances*

Multicriteria Decision Making

# Aircraft Environmental Control System



ECS



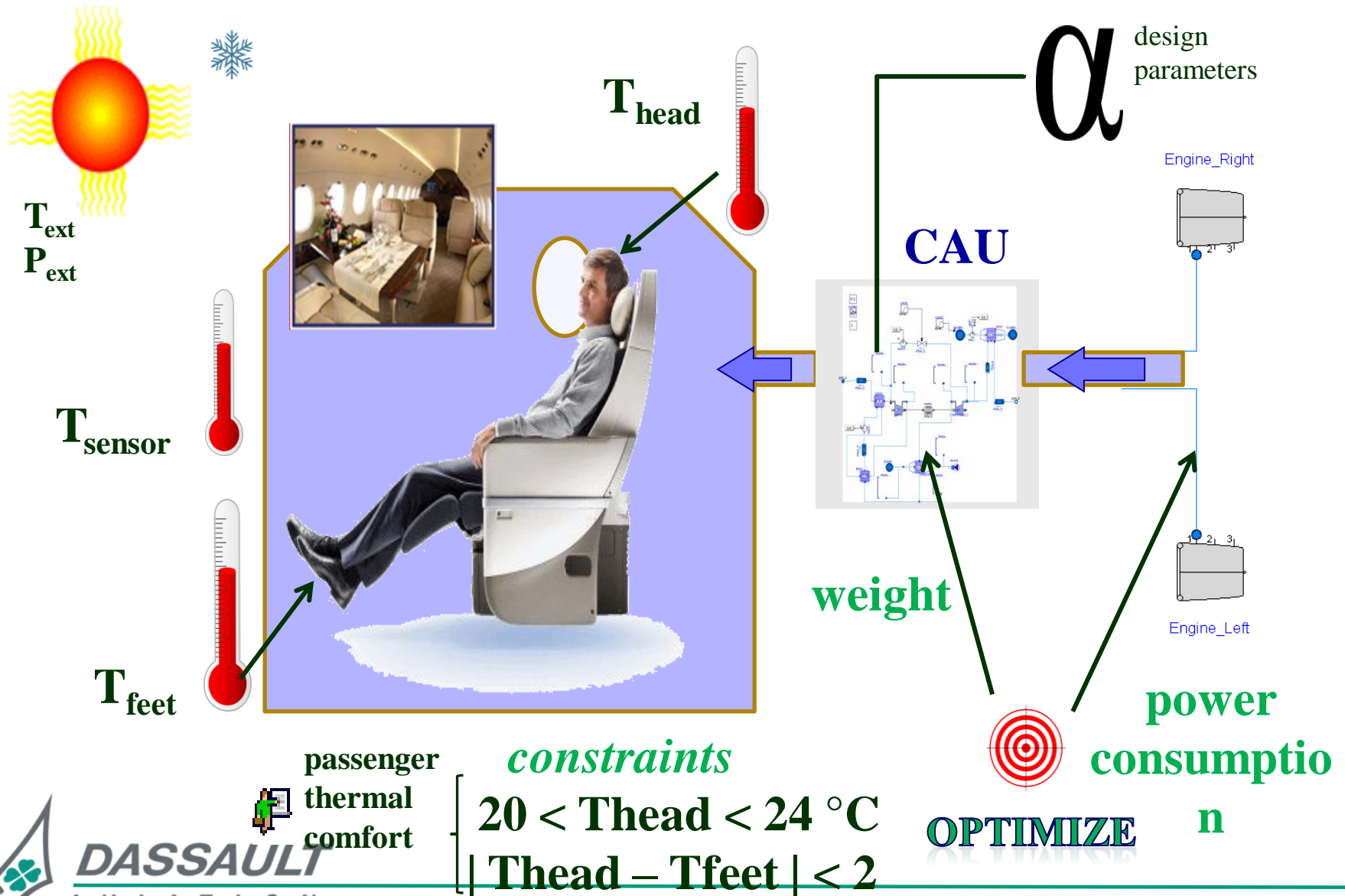
Engine bleed air



AVIATION

Direction Générale Technique

# Sizing of the Cold Air Unit

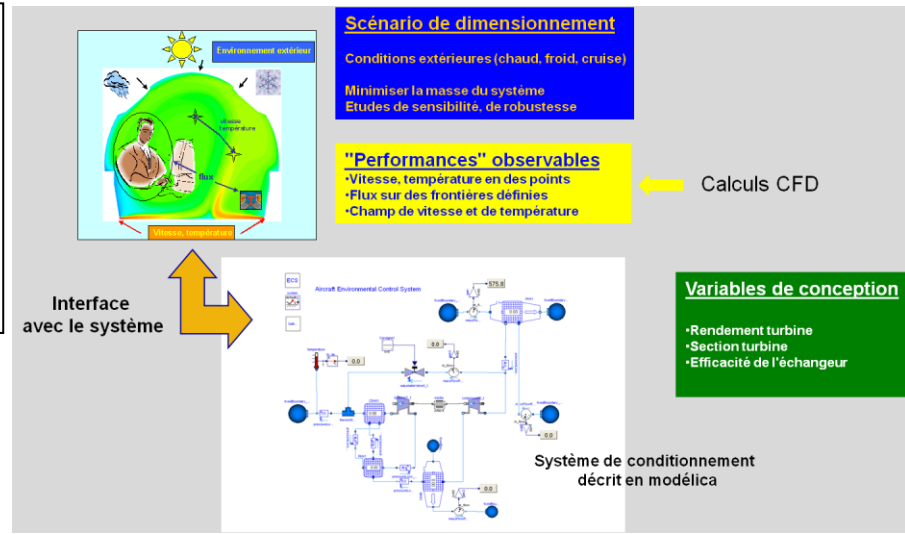


# Design of an ECS system

**Objective :** Size the different elements of the ECS (turbine, heat exchanger) to maintain a comfortable temperature in the cabin on the ground during a hot day or during the high altitude cruise.

CFD computations in the cabin:  
- air flow  
- temperature  
The boundary conditions are specified by the ECS.  
The ECS is modeled using the Modelica language.

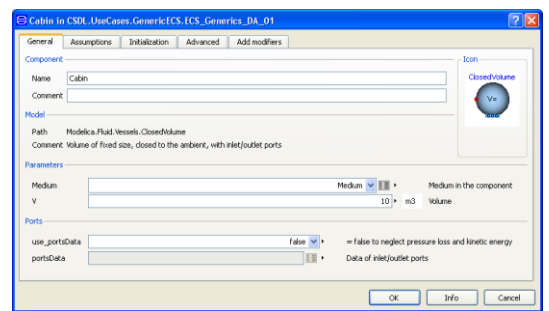
CFD computations : batch on HPC Clusters  
System simulation : interactive on PC (windows)



==> Methodology and process to  
- perform each simulation in its native environment  
- couple the different simulation to explore efficiently explore the design space  
- synthesize the results and support decision making  
  
==> Develop and integrate the elements of the new process.

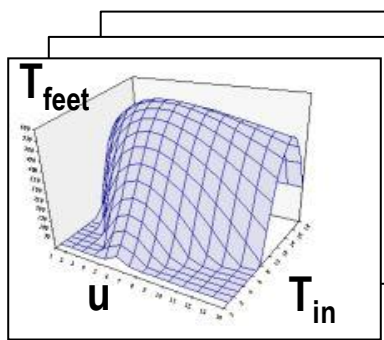
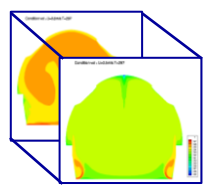
# Multi-level models

original  
Modelica  
component

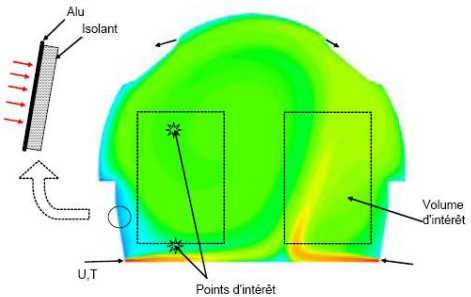


( Modelica.Fluid.Vessels.ClosedVolume )

surrogate models  
with associated accuracy



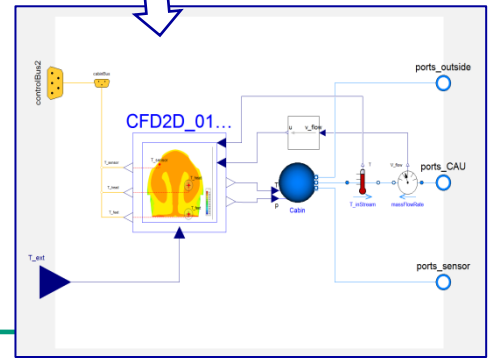
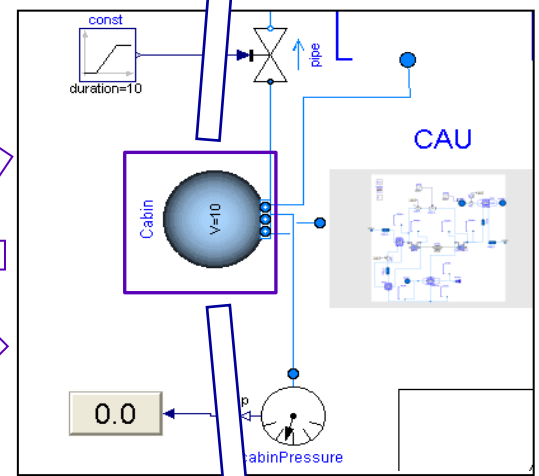
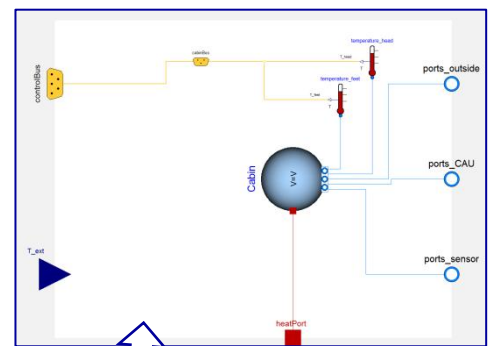
original  
CFD Model(s)



Low fidelity

Choice of  
adequate  
representation

High fidelity



Direction Générale Technique

Modelica ([www.modelica.org](http://www.modelica.org))

# Catia V6 Platform component

Manufacturing Hub - PPR

Engineering Hub - RFLP

**R**

Requirements

**F**

Functional Architectures

**L**

System Architectures & Behavior Modeling

**P**

3D Mechanical Design & FEM

**M**

Model

- Simulation
- Model
- Scenario
- Result

**R**

Result

**S**

Simulation Hub - MSR

Scenario

- RBF Generation rev -
- RBF Specification rev -
- RBF Computation rev -
- RBF integration in Logical Cabin rev -

**Program Central**

**COMPREHENSIVE PLM**

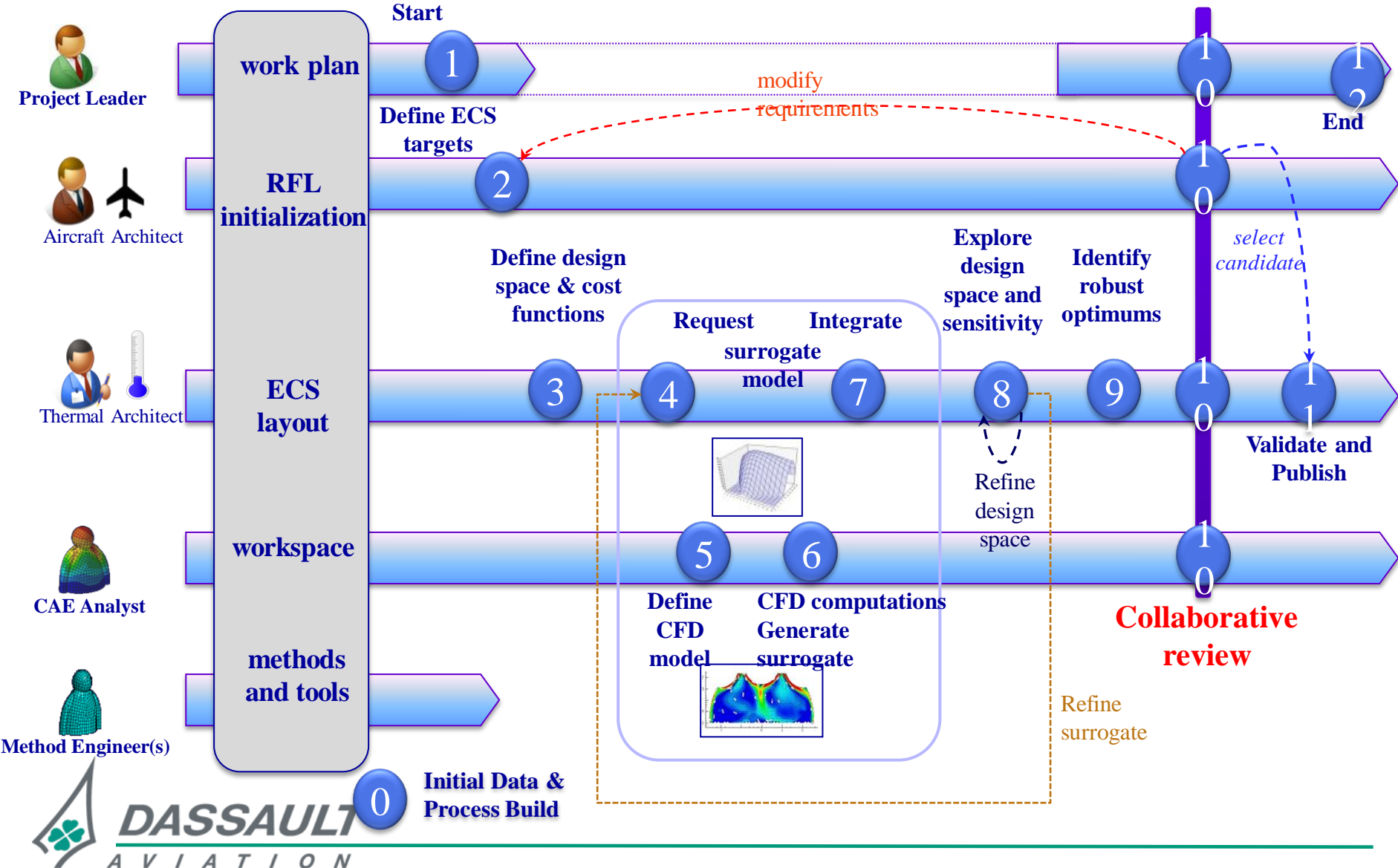
**VISUALIZATION**

**COMPUTATION**

**Standalone executables**

**HPC platform**

# Collaborative process

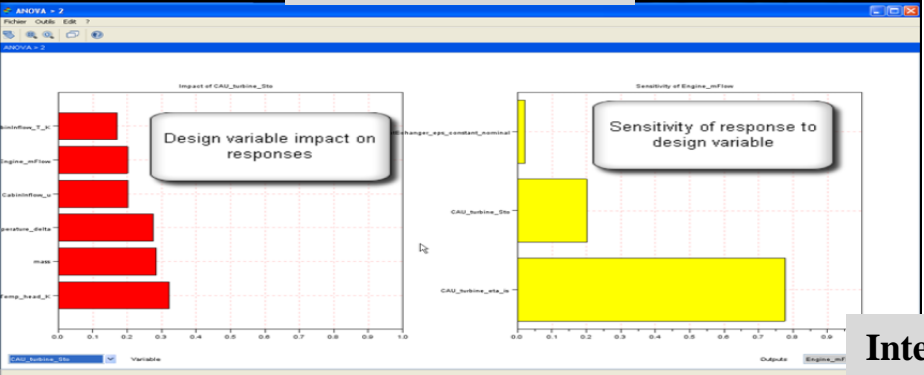




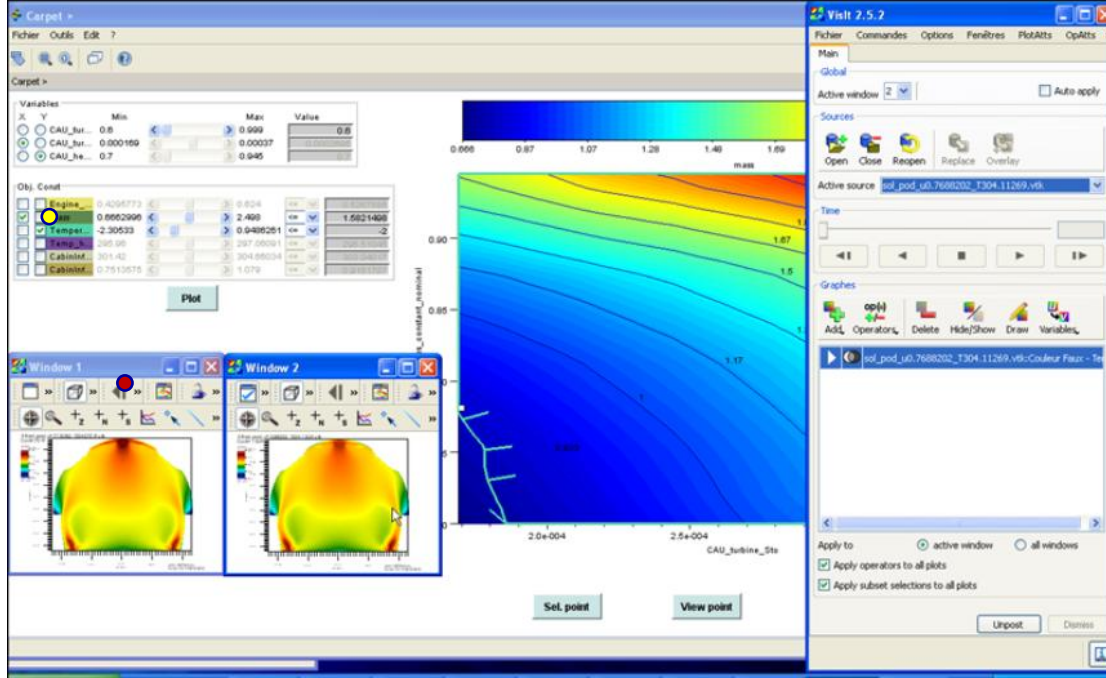
# Design review

## Sensitivity Analysis

Design space explored using surrogate models



Interactive links between performances and physical behavior



# Conclusions

- **Multi-level strategy based on surrogate models**
  - Enables the reuse of high fidelity simulations in different contexts
  - Allows asynchronous allocation of resources
  - Facilitates exchange of information
- **Improved awareness of the decision making process thanks to**
  - Numerical simulations and data sharing at the earliest stage of development
  - Systematic trade-off studies at all the levels of integration in a collaborative framework
- **Better project management through**
  - The assessment of the design margins on the final performances
  - The allocation of resources to the domains with the highest yield
- **PLM with parametric models**
  - Traceability from cradle to grave
  - Interactive collaborative design review

*Exploration efficiency still needs to be improved to better support decision making : towards a collaborative design lab sharing a digital mockup of the design space with all the associated parameterized performance models.*

