

Numerical and analytical investigation of the indirect noise in a nozzle

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Analytical and numerical assessments of the indirect noise generated through a nozzle are presented. The configuration corresponds to an experimental setup operated at DLR by Bake *et al.* (2008) where an entropy wave is generated upstream of the nozzle by means of an electrical heating device. Both 3-D and 2-D axisymmetric simulations are performed to demonstrate that the experiment is mostly driven by linear acoustic phenomena, including pressure wave reflection at the outlet and entropy-to-acoustic conversion in the accelerated regions. On the other hand, the spatial inhomogeneity of the upstream entropy fluctuation has no visible effect for the frequency range investigated (0-100 Hz). Results show that the acoustic impedance downstream of the nozzle must be accounted for appropriately in order to recover the experimental pressure signal. A good agreement is also obtained with a purely analytical assessment based on the compact nozzle approximation.

1. Introduction

Over the last five decades, jet and external aerodynamic noises of aircraft have been substantially reduced. Further developments will be needed for modern aircraft design in order to meet the increasingly restrictive rules about noise reduction; there is no doubt that Computational AeroAcoustics (CAA) will play a major role in these future developments. With the drastic jet noise reduction already achieved, the relative importance of other noise sources has increased and the contribution of these sources must be controlled if further global noise reduction is to be achieved. Among these sources, the noise stemming from the turbulent flame within the combustor is already identified as non-negligible at take-off, especially in the mid-frequency range. Two main mechanisms have been identified (Muthukrishnan *et al.* 1978; Cumpsty & Marble 1977; Pickett 1975) regarding noise propagation from the combustion chamber to the far field (see Fig. 1):

- **direct combustion noise:** acoustic perturbations generated by the unsteady heat release from the turbulent flame (Ihme *et al.* 2008) propagate either upstream or downstream through the turbomachinery stages and can reach the far field after it has been drastically distorted by the mean flow and also diffracted and reflected by the solid walls within the diffuser, the distributor and the turbine and compressor blades.

- **indirect combustion noise:** entropy fluctuations generated within the combustion chambers (hot spots, imperfect mixing, etc.) are propagated downstream and interact with accelerating mean flow. During this interaction, part of the energy contained in the entropy mode is transferred into the acoustic mode and the subsequent acoustic waves

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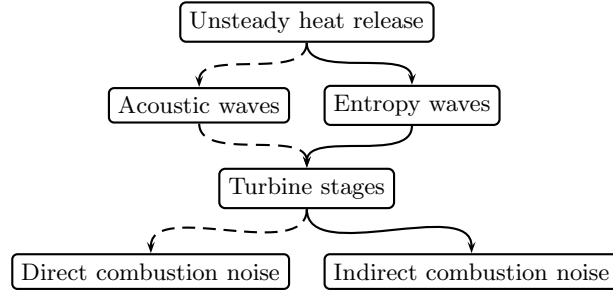


FIGURE 1. The two main mechanisms for noise generation from confined flames: direct (----) and indirect (—) noise.

are transmitted to the far field through the turbine stages in a similar way as for the direct combustion noise.

From the current knowledge and expertise regarding Large Eddy Simulations (LES) of turbulent reacting flows in complex geometries and the accuracy requirements regarding noise prediction in CAA, computing the absolute level of combustion noise from a realistic combustor is certainly out of reach of the actual computing/modeling capabilities. The objectives of this study are threefold:

- to assess/establish the capability of a state-of-the-art LES tool for the computation of compressible reacting flows to reproduce the entropy/acoustic interaction in the presence of a strong mean velocity gradient. To this end, the numerical results will be compared to the measurements from the entropy wave generator experiment studied at DLR by Bake *et al.* (2005, 2007, 2008),
- to gain insight into the first-order physical mechanisms that drive the pressure signal measured in the experiment. Notably the effect of (a) the entropy fluctuations shape and size and (b) the boundary conditions will be assessed,
- to investigate to what extent an analytical approach based on the compact nozzle approximation (Marble & Candel 1977; Leyko *et al.* 2007) and valid for 1-D planar waves can reproduce the experimental data of Bake *et al.* (2005).

The analytical relationships that can be derived under the compact assumption for plane waves are first reviewed in Sec. 2. The experimental setup and associated computational domain are then discussed in Sec. 3 where a short description of the LES solver is also provided. Finally, results are discussed in Sec. 4.

2. Theoretical background

This section builds upon the results obtained by Marble & Candel (1977), who focused on the generation and the transmission of flow perturbations (acoustic and entropy) through a steady non-uniform flow. Assuming a quasi-1-D nozzle flow and quasi-steady perturbations (nozzle compactness), they established the relations linking the different perturbations using mass flow, energy and entropy conservations. These developments are reviewed here to provide a better understanding of the indirect noise-generation mechanism.

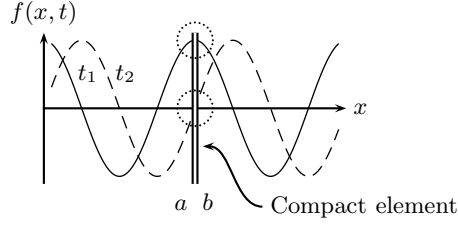


FIGURE 2. Compact element illustration: The quantity f , conserved throughout the element, is the same upstream (a) and downstream (b) at each instant.

2.1. Isentropic nozzle

Consider an isentropic flow of a homogeneous gas of density ρ , velocity u , pressure p , constant heat capacity c_p and $c_v = c_p/\gamma$ within a quasi-1-D adiabatic duct of cross-section area $\mathcal{A}(x)$. In this case, the mass flow

$$\dot{m} = \rho u \mathcal{A}, \quad (2.1)$$

the total temperature

$$T_t = T \left(1 + \frac{\gamma - 1}{2} \mathcal{M}^2 \right), \quad (2.2)$$

and the entropy

$$s = c_p \log \frac{p}{\rho^\gamma}, \quad (2.3)$$

are constant throughout the duct. The above relations can be differentiated to yield:

$$\frac{ds}{c_p} = \frac{dp}{\gamma p} - \frac{d\rho}{\rho}, \quad (2.4)$$

$$\frac{d\dot{m}}{\dot{m}} = \frac{1}{\mathcal{M}} \frac{du}{c} + \frac{dp}{\gamma p} - \frac{ds}{c_p} \quad (2.5)$$

and

$$\frac{dT_t}{T_t} = \frac{1}{1 + \frac{\gamma-1}{2} \mathcal{M}^2} \left((\gamma - 1) \mathcal{M} \frac{du}{c} + (\gamma - 1) \frac{dp}{\gamma p} + \frac{ds}{c_p} \right) \quad (2.6)$$

where the speed of sound $c = \sqrt{\gamma p/\rho}$ and the Mach number u/c have been introduced.

Under the compact nozzle assumption (the wavelengths of the perturbations are large compared with the axial dimension of the nozzle), there is no delay and distortion between the inlet and the outlet of the nozzle. As a result, the instantaneous values of the mass flow, the total temperature and the entropy are conserved throughout the nozzle at each instant, as displayed in Fig. 2. In other words, the compact nozzle assumption allows writing:

$$[ds]_a^b = 0 \quad ; \quad [d\dot{m}]_a^b = 0 \quad ; \quad [dT_t]_a^b = 0 \quad (2.7)$$

where $[\]_a^b$ stands for the jump between downstream (index b) and upstream (index a) of the related object (subcritical nozzle, supercritical nozzle and normal shock). At this point, it proves useful to introduce the following reduced variables and acoustic waves (Marble & Candel 1977):

$$\nu = \frac{du}{c} \quad ; \quad \varphi = \frac{dp}{\gamma p} \quad ; \quad \sigma = \frac{ds}{c_p} \quad ; \quad P^+ = \frac{1}{2}(\varphi + \nu) \quad ; \quad P^- = \frac{1}{2}(\varphi - \nu) \quad (2.8)$$

obtained:

$$\begin{aligned}
\left(1 - \frac{\gamma-1}{2}\mathcal{M}_a\right) P_a^+ - \left(1 + \frac{\gamma-1}{2}\mathcal{M}_a\right) P_a^- - \frac{1}{2}\mathcal{M}_a\sigma_a &= 0 \\
\left(1 - \frac{\gamma-1}{2}\mathcal{M}_b\right) P_b^+ - \left(1 + \frac{\gamma-1}{2}\mathcal{M}_b\right) P_b^- - \frac{1}{2}\mathcal{M}_b\sigma_a &= 0 \\
P_a^+ + P_a^- &= P_b^+ + P_b^- \\
\sigma_a &= \sigma_b
\end{aligned} \tag{2.14}$$

In many practical cases, however, a residual shock stands downstream of the throat of a choked nozzle and the mean flow is not isentropic anymore.

2.2. Waves for a shock

The interaction of acoustic, entropy or vorticity waves with a shock wave is a complicated problem (Mahesh *et al.* 1995, 1997), but it can be managed quite well analytically in 1-D (Moase *et al.* 2007). By construction the flow immediately upstream and downstream of a normal shock is supersonic and subsonic, respectively. This means that four waves are ingoing in this case, namely P_a^+ , P_a^- , σ_a and P_b^- , while only two propagate in the outward direction, viz. P_b^+ and σ_b . The derivation of the outgoing waves as a function of the ingoing ones builds upon the classical jump relations through a normal shock which only depends on the upstream Mach number. This latter quantity is modified by the shock motion induced by the in-going waves. After some algebra, one obtains:

$$\begin{aligned}
(1 + \mathcal{M}_a^2 + 2\mathcal{M}_a^2\mathcal{M}_b) P_b^+ + (1 + \mathcal{M}_a^2 - 2\mathcal{M}_a^2\mathcal{M}_b) P_b^- &= \\
(1 + \mathcal{M}_a^2 + 2\mathcal{M}_a\mathcal{M}_b^2) P_a^+ + (1 + \mathcal{M}_a^2 - 2\mathcal{M}_a\mathcal{M}_b^2) P_a^- & \\
(P_b^+ + P_b^- - P_a^+ - P_a^-) (\gamma - 1) \frac{(\mathcal{M}_a^2 - 1)^2}{((\gamma - 1)\mathcal{M}_a^2 + 2)\mathcal{M}_a^2} &= \sigma_b - \sigma_a
\end{aligned} \tag{2.15}$$

Equations (2.15) generalizes the result given in Marble & Candel (1977) to the case where P_b^- is not zero and indicates that entropy fluctuations can be generated by the interaction between an acoustic wave and a shock.

3. Configuration

All the computations presented in this paper are related to the DLR experimental setup studied by Bake *et al.* (2008). A sketch of the so-called Entropy Wave Generator experiment is displayed in Fig. 3. It consists of an accelerated tube fed by entropy waves generated by an electric heating device located between the upstream plenum and the nozzle. The operating conditions are such that the nozzle is choked but not adapted so that a normal shock takes place just after the throat, within the divergent section. When accelerated through the nozzle, the small amplitude entropy fluctuations (of the order of 10 K) produce backward and forward propagating acoustic waves. The forward part of the generated noise is measured/analyzed by microphones located downstream the nozzle. The main physical parameters defining the operating conditions are presented in Table 1. Note that the heating duration is 100 ms which, with a bulk velocity of the order of 12 m/s, leads to an entropy perturbation of typical length of the order of 1200 mm while the nozzle is about 263 mm long. This is most likely not relevant to practical engine applications where the expected length of the entropy spots is more likely on the order of 100-200 mm.

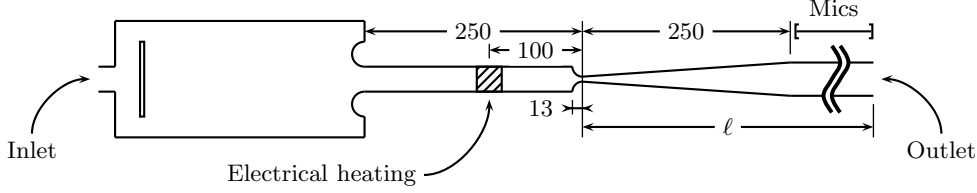


FIGURE 3. Principle of the Entropy Wave Generator experiment (lengths are given in mm).
Short configuration: $\ell = 500$ mm; **Long configuration:** $\ell = 2100$ mm

Plenum pressure	Outlet pressure	Inlet Mach	Shock Mach	Outlet Mach
117,000 Pa	100,800 Pa	0.037	1.340	0.023
Plenum temperature	Pulse amplitude	Pulse duration	Pulse length	
298 K	9 K	100 ms	1000 ms	
Convergent length	Divergent length	Throat diameter	Inlet diameter	Outlet diameter
13 mm	250 mm	7.5 mm	30 mm	40 mm

TABLE 1. Main characteristics of the experimental/numerical experiment

The numerical tool used in this study is the unstructured combustion code AVBP developed at CERFACS (AVBP 2008). AVBP solves the complete Navier-Stokes equations in two and three spatial dimensions. The unstructured approach allows computing not only the nozzle but also the whole air feeding line as well as the exhaust system. This code was selected because it solves the complete compressible Navier-Stokes equations and can naturally account for the energy transfer between the entropy and the acoustic modes of oscillation. The numerical method used is based on a weighted residual, Taylor-Galerkin discretization which is third order in both space and time (Colin & Rudgyard 2000) in order to minimize the dispersion/dissipation errors.

The main characteristics of the simulations performed are presented in Table 2. The entries "short" and "long" refer to the two types of computational domain depicted in Fig. 3. They both include the upstream plenum and the heating section but the "short" one extends only 500 mm downstream of the nozzle throat (length ℓ) while the "long" contains the exhaust duct until the entrance to the anechoic part, viz. approx. 2100 mm downstream of the nozzle. "BC" refers to the boundary condition prescribed at the outlet of the computational domain which can be either non-reflecting, fully reflecting or corresponds to a finite (neither zero nor infinite) acoustic impedance. The "heating" entries correspond to the shape of the temperature pulse: it is 1-D in most cases (viz. uniform in the plane normal to the duct) or it can depend on the distance r to the axis (viz. non-uniform in the cross-section; in the present case, the heating source term is

Run	Geometry	Length	BC	Heating
3D-1	3D	short	non-reflecting	uniform
2D-1	2D axi	short	non-reflecting	uniform
2D-2	2D axi	short	non-reflecting	non-uniform
2D-3	2D axi	short	reflecting	uniform
2D-4	2D axi	long	finite impedance	uniform

TABLE 2. Main characteristics of the small-scale simulations.

proportional to $\cos(r/R \cdot \pi/2)$, with R the radius of the upstream duct). The uniform and non-uniform heatings correspond to the same overall energy so that the comparison between the runs 2D-1 and 2D-2 can provide relevant information regarding the effects of the inhomogeneity of the entropy perturbation on the noise generated. In the same way, comparing runs 2D-1 and 2D-3 will provide information about the sensitivity of the results to the outlet boundary condition while comparing 3D-1 and 2D-1 will be relevant to quantify the 3-D effects in the observed results. At last, run 2D-4 is designed to mimic, as much as possible, the experimental downstream acoustic impedance[†]. In all cases, the mesh resolution is enough to represent the propagation of the entropy and acoustic waves in the duct without significant dissipative/dispersive errors (mesh size on the order of 1mm compared to the perturbation size on the order of 1200 mm; see Sec.3). The 3-D mesh is rather coarse with 1.2 million tetraedras, corresponding to approximately 15 cells in a cross-section. The mesh density is equivalent for 2-D axisymmetric cases. Note that the mesh refinement is not sufficient to resolve the residual shock appropriately which, given the non-dissipative character of the numerical method, can lead to numerical instabilities. Thus extra numerical dissipation has been added in both 3-D and 2-D axisymmetric calculation in the region downstream of the throat of the nozzle.

In order to mimic the experimental heating device, a source term is added to the energy equation. It reads:

$$S(x, t) = S_0 \cdot \frac{1}{2} \left[\tanh \left(\frac{x - x_0 + L_s/2}{a} \right) \cdot \tanh \left(-\frac{x - x_0 - L_s/2}{a} \right) + 1 \right] \cdot s(t)$$

where $L_s = 30$ mm is representative of the length of the experimental heating zone and $a = 3$ mm enables to smooth sufficiently the source term to avoid numerical issues. Moreover, the average location x_0 of the source term has been consistently chosen with the location of the electrical device in the experiment (100 mm upstream of the nozzle

[†] Not available in Bake *et al.* (2005, 2007, 2008) but kindly provided by Dr. Ing. F. Bake during the course of this study.

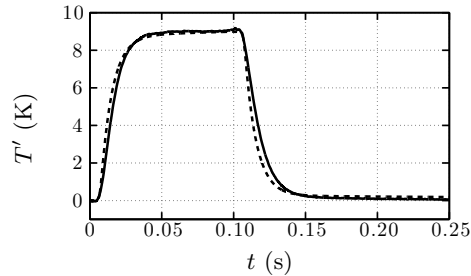


FIGURE 4. Time traces of the experimental (—) and numerical (---) temperature downstream of the heating location.

throat). The temporal evolution $s(t)$ is defined as the following:

$$s(t) = \begin{cases} 1 - e^{-\frac{t-t_0}{\tau}} & \text{if } t \in [t_0, t_0 + T] \\ s(t_0 + T)e^{-\frac{t-t_0}{\tau}} & \text{if } t > t_0 + T \end{cases}$$

where t_0 is the time when the electrical device is triggered, T is the pulse duration and is equal to 100 ms and $\tau = 8$ ms. As shown in Fig. 4, these numerical parameters allow a fair representation of the temperature fluctuation produced in the experiment. The next section analyzes the results obtained in terms of pressure fluctuations generated downstream when the temperature perturbation displayed in Fig. 4 passes through the nozzle.

4. Results

The EWG setup has been studied both numerically and analytically during this study. Numerical simulations have the advantage of integrating all the possible effects involved in the entropy noise generation and contained in the Navier-Stokes equations. The analytical approach is valid only under the compact nozzle assumption and in the linear regime.

The time traces of the pressure computed 350 mm downstream of the throat are displayed in Fig. 5 for runs 2D-1, 2D-2, 2D-3 and 3D-1 together with the experimental signal. Clearly enough, these simulations do not reproduce the experimental data, neither in terms of amplitude, nor in terms of signal shape. For runs 2D-1 and 3D-1, the numerical pressure trace has a top-hat behavior similar to the temperature upstream fluctuation, while the experiment shows a wavy behavior at a frequency close to 30 Hz. The figure also indicates that 3D-1 leads to results very similar to 2D-1, indicating that the disagreement between the 2D-1 computation and the experimental data cannot be attributed to 3-D effects. The same conclusion can be drawn for the temperature inhomogeneity which appears to have no effect, at least for the configuration considered (comparing 2D-1 and 2D-2). On the other hand, Fig. 5 illustrates how large the effects of the downstream acoustic boundary condition can be. When a fully reflecting condition (which imposes pressure) is used instead of a non-reflecting one (which essentially sets the incoming acoustic wave to zero at the outlet), the amplitude decreases drastically. More importantly, the shape of the signal is also strongly modified by the superposition of the downward and backward pressure waves. A wavy behavior is obtained with run 2D-3, although with characteristic amplitude and frequency in quantitative disagreement with the experiment. The previous results suggest that the discrepancies observed in Fig.5 might be related to an incorrect downstream acoustic impedance. Indeed, the short

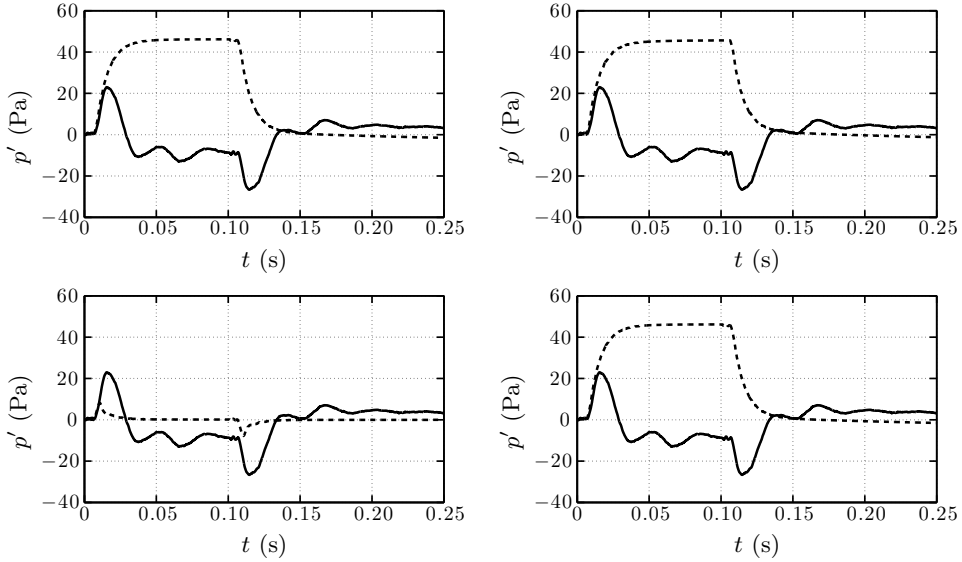


FIGURE 5. Time traces of the fluctuating pressure 350 mm downstream of the nozzle. Experimental data: —; Numerical result: - - - . **Top left:** run 2D-1; **Top right:** run 2D-2; **Bottom left:** run 2D-3; **Bottom right:** run 3D-1.

computational domain and non-reflecting BC used in runs 2D-1, 2D-2 and 3D-1 would only be representative of the actual experimental conditions if a perfect anechoic system would have been used by Bake *et al.* (2008). Actually, Fig. 6 demonstrates that this is not the case and that substantial reflection occurs, especially in the low frequency range: the modulus of the reflection coefficient, defined as the ratio of the backward wave to forward wave at the outlet, is as large as 0.5 at 30 Hz, the typical frequency of the reflections observed in the experimental signal (see Fig. 5). Accounting for a complex-valued, frequency-dependent reflection coefficient in a CFD code solving the flow equations in the time domain is not an easy task although it can be theoretically done by making use of recursive/non-recursive digital filters. A simpler approach has been followed in the present study. Instead of using a non-reflecting outlet boundary condition with zero entering wave L^- , it is common use to write the latter as a pressure difference times a relaxation coefficient κ (Poinsot & Lele 1992), viz. $L^- = 2\kappa\Delta t \cdot (p_{\text{ref}} - p_B)/(\rho c)$, with Δt the time step, p_B the nodal pressure at the outlet boundary and p_{ref} the reference pressure. In doing so, the outlet condition acts as a first-order low pass filter (Selle *et al.* 2004) whose cut-off frequency is inversely proportional to κ and the reflection coefficient R reads:

$$R = -\frac{1}{2i\omega/\kappa + 1} \quad (4.1)$$

It is thus possible to tune the relaxation coefficient κ in order to mimic the amplitude of the experimental reflection coefficient, at least in the low-frequency range. The length ℓ of the downstream duct is then tuned in such a way as to mimic the experimental time delay as well as to compensate for the phase of the relaxation-based outlet partially reflecting condition. The experimental reflection coefficient is considered here to be measured at the nozzle throat ($x = 0$) while the reflection coefficient of numerical boundary condition (Eq. (4.1)) is given at the end of the computational domain ($x = \ell$). The experimental

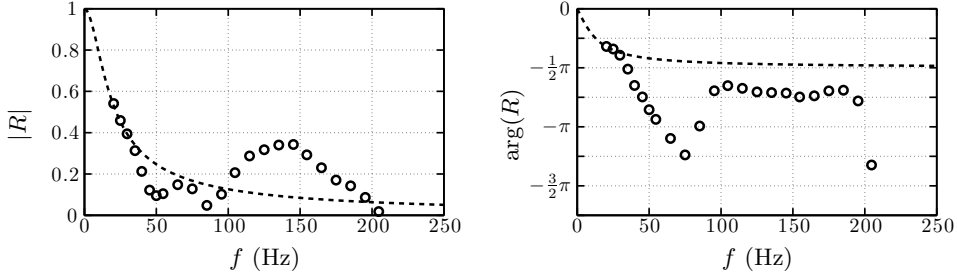


FIGURE 6. Experimental reflection coefficient shifted 2100 mm downstream of the nozzle throat and numerical reflection coefficient. **Shifted experimental data:** \circ ; **Tuned relaxation coefficient:** ---- .

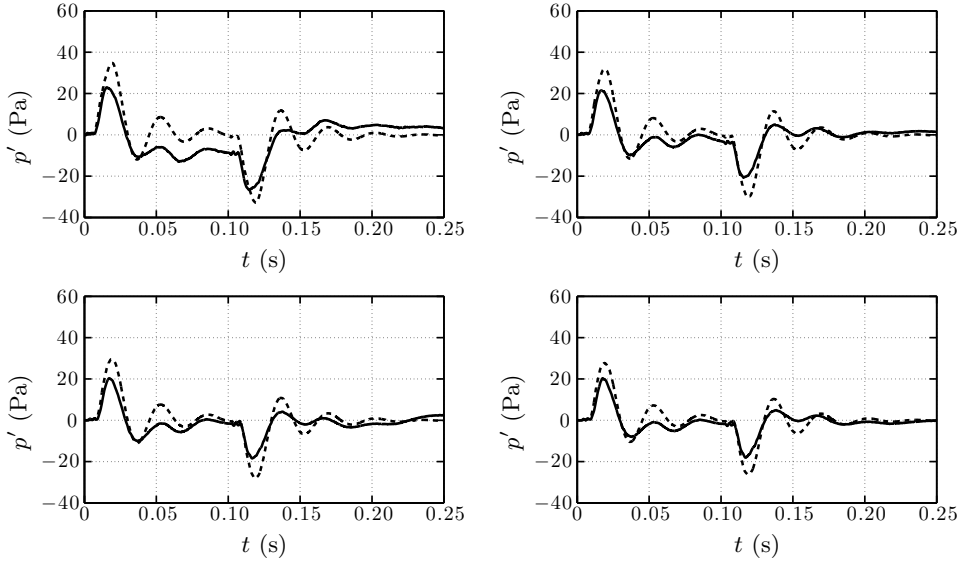


FIGURE 7. Time traces of the fluctuating pressure downstream of the nozzle. Experimental data: — ; Run 2D-4: ---- . Distance downstream of the nozzle : **Top left:** 350 mm; **Top right:** 730 mm; **Bottom left:** 975 mm; **Bottom right:** 1150 mm.

reflection coefficient is thus multiplied by $\exp(-2\ell\omega/c)$ in order to shift it to the same position, at the end of the numerical domain ($x = \ell$). The experimental reflection coefficient obtained in this way is depicted in Fig. 6 where a fair agreement with the numerical one is apparent in the frequency range 20-40 Hz. The "optimized" relaxation coefficient κ and length ℓ are close to 160 s^{-1} and 2100 mm. As anticipated, Fig. 7 indicates that the numerical pressure signal is in better agreement with the measured one when accounting more accurately for the effective downstream boundary condition.

It is also possible to perform these calculations analytically. This can be done using the relations presented previously for the supercritical nozzle (Eq. (2.14)), the normal shock (Eq. (2.15)) and the subcritical nozzle (Eq. (2.9)). The supercritical nozzle starts at point 1 at the nozzle inlet and finishes at point 2 in the divergent section where the normal shock takes place. The normal shock relations are defined between point 2 and 3 and finally the subcritical nozzle starts at point 3, downstream of the shock, and finishes at point 4 at the end of the divergent section as shown in Fig. 8. Only the

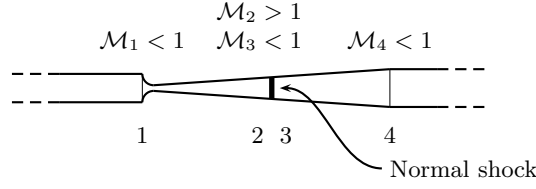


FIGURE 8. Description of the analytic approach

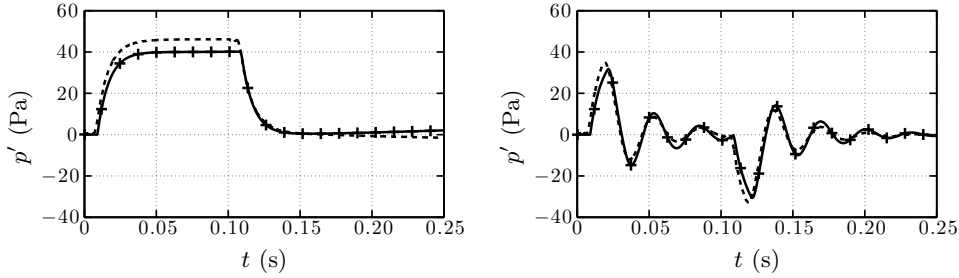


FIGURE 9. Time traces of the fluctuating pressure downstream of the nozzle. Numerical results: ---- ; Analytical results: - + -. **Left:** Non-reflecting case (Analytic compared to Run 2D-1); **Right:** Finite impedance case (Analytic compared to Run 2D-4).

entropy wave generated by the electrical device is taken into account and the upstream part of the nozzle is assumed to be non-reflecting (even if this is not the case in the real configuration). The subsonic nozzle outlet is represented in a general manner by the reflection coefficient $R = P_4^- / P_4^+$, but it will be considered to be infinitely small for the non-reflecting calculation ($R \ll 1$ for numerical issues) and to be equal to the tuned reflection coefficient of the numerical computation 2D-4 for the "real" case. The entropy wave temporal evolution is proportional to the one imposed on the source term on energy in the numerical computation. All the analytical calculations are performed in the frequency domain in order to take into account the frequency dependence of the outlet boundary condition in the real case, but the different nozzle elements are still assumed to be compact. Since the case of a shock in the divergent section is considered here, the supercritical nozzle (from 1 to 2) can be treated independently of the downstream elements, and provide explicitly the waves entering the downstream elements. The shock (from 2 to 3) and the subcritical nozzle with the outlet BC (from 3 to 4) have to be treated together since most of the waves are coupled. Finally, one obtains the reduced pressure fluctuation $\varphi_4(\omega)$ in the frequency domain as a function of the four Mach numbers \mathcal{M}_1 , \mathcal{M}_2 , \mathcal{M}_3 and \mathcal{M}_4 (\mathcal{M}_3 and \mathcal{M}_4 are actually linked by the shock relations), the reflection coefficient $R(\omega)$ and the reduced entropy fluctuation $\sigma_1(\omega)$. The time evolutions of the pressure fluctuations reconstructed from the analytical calculations are compared to the numerical computations. Figure 9 shows a very good agreement between these two approaches. This demonstrates that the EWG experiment (for the given regime) is essentially driven by linear quasi-1-D acoustics.

5. Conclusions

The numerical and analytical analysis performed in this study demonstrates that the pressure signals obtained in the EWG experiment by Bake *et al.* (2008) result from two main mechanisms:

- the entropy-to-acoustic conversion due the strong mean velocity gradient in the nozzle, including the normal shock that stands just downstream of the throat,
- the acoustic reflection within the exhaust system downstream of the nozzle and test section.

Moreover, in the low frequency range investigated, only 1-D planar waves are present and the compact nozzle approximation is valid, even for the entropy perturbations. As a result, the pressure signals observed experimentally and numerically can be nicely reproduced by a simple quasi-1-D analytical model derived in the zero frequency limit for the nozzle.

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REFERENCES

- AVBP 2008 AVBP Code: www.cerfacs.fr/cfd/avbp_code.php and www.cerfacs.fr/cfd/CFDPublications.html.
- BAKE, F., KINGS, N. & ROHLE, I. 2008 Fundamental mechanism of entropy noise in aero-engines: experimental investigation. *J. Eng. Gas Turb. and Power* **130**.
- BAKE, F., MICHEL, U. & ROHLE, I. 2007 Investigation of entropy noise in aero-engine combustors. In *Transaction of the ASME - 129*.
- BAKE, F., MICHEL, U., ROHLE, I., RICHTER, C., THIELE, F., LIU, M. & NOLL., B. 2005 Indirect combustion noise generation in gas turbines. In *11th AIAA/CEAS Aeroacoustics Conference - AIAA 2005-2830*.
- COLIN, O. & RUDGYARD, M. 2000 Development of high-order Taylor-Galerkin schemes for unsteady calculations. *J. Comput. Phys.* **162** (2), 338–371.
- CUMPSTY, N. & MARBLE, F. 1977 The interaction of entropy fluctuations with turbine blade rows ; a mechanism of turbojet engine noise. *Proc. R. Soc. Lond.* **357**, 323–344.
- IHME, M., PITSCH, H. & BODONY, D. 2008 Radiation of noise in turbulent non-premixed flames. In *In Proc. of the Combustion Institute*.
- LEYKO, M., NICOUD, F. & POINSOT, T. 2007 Comparison of indirect and direct combustion noise in aircraft engines. In *11th CEAS-ASC Workshop of X3-Noise*.
- MAHESH, K., LEE, S., LELE, S. & MOIN, P. 1995 The interaction of an isotropic field of acoustic waves with a shock wave. *J. Fluid Mech.* **300**, 383–407.
- MAHESH, K., LELE, S. & MOIN, P. 1997 The influence of entropy fluctuations on the interaction of turbulence with a shock. *J. Fluid Mech.* **334**, 353–379.
- MARBLE, F. & CANDEL, S. 1977 Acoustic disturbances from gas nonuniformities connected through a nozzle. *J. Sound Vibration* **55**, 225–243.

- MOASE, W., BREAR, M. & MANZIE, C. 2007 The forced response of choked nozzles and supersonic diffusers. *J. Fluid Mech.* **585**, 281–304.
- MUTHUKRISHNAN, M., STRAHLE, W. & NEALE, D. 1978 Separation of hydrodynamic, entropy, and combustion noise in a gas turbine combustor. *AIAA Journal* **16** (4), 320–327.
- PICKETT, G. F. 1975 Core engine noise due to temperature fluctuations convecting through turbine blade rows. In *2nd AIAA Aeroacoustics Conference - AIAA 1975-528*.
- POINSOT, T. & LELE, S. 1992 Boundary conditions for direct simulations of compressible viscous flows. *J. Comput. Phys.* **101** (1), 104–129.
- SELLE, L., NICOUD, F. & POINSOT, T. 2004 The actual impedance of non-reflecting boundary conditions: implications for the computation of resonators. *AIAA Journal* **42** (5), 958–964.